COMPUTERS & STRUCTURES, INC.

STRUCTURAL AND EARTHQUAKE ENGINEERING SOFTWARE

Reinforced Slab Design Manual

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Integrated Building Design Software





Reinforced Concrete Slab Design Manual

For ETABS® 2016

ISO ETA122815M62 Rev.0 Proudly developed in the United States of America

July 2016

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Chapter 1 Introduction

ETABS automates several slab and mat design tasks. Specifically, it integrates slab design moments across design strips and designs the required reinforcement; it checks slab punching shear around column supports and concentrated loads; and it designs shear link and shear stud if needed. The actual design algorithms vary based on the specific design code chosen by the user. This manual describes the algorithms used for the various codes.

It should be noted that the design of reinforced concrete slabs is a complex subject and the design codes cover many aspects of this process. ETABS is a tool to help the user in this process. Only the aspects of design documented in this manual are automated by ETABS design capabilities. The user must check the results produced and address other aspects not covered by ETABS.

1.1 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method. As an alternative to this strip based method, ETABS also offers a FEM based design, which is useful for irregular slabs where strip based techniques may not be appropriate.

1.2 Design Strips

ETABS provides two principal strip layers used for design, namely Layer A design strips and Layer B design strips. The strips are defined as polylines with associated widths that can vary along the length of the strip.

The strips need not be mutually perpendicular. The extent of the design strips is defined by the edges of the area objects defining the slab, and strips can overlap if needed. The location of the design strips is usually governed by the support or grid locations. Design strips may be defined as either Column Strips or Middle Strips – models with post-tensioning typically have column strips only.

1.3 Integration of Moments – Wood-Armer

Use of the Wood-Armer method for the integration of design moments results in the following steps:

For a particular combination or load case, for each finite element within the design strip, ETABS calculates the design moments per unit width using the internal forces. Internal forces are converted to design moments per unit width in the following manner:

$$m_{bB} = m_B + |m_{AB}|$$
$$m_{bA} = m_A + |m_{AB}|$$
$$m_{tB} = m_B + |m_{AB}|$$
$$m_{tB} = m_A + |m_{AB}|$$

where m_A , m_B , and m_{AB} are internal moments per unit width, and m_{bA} and m_{bB} are design moments per unit width for the bottom of the slab in the A and B directions, respectively, and m_{tA} and m_{tB} are the design moments for the top of the slab in the A and B directions, respectively. Design moments may be factored combinations for strength design, or unfactored moments for service load checks

when post-tensioning is present. The design moments calculated using the Wood-Armer integration will most likely not completely satisfy equilibrium of the applied loads, but for a mesh that accurately captures the overall behavior of the slab, this integration scheme provides a good design. This is the case because the Wood-Armer integration scheme effectively calculates design moments when cracking occurs diagonally to the design strip directions.

1.4 Required Reinforcement – Strip Based

The design of the mild reinforcement for slabs is carried out for a particular strip at each transverse mesh line location along the length of the strip. The moments are integrated across all elements of like property in the strip to determine the factored design moments. The required reinforcement for slabs is computed for each set of elements with the same property type, and then summed to give the total required reinforcement for the strip. The maximum required top and bottom strip reinforcement for a particular mesh line is obtained, along with the corresponding controlling combinations.

As an option, minimum reinforcement requirements may be enforced in accordance with the selected design code.

1.5 Required Reinforcement – FEM Based

The FEM Based design determines the required reinforcement on an elementby-element basis and is therefore independent of design strips. Several options are available for refining the display of the required reinforcement, including averaging, which will flatten peaks and provide an averaged required reinforcement over a particular area of the slab.

1.6 Slab Punching Shear Check

The distribution of stresses close to concentrated loads or reaction points in reinforced and prestressed concrete slabs is quite complex. Punching shear is one particular failure mode recognized by design codes for which an elastic plate bending analysis may not provide adequate stress distribution. Most codes use empirical methods based on experimental verification to check against punching shear failures. ETABS automates this check for common geometries. If the check results in a punching shear ratio greater than unity (i.e., punching failure), ETABS will design punching shear reinforcement. The ETABS procedure for the punching shear check carried out for each column, for each design combination is as follows:

Locate the critical section around the column or point load. ETABS reports whether it assumed the column to be an interior, edge, or corner column. This determination is based on whether the slab is present within 10 times the slab thickness along the column edges. A column is classified as a corner column when two slab edges are found within 10 times the slab thickness. A column with only one slab edge within 10 times the slab thickness is classified as an edge column, and a column is classified as interior when no slab edges are found within 10 times the slab thickness. For single footings, this determination is based on the minimum area of the critical section.

Check that each slab element in the area enclosed between the face of the column and the critical section for punching shear has the same slab property label. If this is not the case, the minimum slab thickness within the punching shear perimeter is used.

Use the net shear to check punching shear if a point load or column (call it load/column A) is within the critical section for punching shear for another point load or column (call it load/column B).

Calculate punching shear based on net forces in the slab when line objects (beams, walls, or releases) frame into a column.

Calculate the reactive force and moments at the column for the combination. The shear and moment values used in the punching shear check are reduced by the load (or reaction) that is included within the boundaries of the punching shear critical section.

Calculate the distribution of shear stress around the critical section.

Obtain the shear capacity of the critical section.

Compare the shear stress distribution with the shear capacity. The comparison is reported as a ratio for the worst combination. A value above 1.0 indicates failure.

ETABS designs rebar ties or stud rails when such options are activated in the punching shear design overwrites. The details of rebar ties or stud rails are documented in the *Reinforced Concrete Design Manual* and the *Post-Tensioned Concrete Design Manual*.

Design overwrites are available to modify the location type, punching shear perimeter, openings in the slab, and reinforcement pattern, when the punching shear parameters computed need to be changed.

For computing the punching parameters, the following assumptions are used:

Punching shear is calculated for columns punching through a slab or a drop panel. ETABS also checks the drop panel punching through a slab. The effect of column capitals is included in the punching shear calculation.

ETABS uses the effective depth for computing the punching shear. The concrete cover to rebar is taken from the design preferences unless a design strip is present. In that case, the rebar cover is taken from the design strip.

Openings within 10 times the slab thickness are automatically included in the punching shear calculations. The slab edge within the punching zone radius is subtracted from the punching shear perimeter.



Chapter 2 Design for ACI 318-14

This chapter describes in detail the various aspects of the concrete slab design procedure that is used by ETABS when the American code ACI 318-14 [ACI 2014] is selected. Various notations used in this chapter are listed in Table 2-1. For referencing to the pertinent sections or equations of the ACI code in this chapter, a prefix "ACI" followed by the section or equation number is used herein.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on inch-pound-second units. For simplicity, all equations and descriptions presented in this chapter correspond to inch-pound-second units unless otherwise noted.

2.1 Notations

Table 2-1 List of Symbols Used in the ACI 318-14 Code

- A_{cp} Area enclosed by the outside perimeter of the section, sq-in
- A_g Gross area of concrete, sq-in

A_l	Area of longitudinal reinforcement for torsion, sq-in
A_o	Area enclosed by the shear flow path, sq-in
A_{oh}	Area enclosed by the centerline of the outermost closed transverse torsional reinforcement, sq-in
A_s	Area of tension reinforcement, sq-in
A'_s	Area of compression reinforcement, sq-in
A_t/s	Area of closed shear reinforcement per unit length of member for torsion, sq-in/in
A_{v}	Area of shear reinforcement, sq-in
A_v/s	Area of shear reinforcement per unit length, sq-in/in
a	Depth of compression block, in
$a_{\rm max}$	Maximum allowed depth of compression block, in
b	Width of section, in
b_f	Effective width of flange (flanged section), in
b_o	Perimeter of the punching shear critical section, in
b_w	Width of web (flanged section), in
b_1	Width of the punching shear critical section in the direction of bending, in
b_2	Width of the punching shear critical section perpendicular to the di- rection of bending, in
С	Depth to neutral axis, in
d	Distance from compression face to tension reinforcement, in
d'	Distance from compression face to compression reinforcement, in
E_c	Modulus of elasticity of concrete, psi
E_s	Modulus of elasticity of reinforcement, psi
f'_c	Specified compressive strength of concrete, psi

Table 2-1 List of Symbols Used in the ACI 318-14 Code

2 - 2 Notations

Table 2-	I List of Symbols Used in the ACI 318-14 Code
f'_s	Stress in the compression reinforcement, psi
f_y	Specified yield strength of flexural reinforcement, psi
f_{yt}	Specified yield strength of shear reinforcement, psi
h	Overall depth of a section, in
h_{f}	Height of the flange, in
M_u	Factored moment at a section, lb-in
N_u	Factored axial load at a section occurring simultaneously with V_u or T_u , lb
P_u	Factored axial load at a section, lb
p_{cp}	Outside perimeter of concrete cross-section, in
p_h	Perimeter of centerline of outermost closed transverse torsional reinforcement, in
S	Spacing of shear reinforcement along the strip, in
T_{cr}	Critical torsion capacity, lb-in
T_u	Factored torsional moment at a section, lb-in
V_c	Shear force resisted by concrete, lb
$V_{\rm max}$	Maximum permitted total factored shear force at a section, lb
V_s	Shear force resisted by transverse reinforcement, lb
V_u	Factored shear force at a section, lb
α_s	Punching shear scale factor based on column location
eta_c	Ratio of the maximum to the minimum dimensions of the punching shear critical section
β_l	Factor for obtaining depth of the concrete compression block
\mathcal{E}_{C}	Strain in the concrete
$\mathcal{E}_{c \max}$	Maximum usable compression strain allowed in the extreme concrete fiber, (0.003 in/in)

Notations 2 - 3

Table 2-1 List of Sy	ymbols Used in the	ACI 318-14 Code
----------------------	--------------------	-----------------

- \mathcal{E}_s Strain in the reinforcement
- $\mathcal{E}_{s,\min}$ Minimum tensile strain allowed in the reinforcement at nominal strength for tension controlled behavior (0.005 in/in)
- ϕ Strength reduction factor
- γ_{f} Fraction of unbalanced moment transferred by flexure
- γ_{ν} Fraction of unbalanced moment transferred by eccentricity of shear
- λ Shear strength reduction factor for light-weight concrete
- θ Angle of compression diagonals, degrees

2.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For ACI 318-14, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (ACI 5.3.1):

1.4D	(ACI Eqn. 5.3.1a)
$1.2D + 1.6L + 0.5L_r$	(ACI Eqn.5.3.1b)
$1.2D + 1.0L + 1.6L_r$	(ACI Eqn.5.3.1c)
$1.2D + 1.6(0.75 PL) + 0.5L_r$	(ACI Eqn.5.3.1b, 6.4)
1.2D + 1.6L + 0.5S	(ACI Eqn.5.3.1b)
1.2D + 1.0L + 1.6S	(ACI Eqn.5.3.1c)
$0.9D \pm 1.0W$	(ACI Eqn.5.3.1f)
$1.2D + 1.0L + 0.5L_r \pm 1.0W$	(ACI Eqn.5.3.1d)
$1.2D+1.6L_r\pm0.5W$	(ACI Eqn.5.3.1c)
$1.2D + 1.6S \pm 0.5W$	(ACI Eqn.5.3.1c)
$1.2D + 1.0L + 0.5S \pm 1.0W$	(ACI Eqn.5.3.1d)

2 - 4 Design Load Combinations

$0.9D \pm 1.0E$	(ACI Eqn.5.3.1g)
$1.2D + 1.0L + 0.2S \pm 1.0E$	(ACI Eqn.5.3.1e)

These are the default design load combinations in ETABS whenever the ACI 318-14 code is used. The user should use other appropriate load combinations if roof live load is treated separately, or if other types of loads are present.

2.3 Limits on Material Strength

The concrete compressive strength, f'_c , should not be less than 2,500 psi (ACI 19.2.1, Table 19.2.1.1). The upper limit of the reinforcement yield strength, f_y , is taken as 80 ksi (ACI 20.2.2.4a, Table 20.2.2.4a) and the upper limit of the reinforcement shear strength, f_{yt} , is taken as 60 ksi (ACI 21.2.2.4a, Table 21.2.2.4a).

If the input f'_c is less than 2,500 psi, ETABS continues to design the members based on the input f'_c and does not warn the user about the violation of the code. The user is responsible for ensuring that the minimum strength is satisfied.

2.4 Strength Reduction Factors

The strength reduction factors, ϕ , are applied to the specified strength to obtain the design strength provided by a member. The ϕ factors for flexure, shear, and torsion are as follows:

$\phi = 0.90$ for flexure (tension controlled)	(ACI 21.2.1, Table 21.2.1)
$\phi = 0.75$ for shear and torsion	(ACI 21.2.1, Table 21.2.1)

These values can be overwritten; however, caution is advised.

2.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

2.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.

These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

2.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

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The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

2.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete. Note that the flexural reinforcement strength, f_y , is limited to 80 ksi (ACI 20.2.2.4a), even if the material property is defined using a higher value.

The design procedure is based on the simplified rectangular stress block, as shown in Figure 2-1 (ACI 22.2.2). Furthermore, it is assumed that the net tensile strain in the reinforcement shall not be less than 0.005 (tension controlled) (ACI 21.2.2, Table 21.2.2) when the concrete in compression reaches its assumed strain limit of 0.003. When the applied moment exceeds the moment capacity at this design condition, the area of compression reinforcement is calculated assuming that the additional moment will be carried by compression reinforcement and additional tension reinforcement.

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed $(0.1f'_cA_g)$ (ACI 9.5.2.1), axial force is ignored; hence, all slab are designed for major direction flexure, shear, and punching check only. Axial compression greater than $(0.1f'_cA_g)$ and axial tensions are always included in flexural and shear design.

2.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive moment, M_u (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 2-1), where,

$$a = d - \sqrt{d^2 - \frac{2|M_u|}{0.85f'_c \phi b}}$$
(ACI 22.2.2)

and the value of ϕ is taken as that for a tension-controlled section, which by default is 0.90 (ACI 9.3.2.1) in the preceding and the following equations.

The maximum depth of the compression zone, c_{max} , is calculated based on the limitation that the tension reinforcement strain shall not be less than $\varepsilon_{\text{smin}}$, which is equal to 0.005 for tension controlled behavior (ACI 21.2.2, Table 21.2.2):





Figure 2-1 Uniform Thickness Slab Design

where,

$$\varepsilon_{cmax} = 0.003$$
 (ACI 21.2.2, Fig R21.2)
 $\varepsilon_{smin} = 0.005$ (ACI 21.2.2, Fig R21.2.26)

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \beta_l c_{\max} \tag{ACI 22.2.2.4.1}$$

where β_l is calculated as:

$$\beta_1 = 0.85 - 0.05 \left(\frac{f'_c - 4000}{1000} \right), \qquad 0.65 \le \beta_I \le 0.85 \quad (\text{ACI } 22.2.2.4.3)$$

• If $a \le a_{\text{max}}$ (ACI 10.3.4), the area of tension reinforcement is then given by:

$$A_s = \frac{M_u}{\phi f_y \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M_u is positive, or at the top if M_u is negative.

- If $a > a_{\text{max}}$, compression reinforcement is required (ACI 9.3.3.1, 21.2.2, Fig 21.2.26, 22.2.2.4.1) and is calculated as follows:
 - The compressive force developed in the concrete alone is given by:

$$C = 0.85 f'_c ba_{\text{max}}$$
 (ACI 22.2.2.4.1)

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{uc} = \phi C \left(d - \frac{a_{\max}}{2} \right)$$

- Therefore the moment required to be resisted by compression reinforcement and tension reinforcement is:

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$$M_{us} = M_u - M_{uc}$$

- The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{us}}{\phi(f'_{s} - 0.85f'_{c})(d - d')}, \text{ where}$$

$$f'_{s} = E_{s} \varepsilon_{c \max} \left[\frac{c_{\max} - d'}{c_{\max}} \right] \le f_{y} \text{ (ACI } 9.2.1.2, 9.5.2.1, 20.2.2, 22.2.1.2)}$$

- The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{uc}}{\phi f_y \left[d - \frac{a_{\max}}{2} \right]}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{us}}{\phi f_y (d - d')}$$

Therefore, the total tension reinforcement is $A_s = A_{s1} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M_u is positive, and vice versa if M_u is negative.

2.5.1.2.2 Design of nonuniform thickness slab

In designing a nonuniform thickness slab, a simplified stress block, as shown in Figure 2-2, is assumed if the flange is under compression, i.e., if the moment is positive. If the moment is negative, the flange comes under tension, and the flange is ignored. In that case, a simplified stress block similar to that shown in Figure 2-1 is assumed on the compression side.

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Figure 2-2 Nonuniform Thickness Slab Design

2.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_u (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

2.5.1.2.2.2 Flanged Slab Section Under Positive Moment

If $M_u > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M_u}{0.85 f'_c \phi b_f}}$$
(ACI 22.2)

where, the value of ϕ is taken as that for a tension-controlled section, which by default is 0.90 (ACI 21.2.1, 21.2.2, Table 21.2.1, Table 21.2.2) in the preceding and the following equations.

The maximum depth of the compression zone, c_{max} , is calculated based on the limitation that the tension reinforcement strain shall not be less than $\varepsilon_{\text{smin}}$, which is equal to 0.005 for tension controlled behavior (ACI 9.3.3.1, 21.2.2, Fig 21.2.26):

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$$c_{\max} = \frac{\varepsilon_{c\max}}{\varepsilon_{c\max} + \varepsilon_{s\min}} d \qquad (ACI 22.2.1.2)$$

where,

$$\varepsilon_{\rm cmax} = 0.003$$
 (ACI 21.2.2, Fig 21.2.26)

$$\varepsilon_{\rm smin} = 0.005$$
 (ACI 21.2.2, Fig 21.2.26)

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \beta_1 c_{\max}$$
 (ACI 22.2.2.4.11)

where β_l is calculated as:

$$\beta_1 = 0.85 - 0.05 \left(\frac{f'_c - 4000}{1000} \right), \qquad 0.65 \le \beta_1 \le 0.85 \quad (\text{ACI } 22.2.2.4.3)$$

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the rectangular uniform slab design. However, in this case, the width of the slab is taken as b_f . Compression reinforcement is required if $a > a_{max}$.
- If a > h_f, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f, and the second part is for balancing the compressive force from the web, C_w, as shown in Figure 2-2. C_f is given by:

$$C_f = 0.85 f'_c (b_f - b_w) \min(h_f, a_{\max})$$
 (ACI 22.2.2.4.1)

Therefore, $A_{s1} = \frac{C_f}{f_y}$ and the portion of M_u that is resisted by the flange is

given by:

$$M_{uf} = \phi C_f \left(d - \frac{\min(h_f, a_{\max})}{2} \right)$$

Again, the value for ϕ is 0.90 by default. Therefore, the balance of the moment, M_u , to be carried by the web is:

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$$M_{uw} = M_u - M_{uf}$$

The web is a rectangular section with dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{uw}}{0.85f'_c \phi b_w}}$$
(ACI 22.2)

• If $a_1 \le a_{\text{max}}$ (ACI 9.3.3.1, 21.2.2), the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_{uw}}{\phi f_y \left(d - \frac{a_1}{2}\right)}, \text{ and}$$

 $A_s = A_{s1} + A_{s2}$

This reinforcement is to be placed at the bottom of the flanged slab section.

• If $a_1 > a_{\text{max}}$, compression reinforcement is required (ACI 9.3.3.1, 21.2.2, Fig 21.2.2b, 22.2.2.4.1) and is calculated as follows:

- The compressive force in the web concrete alone is given by:

$$C_w = 0.85 f'_c b_w a_{\text{max}}$$
 (ACI 22.2.2.4.1)

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{uc} = C_w \left(d - \frac{a_{\max}}{2} \right) \phi$$

and the moment resisted by compression and tension reinforcement is:

$$M_{us} = M_{uw} - M_{uc}$$

Therefore, the compression reinforcement is computed as:

$$A'_{s} = \frac{M_{us}}{(f'_{s} - 0.85f'_{c})(d - d')\phi}, \text{ where }$$

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$$f'_{s} = E_{s} \varepsilon_{c \max} \left[\frac{c_{\max} - d'}{c_{\max}} \right] \le f_{y}$$
 (ACI 9.2.1.2, 9.5.2.1, 20.2.2, 22.2.1.2)

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{uc}}{f_y \left[d - \frac{a_{\max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{us}}{f_y(d-d')\phi}$$

The total tension reinforcement is $A_s = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

2.5.1.3 Minimum and Maximum Slab Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (ACI 7.6.1.1, 8.6.1.1):

$A_{s,\min} = 0.0020 \ bh \ \text{for} \ f_y < 60 \ \text{ksi}$	(ACI Table 7.6.1.1, Table 8.6.1.1)
$A_{s,\min} = 0.0018 \ bh \ for f_y = 60 \ ksi$	(ACI Table 7.6.1.1, Table 8.6.1.1)
$A_{s,\min} = \frac{0.0018 \times 60000}{f_y} bh \text{ for } f_y > 60$	ksi(ACI Table 7.6.1.1, Table
8.6.1.1)	

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

2.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip,

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for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V_u.
- Determine the shear force, *V_c*, that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

2.5.2.1 Determine Factored Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

2.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_c , is calculated as:

$$V_c = 2\lambda \sqrt{f'_c} b_w d \qquad (\text{ACI } 22.5.5.1)$$

A limit is imposed on the value of $\sqrt{f'_c}$ as $f'_c \le 100$ (ACI 22.5.3.1)

The value of λ should be specified in the material property definition.

2.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\rm max} = V_c + \left(8\sqrt{f'_c}\right)b_w d$$
 (ACI 22.5.1.2)

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows where, ϕ , the strength reduction factor, is 0.75 (ACI 9.3.2.3). The flexural reinforcement strength, f_{yt} , is limited to 60 ksi (ACI 11.5.2) even if the material property is defined with a higher value.

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• If
$$V_u \le \phi V_c$$
,

$$\frac{A_v}{s} = 0$$
(ACI 9.6.3.1)

• If
$$\phi V_c < V_u \le \phi V_{\max}$$
,

$$\frac{A_v}{s} = \frac{\left(V_u - \phi V_c\right)}{\phi f_{yt} d}$$
(ACI 22.5.1.1, 22.5.10.1, 20.5.10.5.3)

• If $V_u > \phi V_{\text{max}}$, a failure condition is declared. (ACI 22.5.1.2)

If V_u exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size (ACI 22.5.1.2).

The minimum shear reinforcement given by ACI 9.6.3.3.

$$\frac{A_{v}}{s} \ge \max\left(\frac{0.75\sqrt{f'_{c}}}{f_{yt}}b_{w}, \frac{50b_{w}}{f_{yt}}\right)$$
(ACI 9.6.3.3, Table 9.6.3.3)

The maximum of all of the calculated A_v/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

2.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

2.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (ACI 22.6.4.2). For rectangular columns and concentrated

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loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (ACI 22.6.4.3). Figure 2-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge or corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 2-3 Punching Shear Perimeters

2.5.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be $\gamma_f M_{sc}$ and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $\gamma_v M_{sc}$.

$$\gamma_{f} = \frac{1}{1 + (2/3)\sqrt{b_{1}/b_{2}}}$$
(ACI 8.4.2.3)

$$\gamma_{v} = 1 - \gamma_{f}$$
(ACI 8.4.2.2)

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For reinforced concrete slabs, γ_f is permitted to increase to the maximum modified values provided in ACI Table 8.4.2.3.4 provided that the limitations on v_{ug} and ε_t given in ACI Table 8.4.2.3.4 are satisfied.

Column	Span	V_{ug}	\mathbf{E}_t	Maximum modified γ_f
Location	Direc-			
	tion			
Corner	Either	$\leq 0.5 \phi v_c$	≥0.004	1.0
column	direction			
	Perpen-	$\leq 0.75 \phi v_c$	≥0.004	1.0
	dicular			
Edge	to the			
column	edge			
	Parallel	$\leq 0.4 \phi v_c$	≥0.010	1.25
	to			$\gamma_f - \frac{1}{1 + (2/3)\sqrt{b_1/b_2}} \le 1.0$
	the edge			$(\gamma - \mathbf{y} \mathbf{v} - 1) = 2$
Interior	Either	$\leq 0.4 \phi v_c$	≥0.010	$\gamma = \frac{1.25}{1.25} \le 1.0$
column	direction			$1 + (2/3)\sqrt{b_1/b_2} \le 1.0$

where b_1 is the width of the critical section measured in the direction of the span and b_2 is the width of the critical section measured in the direction perpendicular to the span.

2.5.3.3 Determine Concrete Capacity

The concrete punching shear stress capacity is taken as the minimum of the following three limits:

$$v_{c} = \min \begin{cases} \left(2 + \frac{4}{\beta_{c}}\right) \lambda \sqrt{f_{c}'} \\ \left(2 + \frac{\alpha_{s}d}{b_{o}}\right) \lambda \sqrt{f_{c}'} \\ 4\lambda \sqrt{f_{c}'} \end{cases}$$
(ACI 22.6.5.2)

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where, β_c is the ratio of the maximum to the minimum dimensions of the critical section, b_o is the perimeter of the critical section, and α_s is a scale factor based on the location of the critical section.

	40	for interior columns,	
$\alpha_s = \langle$	30	for edge columns, and	(ACI 22.6.65.3)
	20	for corner columns.	

A limit is imposed on the value of $\sqrt{f'_c}$ as:

$$\sqrt{f'_c} \le 100$$
 (ACI 22.5.3.1)

2.5.3.4 Computation of Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v_{U} = \frac{V_{U}}{b_{0}d} + \frac{\gamma v_{2}[M_{U2} - V_{U}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{U3} - V_{U}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 2

$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 4

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The equations for \overline{I}_{22} , \overline{I}_{33} , and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 2-axis or parallel to the 3-axis. Refer to Figure 2-4.

$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for the side of the critical section parallel
to the 2-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2, \text{ for the side of the critical section}$$

parallel to the 3-axis Eq. 5b

$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - x_3)^2$$
, for the side of the critical section
parallel to the 2-axis Eq. 6a

$$\overline{I}_{33} = Ld(x_2 - x_3)^2$$
, for the side of the critical section parallel
to the 3-axis Eq. 6b

$$\overline{I}_{23} = Ld(x_2 - x_3)(y_2 - y_3)$$
, for side of critical section parallel
to 2-axis or 3-axis Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

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Figure 2-4 Shear Stress Calculations at Critical Sections

where,

- b_0 = Perimeter of the critical section for punching shear
- d = Effective depth at the critical section for punching shear based on the average of d for 2 direction and d for 3 direction
- I_{22} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 2-axis
- I_{33} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of the inertia of the critical section for punching shear with respect to the 2 and 3 planes

- L = Length of the side of the critical section for punching shear currently being considered
- M_{U2} = Moment about the line parallel to the 2-axis at the center of the column (positive in accordance with the right-hand rule)
- M_{U3} = Moment about the line parallel to the 3-axis at the center of the column (positive in accordance with the right-hand rule)
- v_U = Punching shear stress
- V_U = Shear at the center of the column (positive upward)
- x_1, y_1 = Coordinates of the column centroid
- x_2, y_2 = Coordinates of the center of one side of the critical section for punching shear
- x_3, y_3 = Coordinates of the centroid of the critical section for punching shear
- x_4 , y_4 = Coordinates of the location where stress is being calculated
- γ_{V2} = Percent of M_{U2} resisted by shear
- γ_{V3} = Percent of M_{U3} resisted by shear

2.5.3.5 Determine Capacity Ratio

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section. The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

2.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 6 inches, and not less than 16 times the shear reinforcement bar diameter (ACI 22.6.7.1). If the slab

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thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is described in the subsections that follow.

2.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is limited to:

$$v_c \le 2\lambda \sqrt{f'_c}$$
 for shear links (ACI 22.6.6.1)
 $v_c \le 3\lambda \sqrt{f'_c}$ for shear studs (ACI 22.6.6.1)

2.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\text{max}} = 6\sqrt{f'_c} b_o d$$
 for shear links (ACI 22.6.6.2)

$$V_{\text{max}} = 8\sqrt{f'_c} b_o d$$
 for shear studs (ACI 22.6.6.2)

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows, where, ϕ , the strength reduction factor, is 0.75 (ACI 9.3.2.3).

$$\frac{A_{v}}{s} = \frac{(V_{u} - \phi V_{c})}{\phi f_{ys} d}$$
(ACI 22.5.1.1, 22.5.10.1, 20.5.10.5.3)
$$\frac{A_{v}}{s} \ge \frac{2\sqrt{f'_{c}}b_{o}}{f_{y}}$$
for shear studs

• If $V_u > \phi V_{\text{max}}$, a failure condition is declared. (ACI 22.5.1.2)

• If V_u exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size.

2.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 2-5 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 2-5 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2(ACI 8.7.6.3, Table 8.7.6.3) and the spacing between shear reinforcement shall not exceed d/2(ACI 8.7.6.3, Table 8.7.6.3). The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2*d* measured in a direction parallel to the column face (ACI 8.7.6.3, Table 8.7.6.3).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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2.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in 20.6.1.3 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 3/8-, 1/2-, 5/8-, and 3/4-inch diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d*, and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$$s_{o} \leq 0.5d$$
 (ACI 8.7.7.1.2)
$$s \leq \begin{cases} 0.75d & \text{for} \\ 0.50d & \text{for} \end{cases} v_{u} \leq 6\phi \sqrt{f'_{c}}$$
 (ACI 8.7.7.1.2)

 $g \le 2d$ (ACI 8.7.7.1.2)

The limits of s_o and the spacing, s, between for the links are specified as:

$s_o \leq 0.5d$	(ACI 8.7.6.3)
$s \le 0.50d$	(ACI 8.7.6.3)

Chapter 03 Design for ACI 318-11

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the American code ACI 318-11 [ACI 2011] is selected. Various notations used in this chapter are listed in Table 3-1. For referencing to the pertinent sections or equations of the ACI code in this chapter, a prefix "ACI" followed by the section or equation number is used herein.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on inch-pound-second units. For simplicity, all equations and descriptions presented in this chapter correspond to inch-pound-second units unless otherwise noted.

3.1 Notations

Table 3-1 List of Symbols Used in the ACI 318-11 Code

- A_{cp} Area enclosed by the outside perimeter of the section, sq-in
- A_g Gross area of concrete, sq-in

Table 3-	-1 List of Symbols Used in the ACI 318-11 Code
A_l	Area of longitudinal reinforcement for torsion, sq-in
A_o	Area enclosed by the shear flow path, sq-in
A_{oh}	Area enclosed by the centerline of the outermost closed transverse torsional reinforcement, sq-in
A_s	Area of tension reinforcement, sq-in
A'_s	Area of compression reinforcement, sq-in
A_t/s	Area of closed shear reinforcement per unit length of member for torsion, sq-in/in
A_{v}	Area of shear reinforcement, sq-in
A_v/s	Area of shear reinforcement per unit length, sq-in/in
а	Depth of compression block, in
$a_{\rm max}$	Maximum allowed depth of compression block, in
b	Width of section, in
b_{f}	Effective width of flange (flanged section), in
b_o	Perimeter of the punching shear critical section, in
b_w	Width of web (flanged section), in
b_1	Width of the punching shear critical section in the direction of bending, in
b_2	Width of the punching shear critical section perpendicular to the di- rection of bending, in
С	Depth to neutral axis, in
d	Distance from compression face to tension reinforcement, in
d'	Distance from compression face to compression reinforcement, in
E_c	Modulus of elasticity of concrete, psi
E_s	Modulus of elasticity of reinforcement, psi
f'	Specified compressive strength of concrete nsi

 f'_c Specified compressive strength of concrete, psi

3 - 2 Notations

Table 3-	I List of Symbols Used in the ACI 318-11 Code
f'_s	Stress in the compression reinforcement, psi
f_y	Specified yield strength of flexural reinforcement, psi
f_{yt}	Specified yield strength of shear reinforcement, psi
h	Overall depth of a section, in
h_{f}	Height of the flange, in
M_u	Factored moment at a section, lb-in
N _u	Factored axial load at a section occurring simultaneously with V_u or T_u , lb
P_u	Factored axial load at a section, lb
p_{cp}	Outside perimeter of concrete cross-section, in
p_h	Perimeter of centerline of outermost closed transverse torsional reinforcement, in
S	Spacing of shear reinforcement along the strip, in
T_{cr}	Critical torsion capacity, lb-in
T_u	Factored torsional moment at a section, lb-in
V_c	Shear force resisted by concrete, lb
$V_{\rm max}$	Maximum permitted total factored shear force at a section, lb
V_s	Shear force resisted by transverse reinforcement, lb
V_u	Factored shear force at a section, lb
α_s	Punching shear scale factor based on column location
eta_c	Ratio of the maximum to the minimum dimensions of the punching shear critical section
β_l	Factor for obtaining depth of the concrete compression block
\mathcal{E}_{C}	Strain in the concrete
$\mathcal{E}_{c \max}$	Maximum usable compression strain allowed in the extreme concrete fiber, (0.003 in/in)

Notations 3 - 3

Table 3-1	List of Symbols Used in the ACI 318-11 Code
\mathcal{E}_{s}	Strain in the reinforcement
$\mathcal{E}_{s,\min}$	Minimum tensile strain allowed in the reinforcement at nominal strength for tension controlled behavior (0.005 in/in)
ϕ	Strength reduction factor
γŗ	Fraction of unbalanced moment transferred by flexure
γ_{v}	Fraction of unbalanced moment transferred by eccentricity of shear
λ	Shear strength reduction factor for light-weight concrete
θ	Angle of compression diagonals, degrees

_

Design Load Combinations 3.2

> The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For ACI 318-11, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (ACI 9.2.1):

1.4D	(ACI 9-1)
1.2D + 1.6L	(ACI 9-2)
1.2D + 1.6 (0.75 PL)	(ACI 13.7.6.3, 9-2)
$0.9D \pm 1.0W$	(ACI 9-6)
$1.2D + 1.0L \pm 1.0W$	(ACI 9-4)
$0.9D \pm 1.0E$	(ACI 9-7)
$1.2D + 1.0L \pm 1.0E$	(ACI 9-5)
1.2D + 1.6L + 0.5S	(ACI 9-2)
1.2D + 1.0L + 1.6S	(ACI 9-3)
1.2D + 1.6S + 0.5W	(ACI 9-3)
$1.2D + 1.0L + 0.5S \pm 1.0W$	(ACI 9-4)
$1.2D + 1.0L + 0.2S \pm 1.0E$	(ACI 9-5)

Design Load Combinations 3 - 4

These are the default design load combinations in ETABS whenever the ACI 318-11 code is used. The user should use other appropriate load combinations if roof live load is treated separately, or if other types of loads are present.

3.3 Limits on Material Strength

The concrete compressive strength, f'_c , should not be less than 2,500 psi (ACI 5.1.1). The upper limit of the reinforcement yield strength, f_y , is taken as 80 ksi (ACI 9.4) and the upper limit of the reinforcement shear strength, f_{yt} , is taken as 60 ksi (ACI 11.4.2).

If the input f'_c is less than 2,500 psi, ETABS continues to design the members based on the input f'_c and does not warn the user about the violation of the code. The user is responsible for ensuring that the minimum strength is satisfied.

3.4 Strength Reduction Factors

The strength reduction factors, ϕ , are applied to the specified strength to obtain the design strength provided by a member. The ϕ factors for flexure, shear, and torsion are as follows:

$\phi = 0.90$ for flexure (tension controlled)	(ACI 9.3.2.1)
$\phi = 0.75$ for shear and torsion	(ACI 9.3.2.3)

These values can be overwritten; however, caution is advised.

3.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

Limits on Material Strength 3 - 5

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

3.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.

These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

3.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab

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may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

3.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete. Note that the flexural reinforcement strength, f_y , is limited to 80 ksi (ACI 9.4), even if the material property is defined using a higher value.

The design procedure is based on the simplified rectangular stress block, as shown in Figure 3-1 (ACI 10.2). Furthermore, it is assumed that the net tensile strain in the reinforcement shall not be less than 0.005 (tension controlled) (ACI 10.3.4) when the concrete in compression reaches its assumed strain limit of 0.003. When the applied moment exceeds the moment capacity at this design condition, the area of compression reinforcement is calculated assuming that the additional moment will be carried by compression reinforcement and additional tension reinforcement.

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed $(0.1f'_cA_g)$ (ACI 10.3.5), axial force is ignored; hence, all slabs are designed for major direction flexure, shear, and torsion only. Axial compression greater than $(0.1f'_cA_g)$ and axial tensions are always included in flexural and shear design.

3.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive moment, M_u (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 3-1), where,

$$a = d - \sqrt{d^2 - \frac{2|M_u|}{0.85f'_c \phi b}}$$
(ACI 10.2)

and the value of ϕ is taken as that for a tension-controlled section, which by default is 0.90 (ACI 9.3.2.1) in the preceding and the following equations.

The maximum depth of the compression zone, c_{max} , is calculated based on the limitation that the tension reinforcement strain shall not be less than $\varepsilon_{\text{smin}}$, which is equal to 0.005 for tension controlled behavior (ACI 10.3.4):



Figure 3-1 Uniform Thickness Slab Design

where,

 $\varepsilon_{\rm cmax} = 0.003 \tag{ACI 10.2.3}$

 $\varepsilon_{\rm smin} = 0.005$ (ACI 10.3.4)

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The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \beta_l c_{\max} \tag{ACI 10.2.7.1}$$

where β_l is calculated as:

$$\beta_1 = 0.85 - 0.05 \left(\frac{f'_c - 4000}{1000} \right), \qquad 0.65 \le \beta_1 \le 0.85$$
 (ACI 10.2.7.3)

• If $a \le a_{\text{max}}$ (ACI 10.3.4), the area of tension reinforcement is then given by:

$$A_{s} = \frac{M_{u}}{\phi f_{y} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M_u is positive, or at the top if M_u is negative.

• If *a* > *a*_{max}, compression reinforcement is required (ACI 10.3.5.1) and is calculated as follows:

- The compressive force developed in the concrete alone is given by:

$$C = 0.85 f'_c ba_{\text{max}}$$
 (ACI 10.2.7.1)

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{uc} = \phi C \left(d - \frac{a_{\max}}{2} \right) \tag{ACI 9.3.2.1}$$

- Therefore the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{us} = M_u - M_{uc}$$

- The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{us}}{\phi (f'_{s} - 0.85f'_{c})(d - d')}, \text{ where}$$
$$f'_{s} = E_{s} \varepsilon_{c \max} \left[\frac{c_{\max} - d'}{c_{\max}} \right] \le f_{y} \qquad (\text{ACI 10.2.2, 10.2.3, 10.2.4})$$

- The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{uc}}{\phi f_y \left[d - \frac{a_{\max}}{2} \right]}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{us}}{\phi f_y \left(d - d' \right)}$$

Therefore, the total tension reinforcement is $A_s = A_{sI} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M_u is positive, and vice versa if M_u is negative.

3.5.1.2.2 Design of nonuniform thickness slab

In designing a nonuniform thickness slab, a simplified stress block, as shown in Figure 3-2, is assumed if the flange is under compression, i.e., if the moment is positive. If the moment is negative, the flange comes under tension, and the flange is ignored. In that case, a simplified stress block similar to that shown in Figure 3-1 is assumed on the compression side.

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Figure 3-2 Nonuniform Thickness Slab Design

3.5.1.2.2.1Flanged Slab Under Negative Moment

In designing for a factored negative moment, M_u (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

3.5.1.2.2.2Flanged Slab Under Positive Moment

If $M_u > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M_u}{0.85 f'_c \phi b_f}}$$
(ACI 10.2)

where, the value of ϕ is taken as that for a tension-controlled section, which by default is 0.90 (ACI 9.3.2.1) in the preceding and the following equations.

The maximum depth of the compression zone, c_{max} , is calculated based on the limitation that the tension reinforcement strain shall not be less than $\varepsilon_{\text{smin}}$, which is equal to 0.005 for tension controlled behavior (ACI 10.3.4):

$$c_{\max} = \frac{\varepsilon_{c\max}}{\varepsilon_{c\max} + \varepsilon_{s\min}} d$$
(ACI 10.2.2)

where,

$$\varepsilon_{\rm cmax} = 0.003$$
 (ACI 10.2.3)

$$\varepsilon_{\rm smin} = 0.005$$
 (ACI 10.3.4)

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \beta_1 c_{\max} \tag{ACI 10.2.7.1}$$

where β_l is calculated as:

$$\beta_1 = 0.85 - 0.05 \left(\frac{f'_c - 4000}{1000} \right), \qquad 0.65 \le \beta_I \le 0.85 \quad (\text{ACI } 10.2.7.3)$$

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the rectangular slabdesign. However, in this case, the width of the slab is taken as b_f . Compression reinforcement is required if $a > a_{max}$.
- If a > h_f, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f, and the second part is for balancing the compressive force from the web, C_w, as shown in Figure 3-2. C_f is given by:

$$C_f = 0.85 f'_c (b_f - b_w) \min(h_f, a_{\max})$$
 (ACI 10.2.7.1)

Therefore, $A_{s1} = \frac{C_f}{f_y}$ and the portion of M_u that is resisted by the flange is

given by:

$$M_{uf} = \phi C_f \left(d - \frac{\min(h_f, a_{\max})}{2} \right)$$
(ACI 9.3.2.1)

Again, the value for ϕ is 0.90 by default. Therefore, the balance of the moment, M_u , to be carried by the web is:

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$$M_{uw} = M_u - M_{uf}$$

The web is a rectangular section with dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{uw}}{0.85f'_c \phi b_w}}$$
(ACI 10.2)

• If $a_1 \le a_{\text{max}}$ (ACI 10.3.4), the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_{uw}}{\phi f_y \left(d - \frac{a_1}{2}\right)}, \text{ and}$$

$$A_s = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged slab.

- If a₁ > a_{max}, compression reinforcement is required (ACI 10.3.5.1) and is calculated as follows:
 - The compressive force in the web concrete alone is given by:

$$C_w = 0.85 f'_c b_w a_{\text{max}}$$
 (ACI 10.2.7.1)

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{uc} = C_w \left(d - \frac{a_{\max}}{2} \right) \phi$$

and the moment resisted by compression and tension reinforcement is:

$$M_{us} = M_{uw} - M_{uc}$$

Therefore, the compression reinforcement is computed as:

$$A'_{s} = \frac{M_{us}}{(f'_{s} - 0.85f'_{c})(d - d')\phi}, \text{ where}$$

$$f'_{s} = E_{s} \varepsilon_{c \max} \left[\frac{c_{\max} - d'}{c_{\max}} \right] \le f_{y}$$
 (ACI 10.2.2, 10.2.3, 10.2.4)

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{uc}}{f_y \left[d - \frac{a_{\max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{us}}{f_y(d-d')\phi}$$

The total tension reinforcement is $A_s = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

3.5.1.1 Minimum and Maximum Slab Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (ACI 7.12.2, 13.3.1):

$A_{s,\min} = 0.0020 \ bh \ \text{for} \ f_y = 40 \ \text{ksi} \ \text{or} \ 50 \ \text{ksi}$	(ACI 7.12.2.1(a))
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 $A_{s,\min} = 0.0018 \ bh \ \text{for} \ f_y = 60 \ \text{ksi}$ (ACI 7.12.2.1(b))

$$A_{s,\min} = \frac{0.0018 \times 60000}{f_y} bh \text{ for } f_y > 60 \text{ ksi}$$
 (ACI 7.12.2.1(c))

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

3.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip,

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for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V_u.
- Determine the shear force, *V_c*, that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

3.5.2.1 Determine Factored Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

3.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_c , is calculated as:

$$V_c = 2\lambda \sqrt{f'_c} b_w d \qquad (\text{ACI 11.2.1.2})$$

A limit is imposed on the value of $\sqrt{f'_c}$ as $f'_c \le 100$ (ACI 11.1.2)

The value of λ should be specified in the material property definition.

3.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\rm max} = V_c + \left(8\sqrt{f'_c}\right)b_w d$$
 (ACI 11.4.7.9)

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows where, ϕ , the strength reduction factor, is 0.75 (ACI 9.3.2.3). The flexural reinforcement strength, f_{yt} , is limited to 60 ksi (ACI 11.5.2) even if the material property is defined with a higher value.

• If
$$V_u \le \phi V_c$$
,

$$\frac{A_v}{s} = 0$$
(ACI 11.4.6.1)

• If
$$\phi V_c < V_u \le \phi V_{\max}$$
,

$$\frac{A_{v}}{s} = \frac{\left(V_{u} - \phi V_{c}\right)}{\phi f_{yt} d}$$
(ACI 11.4.7.1, 11.4.7.2)

• If $V_u > \phi V_{\text{max}}$, a failure condition is declared. (ACI 11.4.7.9)

If V_u exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size (ACI 11.4.7.9).

The minimum shear reinforcement given by ACI 11.4.6.3 is not enforced (ACI 11.4.6.1).

$$\frac{A_{v}}{s} \ge \max\left(\frac{0.75\sqrt{f'_{c}}}{f_{yt}}b_{w}, \frac{50b_{w}}{f_{yt}}\right)$$
(ACI 11.4.6.3)

The maximum of all of the calculated A_v/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

3.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

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3.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (ACI 11.11.1.2). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (ACI 11.11.1.3). Figure 3-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 3-3 Punching Shear Perimeters

3.5.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be $\gamma_f M_u$ and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $\gamma_v M_u$.

$$\gamma_f = \frac{1}{1 + (2/3)\sqrt{b_1/b_2}}$$
(ACI 13.5.3.2)

$$\gamma_v = 1 - \gamma_f$$
 (ACI 13.5.3.1)

For flat plates, γ_v is determined from the following equations taken from ACI 421.2R-07 *Seismic Design of Punching Shear Reinforcement in Flat Plates* [ACI 2007].

For interior columns,

$$\gamma_{vx} = 1 - \frac{1}{1 + (2/3)\sqrt{l_y/l_x}}$$
(ACI 421.2 C-11)

$$\gamma_{vy} = 1 - \frac{1}{1 + (2/3)\sqrt{l_x/l_y}}$$
(ACI 421.2 C-12)

For edge columns,

 $\gamma_{\nu x}$ = same as for interior columns (ACI 421.2 C-13)

$$\gamma_{vy} = 1 - \frac{1}{1 + (2/3)\sqrt{l_x/l_y - 0.2}}$$
(ACI 421.2 C-14)

$$\gamma_{vy} = 0$$
 when $l_x / l_y \le 0.2$

For corner columns,

$\gamma_{vx} = 0.4$	(ACI 421.2 C-15)
γ_{vy} = same as for edge columns	(ACI 421.2 C-16)

NOTE: Program uses ACI 421.2-12 and ACI 421.2-15 equations in lieu of ACI 421.2 C-14 and ACI 421.2 C-16 which are currently NOT enforced.

where b_1 is the width of the critical section measured in the direction of the span and b_2 is the width of the critical section measured in the direction perpendicular to the span. The values l_x and l_y are the projections of the shear-critical section onto its principal axes, x and y, respectively.

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3.5.3.3 Determine Concrete Capacity

The concrete punching shear stress capacity is taken as the minimum of the following three limits:

$$v_{c} = \min \begin{cases} \left(2 + \frac{4}{\beta_{c}}\right) \lambda \sqrt{f'_{c}} \\ \left(2 + \frac{\alpha_{s}d}{b_{o}}\right) \lambda \sqrt{f'_{c}} \\ 4\lambda \sqrt{f'_{c}} \end{cases}$$
(ACI 11.11.2.1)

where, β_c is the ratio of the maximum to the minimum dimensions of the critical section, b_o is the perimeter of the critical section, and α_s is a scale factor based on the location of the critical section.

$$\alpha_s = \begin{cases} 40 & \text{for interior columns,} \\ 30 & \text{for edge columns, and} \\ 20 & \text{for corner columns.} \end{cases}$$
(ACI 11.11.2.1)

A limit is imposed on the value of $\sqrt{f'_c}$ as:

$$\sqrt{f'_c} \le 100$$
 (ACI 11.1.2)

3.5.3.4 Computation of Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v_{U} = \frac{V_{U}}{b_{0}d} + \frac{\gamma v_{2}[M_{U2} - V_{U}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{U3} - V_{U}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 2

$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 4

The equations for \overline{I}_{22} , \overline{I}_{33} , and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 2-axis or parallel to the 3-axis. Refer to Figure 3-4.

$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for the side of the critical section parallel
to the 2-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2$$
, for the side of the critical section parallel to the 3-axis Eq. 5b

$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - x_3)^2$$
, for the side of the critical section parallel to the 2-axis Eq. 6a

$$\overline{I}_{33} = Ld(x_2 - x_3)^2$$
, for the side of the critical section parallel
to the 3-axis Eq. 6b

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Figure 3-4 Shear Stress Calculations at Critical Sections

$$\overline{I}_{23} = Ld(x_2 - x_3)(y_2 - y_3)$$
, for side of critical section parallel
to 2-axis or 3-axis Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

where,

- b_0 = Perimeter of the critical section for punching shear
- d = Effective depth at the critical section for punching shear based on the average of d for 2 direction and d for 3 direction
- I_{22} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 2-axis

- I_{33} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of the inertia of the critical section for punching shear with respect to the 2 and 3 planes
- L = Length of the side of the critical section for punching shear currently being considered
- M_{U2} = Moment about the line parallel to the 2-axis at the center of the column (positive in accordance with the right-hand rule)
- M_{U3} = Moment about the line parallel to the 3-axis at the center of the column (positive in accordance with the right-hand rule)
- v_U = Punching shear stress
- V_U = Shear at the center of the column (positive upward)
- $x_1, y_1 =$ Coordinates of the column centroid
- x_2, y_2 = Coordinates of the center of one side of the critical section for punching shear
- x_3, y_3 = Coordinates of the centroid of the critical section for punching shear
- x_4, y_4 = Coordinates of the location where stress is being calculated
- γ_{V2} = Percent of M_{U2} resisted by shear
- γ_{V3} = Percent of M_{U3} resisted by shear

3.5.3.5 Determine Capacity Ratio

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section. The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

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3.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 6 inches, and not less than 16 times the shear reinforcement bar diameter (ACI 11.11.3). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is described in the subsections that follow.

3.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is limited to:

$$v_c \le 2\lambda \sqrt{f'_c}$$
 for shear links (ACI 11.11.3.1)

$$v_c \le 3\lambda \sqrt{f'_c}$$
 for shear studs (ACI 11.11.5.1)

3.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\text{max}} = 6\sqrt{f'_c} \ b_o d \text{ for shear links}$$
(ACI 11.11.3.2)
$$V_{\text{max}} = 8\sqrt{f'_c} \ b_o d \text{ for shear studs}$$
(ACI 11.11.5.1)

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows, where, ϕ , the strength reduction factor, is 0.75 (ACI 9.3.2.3).

$$\frac{A_v}{s} = \frac{\left(V_u - \phi V_c\right)}{\phi f_{ys} d}$$
(ACI 11.4.7.1, 11.4.7.2)

$$\frac{A_{v}}{s} \ge \frac{2\sqrt{f_{c}'}b_{o}}{f_{y}} \quad \text{for shear studs} \tag{ACI 11.11.5.1}$$

- If $V_u > \phi V_{\text{max}}$, a failure condition is declared. (ACI 11.11.3.2)
- If V_u exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size.

3.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 3-6 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 3-6 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2(ACI R11.11.3.3, 11.11.5.2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2*d* measured in a direction parallel to the column face (ACI 11.11.3.3).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of

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shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

3.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in ACI 7.7 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 3/8-, 1/2-, 5/8-, and 3/4-inch diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d*, and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

 $s_o \le 0.5d$ (ACI 11.11.5.2)

$$s \leq \begin{cases} 0.75d & \text{for} & v_u \leq 6\phi \sqrt{f'_c} \\ 0.50d & \text{for} & v_u > 6\phi \sqrt{f'_c} \end{cases}$$
(ACI 11.11.5.2)

$$g \le 2d$$
 (ACI 11.11.5.3)

The limits of s_o and the spacing, s, between for the links are specified as:

$s_o \leq 0.5d$	(ACI 11.11.3)
$s \le 0.50d$	(ACI 11.11.3)

Chapter 4 Design for ACI 318-08

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the American code ACI 318-08 [ACI 2008] is selected. Various notations used in this chapter are listed in Table 4-1. For referencing to the pertinent sections or equations of the ACI code in this chapter, a prefix "ACI" followed by the section or equation number is used herein.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on inch-pound-second units. For simplicity, all equations and descriptions presented in this chapter correspond to inch-pound-second units unless otherwise noted.

4.1 Notations

Table 4-1 List of Symbols Used in the ACI 318-08 Code

- A_{cp} Area enclosed by the outside perimeter of the section, sq-in
- A_g Gross area of concrete, sq-in

A_l	Area of longitudinal reinforcement for torsion, sq-in
A_o	Area enclosed by the shear flow path, sq-in
A_{oh}	Area enclosed by the centerline of the outermost closed transverse torsional reinforcement, sq-in
A_s	Area of tension reinforcement, sq-in
A'_s	Area of compression reinforcement, sq-in
A_t/s	Area of closed shear reinforcement per unit length of member for torsion, sq-in/in
A_{v}	Area of shear reinforcement, sq-in
A_v/s	Area of shear reinforcement per unit length, sq-in/in
a	Depth of compression block, in
$a_{\rm max}$	Maximum allowed depth of compression block, in
b	Width of section, in
b_f	Effective width of flange (flanged section), in
b_o	Perimeter of the punching shear critical section, in
b_w	Width of web (flanged section), in
b_1	Width of the punching shear critical section in the direction of bending, in
b_2	Width of the punching shear critical section perpendicular to the di- rection of bending, in
С	Depth to neutral axis, in
d	Distance from compression face to tension reinforcement, in
d'	Distance from compression face to compression reinforcement, in
E_c	Modulus of elasticity of concrete, psi
E_s	Modulus of elasticity of reinforcement, psi
f'_c	Specified compressive strength of concrete, psi

Table 4-1 List of Symbols Used in the ACI 318-08 Code

4 - 2 Notations

Table 4-	1 List of Symbols Used in the ACI 318-08 Code
f'_s	Stress in the compression reinforcement, psi
f_y	Specified yield strength of flexural reinforcement, psi
f_{yt}	Specified yield strength of shear reinforcement, psi
h	Overall depth of a section, in
h_{f}	Height of the flange, in
M_u	Factored moment at a section, lb-in
Nu	Factored axial load at a section occurring simultaneously with V_u or T_u , lb
P_u	Factored axial load at a section, lb
p_{cp}	Outside perimeter of concrete cross-section, in
p_h	Perimeter of centerline of outermost closed transverse torsional reinforcement, in
S	Spacing of shear reinforcement along the strip, in
T_{cr}	Critical torsion capacity, lb-in
T_u	Factored torsional moment at a section, lb-in
V_c	Shear force resisted by concrete, lb
$V_{\rm max}$	Maximum permitted total factored shear force at a section, lb
V_s	Shear force resisted by transverse reinforcement, lb
V_u	Factored shear force at a section, lb
α_{s}	Punching shear scale factor based on column location
eta_c	Ratio of the maximum to the minimum dimensions of the punching shear critical section
β_l	Factor for obtaining depth of the concrete compression block
\mathcal{E}_{C}	Strain in the concrete
$\mathcal{E}_{c \max}$	Maximum usable compression strain allowed in the extreme concrete fiber, (0.003 in/in)

Notations 4 - 3

Table 4-1 List of Symbols Used in the ACI 510-00 Code

- \mathcal{E}_s Strain in the reinforcement
- $\mathcal{E}_{s,\min}$ Minimum tensile strain allowed in the reinforcement at nominal strength for tension controlled behavior (0.005 in/in)
- ϕ Strength reduction factor
- γ_{f} Fraction of unbalanced moment transferred by flexure
- γ_{ν} Fraction of unbalanced moment transferred by eccentricity of shear
- λ Shear strength reduction factor for light-weight concrete
- θ Angle of compression diagonals, degrees

4.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For ACI 318-08, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (ACI 9.2.1):

1.4D	(ACI 9-1)
1.2D + 1.6L	(ACI 9-2)
1.2D + 1.6 (0.75 PL)	(ACI 13.7.6.3, 9-2)
$0.9D \pm 1.6W$ $1.2D + 1.0L \pm 1.6W$	(ACI 9-6) (ACI 9-4)
$0.9D \pm 1.0E$ $1.2D + 1.0L \pm 1.0E$	(ACI 9-7) (ACI 9-5)
$\begin{array}{l} 1.2D + 1.6L + 0.5S \\ 1.2D + 1.0L + 1.6S \\ 1.2D + 1.6S \pm 0.8W \end{array}$	(ACI 9-2) (ACI 9-3) (ACI 9-3)
$1.2D + 1.0L + 0.5S \pm 1.6W$ $1.2D + 1.0L + 0.2S \pm 1.0E$	(ACI 9-4) (ACI 9-5)

4 - 4 Design Load Combinations

These are the default design load combinations in ETABS whenever the ACI 318-08 code is used. The user should use other appropriate load combinations if roof live load is treated separately, or if other types of loads are present.

4.3 Limits on Material Strength

The concrete compressive strength, f'_c , should not be less than 2,500 psi (ACI 5.1.1). If the input f'_c is less than 2,500 psi, ETABS continues to design the members based on the input f'_c and does not warn the user about the violation of the code. The user is responsible for ensuring that the minimum strength is satisfied.

4.4 Strength Reduction Factors

The strength reduction factors, ϕ , are applied to the specified strength to obtain the design strength provided by a member. The ϕ factors for flexure, shear, and torsion are as follows:

$\phi = 0.90$ for flexure (tension controlled)	(ACI 9.3.2.1)
$\phi = 0.75$ for shear and torsion	(ACI 9.3.2.3)

These values can be overwritten; however, caution is advised.

4.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

Design flexural reinforcement

- Design shear reinforcement
- Punching check

4.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

4.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

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4.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete. Note that the flexural reinforcement strength, f_y , is limited to 80 ksi (ACI 9.4), even if the material property is defined using a higher value.

The design procedure is based on the simplified rectangular stress block, as shown in Figure 4-1 (ACI 10.2). Furthermore, it is assumed that the net tensile strain in the reinforcement shall not be less than 0.005 (tension controlled) (ACI 10.3.4) when the concrete in compression reaches its assumed strain limit of 0.003. When the applied moment exceeds the moment capacity at this design condition, the area of compression reinforcement is calculated assuming that the additional moment will be carried by compression reinforcement and additional tension reinforcement.

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T- shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed $(0.1f'_cA_g)$ (ACI 10.3.5), axial force is ignored; hence, all slabs are designed for major direction flexure and shear only. Axial compression greater than $(0.1f'_cA_g)$ and axial tensions are always included in flexural and shear design.

4.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive moment, M_u (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 4-1), where,

$$a = d - \sqrt{d^2 - \frac{2|M_u|}{0.85f'_c \phi b}}$$
(ACI 10.2)

and the value of ϕ is taken as that for a tension-controlled section, which by default is 0.90 (ACI 9.3.2.1) in the preceding and the following equations.

The maximum depth of the compression zone, c_{max} , is calculated based on the limitation that the tension reinforcement strain shall not be less than $\varepsilon_{\text{smin}}$, which is equal to 0.005 for tension controlled behavior (ACI 10.3.4):

$$c_{\max} = \frac{\varepsilon_{c\max}}{\varepsilon_{c\max} + \varepsilon_{s\min}} d$$
 (ACI 10.2.2)



Figure 4-1 Uniform Thickness Slab Design

where,

$$\varepsilon_{\rm cmax} = 0.003$$
 (ACI 10.2.3)

$$\varepsilon_{\rm smin} = 0.005 \tag{ACI 10.3.4}$$

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \beta_l c_{\max} \tag{ACI 10.2.7.1}$$

where β_l is calculated as:

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$$\beta_1 = 0.85 - 0.05 \left(\frac{f'_c - 4000}{1000} \right), \qquad 0.65 \le \beta_l \le 0.85$$
 (ACI 10.2.7.3)

• If $a \le a_{\text{max}}$ (ACI 10.3.4), the area of tension reinforcement is then given by:

$$A_{s} = \frac{M_{u}}{\phi f_{y} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M_u is positive, or at the top if M_u is negative.

If a > a_{max}, compression reinforcement is required (ACI 10.3.5.1) and is calculated as follows:

- The compressive force developed in the concrete alone is given by:

$$C = 0.85 f'_c ba_{\rm max} \tag{ACI 10.2.7.1}$$

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{uc} = \phi C \left(d - \frac{a_{\text{max}}}{2} \right) \tag{ACI 9.3.2.1}$$

- Therefore the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{us} = M_u - M_{uc}$$

- The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{us}}{\phi(f'_{s} - 0.85f'_{c})(d - d')}, \text{ where}$$
$$f'_{s} = E_{s}\varepsilon_{c\max} \left[\frac{c_{\max} - d'}{c_{\max}}\right] \le f_{y} \qquad (\text{ACI 10.2.2, 10.2.3, 10.2.4})$$

- The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{uc}}{\phi f_y \left[d - \frac{a_{\max}}{2} \right]}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{us}}{\phi f_y \left(d - d' \right)}$$

Therefore, the total tension reinforcement is $A_s = A_{s1} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M_u is positive, and vice versa if M_u is negative.

4.5.1.2.2 Design of nonuniform thickness slab

In designing a nonuniform thickness slab, a simplified stress block, as shown in Figure 4-2, is assumed if the flange is under compression, i.e., if the moment is positive. If the moment is negative, the flange comes under tension, and the flange is ignored. In that case, a simplified stress block similar to that shown in Figure 4-1 is assumed on the compression side.

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Figure 4-2 Nonuniform Thickness Slab Design

4.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_u (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

4.5.1.2.2.2 Flanged Slab Section Under Positive Moment

If $M_u > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M_u}{0.85 f'_c \phi b_f}}$$
(ACI 10.2)

where, the value of ϕ is taken as that for a tension-controlled section, which by default is 0.90 (ACI 9.3.2.1) in the preceding and the following equations.

The maximum depth of the compression zone, c_{max} , is calculated based on the limitation that the tension reinforcement strain shall not be less than $\varepsilon_{\text{smin}}$, which is equal to 0.005 for tension controlled behavior (ACI 10.3.4):

$$c_{\max} = \frac{\varepsilon_{c\max}}{\varepsilon_{c\max} + \varepsilon_{s\min}} d$$
(ACI 10.2.2)

where,

$$\varepsilon_{\rm cmax} = 0.003$$
 (ACI 10.2.3)

$$\varepsilon_{\rm smin} = 0.005 \tag{ACI 10.3.4}$$

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \beta_1 c_{\max} \tag{ACI 10.2.7.1}$$

where β_l is calculated as:

$$\beta_1 = 0.85 - 0.05 \left(\frac{f'_c - 4000}{1000} \right), \qquad 0.65 \le \beta_I \le 0.85 \quad (\text{ACI } 10.2.7.3)$$

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in this case, the width of the slab is taken as b_f . Compression reinforcement is required if $a > a_{max}$.
- If $a > h_f$, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 4-2. C_f is given by:

$$C_{f} = 0.85 f'_{c} (b_{f} - b_{w}) \min(h_{f}, a_{\max})$$
 (ACI 10.2.7.1)

Therefore, $A_{s1} = \frac{C_f}{f_y}$ and the portion of M_u that is resisted by the flange is

given by:

$$M_{uf} = \phi C_f \left(d - \frac{\min(h_f, a_{\max})}{2} \right)$$
(ACI 9.3.2.1)

Again, the value for ϕ is 0.90 by default. Therefore, the balance of the moment, M_u , to be carried by the web is:

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$$M_{uw} = M_u - M_{uf}$$

The web is a rectangular section with dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{uw}}{0.85f'_c \phi b_w}}$$
(ACI 10.2)

• If $a_1 \le a_{\text{max}}$ (ACI 10.3.4), the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_{uw}}{\phi f_y \left(d - \frac{a_1}{2}\right)}, \text{ and}$$

$$A_s = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged slab.

- If a₁ > a_{max}, compression reinforcement is required (ACI 10.3.5.1) and is calculated as follows:
 - The compressive force in the web concrete alone is given by:

$$C_w = 0.85 f'_c b_w a_{\text{max}}$$
 (ACI 10.2.7.1)

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{uc} = C_w \left(d - \frac{a_{\max}}{2} \right) \phi$$

and the moment resisted by compression and tension reinforcement is:

$$M_{us} = M_{uw} - M_{uc}$$

Therefore, the compression reinforcement is computed as:

$$A'_{s} = \frac{M_{us}}{(f'_{s} - 0.85f'_{c})(d - d')\phi}, \text{ where}$$

$$f'_{s} = E_{s} \varepsilon_{c \max} \left[\frac{c_{\max} - d'}{c_{\max}} \right] \le f_{y}$$
 (ACI 10.2.2, 10.2.3, 10.2.4)

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{uc}}{f_y \left[d - \frac{a_{\max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{us}}{f_y(d-d')\phi}$$

The total tension reinforcement is $A_s = A_{sl} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

4.5.1.2.3 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (ACI 7.12.2):

$A_{s,\min} = 0.0020 \ bh$ for $f_y = 40 \ ksi$ or 50 ksi	(ACI 7.12.2.1(a))

$$A_{s,\min} = 0.0018 \ bh \ \text{for} \ f_y = 60 \ \text{ksi}$$
 (ACI 7.12.2.1(b))

$$A_{s,\min} = \frac{0.0018 \times 60000}{f_y} bh \text{ for } f_y > 60 \text{ ksi}$$
 (ACI 7.12.2.1(c))

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

4.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip,

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for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V_u.
- Determine the shear force, *V_c*, that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

4.5.2.1 Determine Factored Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

4.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_c , is calculated as:

$$V_c = 2\lambda \sqrt{f'_c b_w d}$$
 (ACI 11.2.1.2, 11.2.1.2, 11.2.2.3)

A limit is imposed on the value of $\sqrt{f'_c}$ as $f'_c \le 100$ (ACI 11.1.2)

The value of λ should be specified in the material property definition.

4.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\rm max} = V_c + \left(8\sqrt{f'_c}\right)b_w d$$
 (ACI 11.4.7.9)

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows where, ϕ , the strength reduction factor, is 0.75 (ACI 9.3.2.3). The flexural reinforcement strength, f_{yt} , is limited to 60 ksi (ACI 11.5.2) even if the material property is defined with a higher value.

• If
$$V_u \le \phi V_c$$
,

$$\frac{A_v}{s} = 0$$
(ACI 11.5.6.1)

• If
$$\phi V_c < V_u \le \phi V_{\max}$$
,

$$\frac{A_{v}}{s} = \frac{\left(V_{u} - \phi V_{c}\right)}{\phi f_{yt} d}$$
(ACI 11.4.7.1, 11.4.7.2)

• If $V_u > \phi V_{\text{max}}$, a failure condition is declared. (ACI 11.4.7.9)

If V_u exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size (ACI 11.4.7.9).

The minimum shear reinforcement given by ACI 11.4.6.3 is not enforced (ACI 11.4.6.1).

$$\frac{A_v}{s} \ge \max\left(\frac{0.75\lambda\sqrt{f'_c}}{f_{yt}}b_w, \frac{50b_w}{f_{yt}}\right)$$
(ACI 11.4.6.3)

The maximum of all of the calculated A_v/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

4.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

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4.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (ACI 11.11.1.2). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (ACI 11.11.1.3). Figure 4-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 4-3 Punching Shear Perimeters

4.5.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be $\gamma_f M_u$ and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $\gamma_v M_u$.

$$\gamma_f = \frac{1}{1 + (2/3)\sqrt{b_1/b_2}}$$
(ACI 13.5.3.2)

$$\gamma_v = 1 - \gamma_f$$
 (ACI 13.5.3.1)

For flat plates, γ_v is determined from the following equations taken from ACI 421.2R-07 *Seismic Design of Punching Shear Reinforcement in Flat Plates* [ACI 2007].

For interior columns,

$$\gamma_{vx} = 1 - \frac{1}{1 + (2/3)\sqrt{l_y/l_x}}$$
(ACI 421.2 C-11)

$$\gamma_{vy} = 1 - \frac{1}{1 + (2/3)\sqrt{l_x/l_y}}$$
(ACI 421.2 C-12)

For edge columns,

 γ_{vx} = same as for interior columns (ACI 421.2 C-13)

$$\gamma_{vy} = 1 - \frac{1}{1 + (2/3)\sqrt{l_x/l_y - 0.2}}$$
 (ACI 421.2 C-14)

$$\gamma_{vy} = 0$$
 when $l_x / l_y \le 0.2$

For corner columns,

$\gamma_{vx} = 0.4$	(ACI 421.2 C-15)
γ_{vy} = same as for edge columns	(ACI 421.2 C-16)

NOTE: Program uses ACI 421.4-12 and ACI 421.4-15 equations in lieu of ACI 421.2 C-14 and ACI 421.2 C-16 which are currently NOT enforced.

where b_1 is the width of the critical section measured in the direction of the span and b_2 is the width of the critical section measured in the direction perpendicular to the span. The values l_x and l_y are the projections of the shear-critical section onto its principal axes, x and y, respectively.

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4.5.3.3 Determine Concrete Capacity

The concrete punching shear stress capacity is taken as the minimum of the following three limits:

$$v_{c} = \min \begin{cases} \phi \left(2 + \frac{4}{\beta_{c}}\right) \lambda \sqrt{f_{c}'} \\ \phi \left(2 + \frac{\alpha_{s}d}{b_{o}}\right) \lambda \sqrt{f_{c}'} \\ \phi 4 \lambda \sqrt{f_{c}'} \end{cases}$$
(ACI 11.11.2.1)

where, β_c is the ratio of the maximum to the minimum dimensions of the critical section, b_o is the perimeter of the critical section, and α_s is a scale factor based on the location of the critical section.

$$\alpha_s = \begin{cases} 40 & \text{for interior columns,} \\ 30 & \text{for edge columns, and} \\ 20 & \text{for corner columns.} \end{cases}$$
(ACI 11.11.2.1)

A limit is imposed on the value of $\sqrt{f'_c}$ as:

$$\sqrt{f'_c} \le 100$$
 (ACI 11.1.2)

4.5.3.4 Computation of Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v_{U} = \frac{V_{U}}{bod} + \frac{\gamma v_{2}[M_{U2} - V_{U}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{U3} - V_{U}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 2

$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "sides" refers to the sides of the critical section
for punching shear Eq. 4

The equations for \overline{I}_{22} , \overline{I}_{33} , and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 4-axis or parallel to the 3-axis. Refer to Figure 4-4.

$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for the side of the critical section parallel
to the 4-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2, \text{ for the side of the critical section} \\ \text{parallel to the 3-axis} \qquad \text{Eq. 5b}$$

$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - x_3)^2$$
, for the side of the critical section
parallel to the 4-axis Eq. 6a

$$\overline{I}_{33} = Ld(x_2 - x_3)^2$$
, for the side of the critical section parallel
to the 3-axis Eq. 6b

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$$\overline{I}_{23} = Ld(x_2 - x_3)(y_2 - y_3)$$
, for side of critical section parallel
to 4-axis or 3-axis Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

where,

- b_0 = Perimeter of the critical section for punching shear
- d = Effective depth at the critical section for punching shear based on the average of d for 2 direction and d for 3 direction
- I_{22} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 4-axis

- I_{33} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of the inertia of the critical section for punching shear with respect to the 2 and 3 planes
- L = Length of the side of the critical section for punching shear currently being considered
- M_{U2} = Moment about the line parallel to the 4-axis at the center of the column (positive in accordance with the right-hand rule)
- M_{U3} = Moment about the line parallel to the 3-axis at the center of the column (positive in accordance with the right-hand rule)
- v_U = Punching shear stress
- V_U = Shear at the center of the column (positive upward)
- $x_1, y_1 =$ Coordinates of the column centroid
- x_2, y_2 = Coordinates of the center of one side of the critical section for punching shear
- x_3, y_3 = Coordinates of the centroid of the critical section for punching shear
- x_4, y_4 = Coordinates of the location where stress is being calculated
- γ_{V2} = Percent of M_{U2} resisted by shear
- γ_{V3} = Percent of M_{U3} resisted by shear

4.5.3.5 Determine Capacity Ratio

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section. The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

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4.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 6 inches, and not less than 16 times the shear reinforcement bar diameter (ACI 11.11.3). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is described in the subsections that follow.

4.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is limited to:

$$v_c \le \phi 2\lambda \sqrt{f'_c}$$
 for shear links (ACI 11.11.3.1)

$$v_c \le \phi 3\lambda \sqrt{f'_c}$$
 for shear studs (ACI 11.11.5.1)

4.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\text{max}} = 6\sqrt{f'_c} b_o d$$
 for shear links (ACI 11.11.3.2)

$$V_{\text{max}} = 8\sqrt{f'_c} b_o d$$
 for shear studs (ACI 11.11.5.1)

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows, where, ϕ , the strength reduction factor, is 0.75 (ACI 9.3.2.3).

$$\frac{A_{v}}{s} = \frac{\left(V_{u} - \phi V_{c}\right)}{\phi f_{vs} d}$$
(ACI 11.4.7.1, 11.4.7.2)

$$\frac{A_{v}}{s} \ge \frac{2\sqrt{f_{c}'}b_{o}}{f_{y}} \quad \text{for shear studs}$$
(ACI 11.11.5.1)

- If $V_u > \phi V_{\text{max}}$, a failure condition is declared. (ACI 11.11.3.2)
- If V_u exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size.

4.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 4-6 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 4-6 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2(ACI R11.3.3, 11.11.5.2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2*d* measured in a direction parallel to the column face (ACI 11.11.3.3).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of

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shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

4.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in ACI 7.7 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 3/8-, 1/4-, 5/8-, and 3/4-inch diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d*, and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

 $s_o \le 0.5d$ (ACI 11.11.5.2)

$$s \leq \begin{cases} 0.75d \quad \text{for} \qquad v_u \leq 6\phi\lambda\sqrt{f'_c} \\ 0.50d \quad \text{for} \qquad v_u > 6\phi\lambda\sqrt{f'_c} \end{cases}$$
(ACI 11.11.5.2)

$$g \le 2d$$
 (ACI 11.11.5.3)

The limits of s_o and the spacing, s, between for the links are specified as:

$s_o \leq 0.5d$	(ACI 11.11.3)
$s \le 0.50d$	(ACI 11.11.3)

Chapter 05 Design for AS 3600-09

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Australian code AS 3600-2009 [AS 2009] is selected. Various notations used in this chapter are listed in Table 5-1. For referencing to the pertinent sections of the AS code in this chapter, a prefix "AS" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

5.1 Notations

Table 5-1 List of Symbols Used in the AS 3600-2009 Code

- A_g Gross area of concrete, mm² A_l Area of longitudinal reinforcement for torsion, mm²
- A_{sc} Area of compression reinforcement, mm²

	List of Symbols Used in the AS 5000-2009 Code
A_{st}	Area of tension reinforcement, mm ²
Ast(re-	Area of required tension reinforcement, mm ²
quired)	
A_{sv}	Area of shear reinforcement, mm ²
$A_{sv,\min}$	Minimum area of shear reinforcement, mm ²
A_{sv}/s	Area of shear reinforcement per unit length, mm ² /mm
A_{sw}/s	Area of shear reinforcement per unit length consisting of closed ties, mm^2/mm
A_t	Area of a polygon with vertices at the center of longitudinal bars at the corners of a section, mm^2
a	Depth of compression block, mm
a_b	Depth of compression block at balanced condition, mm
a_{\max}	Maximum allowed depth of compression block, mm
b	Width of member, mm
b_{ef}	Effective width of flange (flanged section), mm
b_w	Width of web (flanged section), mm
С	Depth to neutral axis, mm
d	Distance from compression face to tension reinforcement, mm
d'	Concrete cover to compression reinforcement, mm
d_o	Distance from the extreme compression fiber to the centroid of the outermost tension reinforcement, mm
$d_{o\mathrm{m}}$	Mean value of d_o , averaged around the critical shear perimeter, mm
D	Overall depth of a section, mm
D_s	Thickness of slab (flanged section), mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement, MPa
f'_c	Specified compressive strength of concrete, MPa
f'_{cf}	Characteristic flexural tensile strength of concrete, MPa

Table 5-1 List of Symbols Used in the AS 3600-2009 Code

5 - 2 Notations

Table 5-1 List of Symbols Used in the AS 3600-2009 Code		
f_{cv}	Concrete shear strength, MPa	
f_{sy}	Specified yield strength of flexural reinforcement, MPa	
$f_{sy,f}$	Specified yield strength of shear reinforcement, MPa	
f'_s	Stress in the compression reinforcement, MPa	
J_t	Torsional modulus, mm ³	
k_u	Ratio of the depth to the neutral axis from the compression face, to the effective depth, d	
M_{ud}	Reduced ultimate strength in bending without axial force, N-mm	
M^*	Factored moment at section, N-mm	
N^*	Factored axial load at section, N	
S	Spacing of shear reinforcement along the strip, mm	
T _{uc}	Torsional strength of section without torsional reinforcement, N-mm	
$T_{u.\max}$	Maximum permitted total factored torsion at a section, N-mm	
Tus	Torsion strength of section with torsion reinforcement, N-mm	
T^*	Factored torsional moment at a section, N-mm	
u_t	Perimeter of the polygon defined by A_t , mm	
V^*	Factored shear force at a section, N	
$V_{u.max}$	Maximum permitted total factored shear force at a section, N	
$V_{u.\min}$	Shear strength provided by minimum shear reinforcement, N	
V_{uc}	Shear force resisted by concrete, N	
V_{us}	Shear force resisted by reinforcement, N	
γ1	Factor for obtaining depth of compression block in concrete	
eta_h	Ratio of the maximum to the minimum dimensions of the punch- ing critical section	
\mathcal{E}_{c}	Strain in concrete	
$\mathcal{E}_{c, \max}$	Maximum usable compression strain allowed in extreme concrete fiber, (0.003 mm/mm)	

Notations 5 - 3

Table 5-1 List of Symbols Used in the AS 3600-2009 Code

- ε_s Strain in reinforcement
- ϕ Strength reduction factor
- θ_t Angle of compression strut for torsion, degrees
- θ_{ν} Angle of compression strut for shear, degrees

5.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For AS 3600-09, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be defined (AS 2.4.2):

(AS/NZS 1170.0-02, 4.2.2(a))
(AS/NZS 1170.0-02, 4.2.2(b))
(AS/NZS 1170.0-02, 4.2.2(b))
(AS/NZS 1170.0-02, 4.2.2(g))
(AS/NZS 1170.0-02, 4.2.2(e))
(AS/NZS 1170.0-02, 4.2.2(d))
(AS/NZS 1170.0-02, 4.2.2(d))
(AS/NZS 1170.0-02, 4.2.2(f))
$(A \cap A) = (A \cap A) = (A \cap A) = (A \cap A) = (A \cap A)$

Note that the 0.4 factor on the live load in three of the combinations is not valid for live load representing storage areas. These are also the default design load combinations in ETABS whenever the AS 3600-2009 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

5 - 4 Design Load Combinations

5.3 Limits on Material Strength

The upper and lower limits of f'_c are 100 MPa and 20 MPa, respectively, for all framing types (AS 3.1.1.1(b)).

$f'_c \leq 1$	00 MPa ((AS 3.1	l.1.1)
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$$f'_{c} \ge 20 \,\mathrm{MPa}$$
 (AS 3.1.1.1)

The upper limit of f_{sy} is 500 MPa for all frames (AS 3.2.1, Table 3.2.1).

The code allows use of f'_c and f_{sy} beyond the given limits, provided special care is taken regarding the detailing and ductility (AS 3.1.1, 3.2.1, 17.2.1.1).

ETABS enforces the upper material strength limits for flexure and shear design o slabs. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. The user is responsible for ensuring that the minimum strength is satisfied.

5.4 Strength Reduction Factors

For

The strength reduction factor, ϕ , is defined as given in AS 2.2.2(ii), Table 2.2.2:

For members with Class N reinforcement only

$\phi = 0.80$ for flexure (tension controlled)	(Table 2.2.2(b))
$\phi = 0.60$ for flexure (compression controlled)	(Table 2.2.2(b))
members with Class L reinforcement	
$\phi = 0.64$ for flexure (tension controlled)	(Table 2.2.2(b))
$\phi = 0.60$ for flexure (compression controlled)	(Table 2.2.2(b))

 $\phi = 0.70$ for shear and torsion (Table 2.2.2(b))

These values can be overwritten; however, caution is advised.

Limits on Material Strength 5 - 5

5.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

5.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

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5.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

5.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete. Note that the flexural reinforcement strength, f_y , is limited to 500MPa (AS 3.2.1), even if the material property is defined using a higher value.

The design procedure is based on the simplified rectangular stress block, as shown in Figure 5-1 (AS 8.1.2).

The following assumptions apply to the stress block used to compute the flexural bending capacity of rectangular sections (AS 8.1.2).

- The maximum strain in the extreme compression fiber is taken as 0.003 (AS 8.1.3(a)).
- A uniform compressive stress of α₂ f'_c acts on an area (AS 8.1.3(b)) bounded by:
 - The edges of the cross-sections.
 - A line parallel to the neutral axis at the strength limit under the loading concerned, and located at a distance $\gamma k_u d$ from the extreme compression fiber.

The maximum allowable depth of the rectangular compression block, a_{max} , is given by

$$a_{\text{max}} = \gamma k_u d$$
 where, (AS 8.1.3(b))

$$\alpha_2 = 1.0 - 0.003 f'_c$$
 where, $0.67 \le \alpha_2 \le 0.85$ (AS 8.1.3(1))

$$\gamma = 1.05 - 0.007 f'_c$$
 where, $0.67 \le \gamma \le 0.85$ (AS 8.1.3(2))

$$k_u = 0.36$$
 (AS 8.1.5)

The design procedure used by ETABS for both rectangular and flanged sections (L- and T-shaped sections) is summarized in the following subsections. It is assumed that the design ultimate axial force does not exceed ($A_{sc}f_{sy} > 0.15N^*$) (AS 10.7.1a); hence, all slabs are designed for major direction flexure, shear, and torsion only.

5.5.1.3 Design of uniform thickness slab

In designing for a factored negative or positive moment, M^* (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 5-1), where,

$$a = d - \sqrt{d^2 - \frac{2|M^*|}{\alpha_2 f'_c \,\varphi b}}$$
(AS 8.1.3)

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Figure 5-1 Uniform Thickness Slab Design

where, the value of ϕ is taken as that for a tension controlled section ($k_u \le 0.36$), which by default is 0.80 (AS 2.2.2) in the preceding and following equations. The selection of Reinforcement Class can be made using the Design Preferences.

• If $a \le a_{\text{max}}$, the area of tension reinforcement is then given by:

$$A_{st} = \frac{M^*}{\varphi f_{sy} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M^* is positive, or at the top if M^* is negative.

• If $a > a_{\text{max}}$, i.e., $k_u > 0.36$, compression reinforcement is required (AS 8.1.5) and is calculated as follows:

The compressive force developed in the concrete alone is given by:

$$C = \alpha_2 f'_c b a_{\text{max}}$$
(AS 8.1.3)

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{uc} = C \left(d - \frac{a_{\max}}{2} \right) \phi$$

Therefore, the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{us} = M^* - M_{uc}$$

The required compression reinforcement is given by:

$$A_{sc} = \frac{M_{us}}{\left(f'_s - \alpha_2 f'_c\right)\left(d - d'\right)\phi}, \text{ where}$$
$$f'_s = 0.003E_s \left[\frac{c - d'}{c}\right] \le f_{sy} \tag{AS 8.1.2.1, 3.2.2}$$

The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{uc}}{f_{sy} \left[d - \frac{a_{\max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{us}}{f_{sy} \left(d - d' \right) \phi}$$

Therefore, the total tension reinforcement is $A_{st} = A_{s1} + A_{s2}$, and the total compression reinforcement is A_{sc} . A_{st} is to be placed at the bottom and A_{sc} is to be placed at the top if M^* is positive, and vice versa if M^* is negative.

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5.5.1.4 Design of nonuniform thickness slab

In designing a nonuniform thickness slab, a simplified stress block, as shown in Figure 5-2, is assumed if the flange is under compression, i.e., if the moment is positive. If the moment is negative, the flange comes under tension, and the flange is ignored. In that case, a simplified stress block similar to that shown in Figure 5-1 is assumed on the compression side (AS 8.1.5).



Figure 5-2 T- Nonuniform Thickness Slab Design

5.5.1.5 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M^* (i.e., designing top reinforcement), the calculation of the reinforcement is exactly the same as above, i.e., no flanged data is used.

5.5.1.6 Flanged Slab Section Under Positive Moment

If $M^* > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M^*}{\alpha_2 f'_c \varphi b_f}}$$

where, the value of ϕ is taken as that for $k_u \le 0.36$, which is 0.80 by default (AS 2.2.2) in the preceding and the following equations.

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \gamma k_u d$$
 where, $k_u = 0.36$ (AS 8.1.5)

- If $a \le D_s$, the subsequent calculations for A_{st} are exactly the same as previously defined for the uniform thickness slab design. However, in that case, the width of the slkab is taken as b_f . Compression reinforcement is required when $a > a_{\text{max}}$.
- If $a > D_s$, the calculation for A_{st} has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 5-2. C_f is given by:

$$C_f = \alpha_2 f'_c \left(b_{ef} - b_w \right) \times \min\left(D_s, a_{\max} \right)$$
(AS 8.1.3(b))

Therefore, $A_{s1} = \frac{C_f}{f_{sy}}$ and the portion of M^* that is resisted by the flange is

given by:

$$M_{uf} = \varphi C_f \left(d - \frac{\min(D_s, a_{\max})}{2} \right)$$

Therefore, the balance of the moment M^* to be carried by the web is:

$$M_{uw} = M^* - M_{uf}$$

The web is a rectangular section of dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{uw}}{\alpha_2 f'_c \phi b_w}}$$

• If $a_1 \le a_{\text{max}}$, the area of tension reinforcement is then given by:

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$$A_{s2} = \frac{M_{uw}}{\phi f_{sy} \left(d - \frac{a_1}{2} \right)}, \text{ and}$$
$$A_{st} = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged slab.

• If $a_1 > a_{\text{max}}$, compression reinforcement is required and is calculated as follows:

The compression force in the web concrete alone is given by:

$$C_{\rm w} = \alpha_2 f'_c b_{\rm w} a_{\rm max} \tag{AS 8.1.3}$$

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{uc} = C_w \left(d - \frac{a_{\max}}{2} \right) \phi$$

and the moment resisted by compression and tension reinforcement is:

$$M_{us} = M_{uw} - M_{uc}$$

Therefore, the compression reinforcement is computed as:

$$A_{sc} = \frac{M_{us}}{\left(f'_{s} - \alpha_{2}f'_{c}\right)\left(d - d'\right)\phi}, \text{ where}$$

$$f'_{s} = 0.003E_{s} \left[\frac{c_{\max} - d'}{c_{\max}}\right] \le f_{sy} \text{ (AS}$$

$$8.1.2.1,$$

$$3.2.2)$$

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{uc}}{f_{sy} \left[d - \frac{a_{max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{us}}{f_{sy} \left(d - d' \right) \phi}$$

The total tensile reinforcement is $A_{st} = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A_{sc} . A_{st} is to be placed at the bottom and A_{sc} is to be placed at the top.

5.5.1.7 Minimum and Maximum Reinforcement

The minimum flexural tensile reinforcement required for each direction of a slab is given by the following limits (AS 9.1.1):

$$A_{s} = 0.24 \left(\frac{h}{d}\right)^{2} \frac{f_{ct,f}^{'}}{f_{sy,f}} bh \text{ for flat slabs}$$
(AS 9.1.1(a))
$$A_{s} = 0.19 \left(\frac{h}{d}\right)^{2} \frac{f_{ct,f}^{'}}{f_{sy,f}} bh$$

for slabs supported by beams/walls and slab footings. (AS 9.1.1(b))

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

5.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V^* .
- Determine the shear force, V_{uc} , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

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The following three sections describe in detail the algorithms associated with these steps.

5.5.2.1 Determine Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

5.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_{uc} , is calculated as:

$$V_{uc} = \beta_1 \beta_2 \beta_3 b_w d_o f'_{cv} \left[\frac{A_{st}}{b_w d_o} \right]^{1/3}$$
(AS 8.2.7.1)

where,

$$f'_{cv} = (f'_{c})^{1/3} \le 4$$
MPa (AS 8.2.7.1)

$$\beta_1 = 1.1 \left(1.6 - \frac{d_o}{1000} \right) \ge 1.1$$
 (AS 8.2.7.1)

$$\beta_2 = 1, \text{ or }$$
 (AS 8.2.7.1)

 $= 1 - \left(\frac{N^*}{3.5A_g}\right) \ge 0$ for members subject to significant axial tension, or

$$= 1 + \left(\frac{N^*}{14A_g}\right)$$
 for members subject to significant axial compression.

 $\beta_3 = 1$

5.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to:

$$V_{u.\min} = V_{uc} + 0.6b_v d_o \tag{AS 8.2.9}$$

$$V_{u.\text{max}} = 0.2 f'_c b d_o$$
 (AS 8.2.6)

Given V^* , V_{uc} , and $V_{u.max}$, the required shear reinforcement is calculated as follows, where, ϕ , the strength reduction factor, is 0.75 by default (AS 2.2.2).

• If $V^* \le \phi V_{uc} / 2$,

 $\frac{A_{sv}}{s} = 0$, if $D \le 750$ mm; otherwise $A_{sv.min}$ shall be provided. (AS 8.2.5).

• If $(\phi V_{uc}/2) < V^* \leq \phi V_{u.\min}$,

 $\frac{A_{sv}}{s} = 0, \text{ if } D < b_w/2 \text{ or } 250 \text{ mm, whichever is greater (AS 8.2.5(c)(i));}$ otherwise $A_{sv,\min}$ shall be provided.

• If $\phi V_{u.\min} < V^* \le \phi V_{u.\max}$, $\frac{A_{sv}}{s} = \frac{\left(V^* - \phi V_{uc}\right)}{\phi f_{sy.f} d_o \cot \theta_v},$ (AS 8.2.10)

and greater than $A_{sv.min}$, defined as:

$$\frac{A_{sv.\min}}{s} = \left(0.35 \frac{b_w}{f_{sy.f}}\right) \tag{AS 8.2.8}$$

 θ_v = the angle between the axis of the concrete compression strut and the longitudinal axis of the member, which varies linearly from 30 degrees when $V^* = \phi V_{u,\min}$ to 45 degrees when $V^* = \phi V_{u,\max}$.

• If
$$V^* > \phi V_{\text{max}}$$
, a failure condition is declared. (AS 8.2.6)

• If V^* exceeds its maximum permitted value ϕV_{max} , the concrete section size should be increased (AS 8.2.6).

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Note that if torsion design is considered and torsion reinforcement is required, the calculated shear reinforcement is ignored. Closed stirrups are designed for combined shear and torsion according to AS 8.3.4(b).

The maximum of all of the calculated A_{sv}/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

5.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

5.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of $d_{om}/2$ from the face of the support (AS 9.2.1.1). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (AS 9.2.1.3). Figure 5-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.


Figure 5-3 Punching Shear Perimeters

5.5.3.2 Determine Concrete Capacity

The shear capacity, f_{cv} , is calculated based on the minimum of the two expressions from AS 9.2.3, as shown, with the d_{om} and u terms removed to convert force to stress.

$$f_{cv} = \min \begin{cases} 0.17 \left(1 + \frac{2}{\beta_h} \right) \sqrt{f'_c} \\ 0.34 \sqrt{f'_c} \end{cases}$$
(AS 9.2.3(a))

where, β_h is the ratio of the longest dimension to the shortest dimension of the critical section.

5.5.3.3 Determine Maximum Shear Stress

The maximum design shear stress is computed along the major and minor axis of column separately using the following equation:

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$$v_{\max} = \frac{V^*}{ud_{om}} \left[1.0 + \frac{uM_v}{8V^* ad_{om}} \right]$$
(AS 9.2.4(a))

5.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

5.5.4 Design Punching Shear Reinforcement

The design guidelines for shear links or shear studs are not available in AS 3600-2009. ETABS uses the NZS 3101-06 guidelines to design shear studs or shear links.

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 150 mm, and not less than 16 times the shear reinforcement bar diameter (NZS 12.7.4.1). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is carried out as described in the subsections that follow.

5.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

5.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\text{max}} = 3 V_{u,\min} = 3 V_u$$
 (AS 9.2.4(a), (d))

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where V_u is computed from AS 9.2.3 or 9.2.4. Given V^* , V_u , and $V_{u,\text{max}}$, the required shear reinforcement is calculated as follows, where, ϕ is the strength reduction factor.

$$\frac{A_{sv}}{s} = \frac{\left(V^* - \phi V_u\right)}{f_{sv} d_{om}},$$
 (AS 8.2.10)

Minimum punching shear reinforcement should be provided such that:

$$V_s \ge \frac{1}{16} \sqrt{f'_c} u d_{om}$$
 (NZS 12.7.4.3)

- If $V^* > \phi V_{\text{max}}$, a failure condition is declared. (NZS 12.7.3.4)
- If V^* exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size.

5.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 5-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2d measured in a direction parallel to the column face (NZS 12.7.4.4).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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Figure 5-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

5.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in NZS 3.11 plus one-half of the diameter of the flexural reinforcement.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d* and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$s_o \leq 0.5d$	(NZS 12.7.4.4)
$s \leq 0.5d$	(NZS 12.7.4.4)
$g \leq 2d$	(NZS 12.7.4.4)

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Chapter 6 Design for AS 3600-01

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Australian code AS 3600-2001 [AS 2001] is selected. Various notations used in this chapter are listed in Table 6-1. For referencing to the pertinent sections of the AS code in this chapter, a prefix "AS" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

6.1 Notations

Table 6-1 List of Symbols Used in the AS 3600-2001 Code

- A_g Gross area of concrete, mm²
- A_l Area of longitudinal reinforcement for torsion, mm²
- A_s Area of tension reinforcement, mm²

	List of Symbols Used in the AS 3000-2001 Code
A_{sc}	Area of compression reinforcement, mm ²
A_{st}	Area of tension reinforcement, mm ²
$A_{s(required)}$	Area of required tension reinforcement, mm ²
A_{sv}	Area of shear reinforcement, mm ²
$A_{sv,\min}$	Minimum area of shear reinforcement, mm ²
A_{sv}/s	Area of shear reinforcement per unit length, mm ² /mm
A_{sw}/s	Area of shear reinforcement per unit length consisting of closed ties, mm^2/mm
A_t	Area of a polygon with vertices at the center of longitudinal bars at the corners of a section, mm^2
a	Depth of compression block, mm
a_b	Depth of compression block at balanced condition, mm
a_{\max}	Maximum allowed depth of compression block, mm
b	Width of member, mm
b_{ef}	Effective width of flange (flanged section), mm
b_w	Width of web (flanged section), mm
С	Depth to neutral axis, mm
d	Distance from compression face to tension reinforcement, mm
d'	Concrete cover to compression reinforcement, mm
d_o	Distance from the extreme compression fiber to the centroid of the outermost tension reinforcement, mm
$d_{o\mathrm{m}}$	Mean value of d_o , averaged around the critical shear perimeter, mm
D	Overall depth of a section, mm
D_s	Thickness of slab (flanged section), mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement, MPa
f'_c	Specified compressive strength of concrete, MPa
f'_{cf}	Characteristic flexural tensile strength of concrete, MPa

Table 6-1 List of Symbols Used in the AS 3600-2001 Code

6 - 2 Notations

Table 6-1 List of Symbols Used in the AS 3600-2001 Code		
f_{cv}	Concrete shear strength, MPa	
f_{sy}	Specified yield strength of flexural reinforcement, MPa	
$f_{sy,f}$	Specified yield strength of shear reinforcement, MPa	
f'_s	Stress in the compression reinforcement, MPa	
J_t	Torsional modulus, mm ³	
k_u	Ratio of the depth to the neutral axis from the compression face, to the effective depth, d	
M_{ud}	Reduced ultimate strength in bending without axial force, N-mm	
M^*	Factored moment at section, N-mm	
N^*	Factored axial load at section, N	
S	Spacing of shear reinforcement along the strip, mm	
T_{uc}	Torsional strength of section without torsional reinforcement, N-mm	
$T_{u.\max}$	Maximum permitted total factored torsion at a section, N-mm	
T_{us}	Torsion strength of section with torsion reinforcement, N-mm	
T^*	Factored torsional moment at a section, N-mm	
\mathcal{U}_t	Perimeter of the polygon defined by A_t , mm	
V^*	Factored shear force at a section, N	
$V_{u.max}$	Maximum permitted total factored shear force at a section, N	
$V_{u.\min}$	Shear strength provided by minimum shear reinforcement, N	
V_{uc}	Shear force resisted by concrete, N	
V_{us}	Shear force resisted by reinforcement, N	
γ1	Factor for obtaining depth of compression block in concrete	
eta_h	Ratio of the maximum to the minimum dimensions of the punch- ing critical section	
\mathcal{E}_{c}	Strain in concrete	
$\mathcal{E}_{c, \max}$	Maximum usable compression strain allowed in extreme concrete fiber, (0.003 mm/mm)	

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Table 6-1 List of Symbols Used in the AS 3600-2001 Code

- ε_s Strain in reinforcement
- ϕ Strength reduction factor
- θ_t Angle of compression strut for torsion, degrees
- θ_v Angle of compression strut for shear, degrees

6.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For AS 3600-01, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be defined (AS 3.3.1):

ı))
)))
)))
g))
e))
1))
ł))
f))

Note that the 0.4 factor on the live load in three of the combinations is not valid for live load representing storage areas. These are also the default design load combinations in ETABS whenever the AS 3600-2001 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

6 - 4 Design Load Combinations

6.3 Limits on Material Strength

The upper and lower limits of f'_c are 65 MPa and 20 MPa, respectively, for all framing types (AS 6.1.1.1(b)).

f'	$_c \leq 65 \mathrm{MPa}$	(AS 6.1.1.1)
----	---------------------------	--------------

$$f'_{c} \ge 20 \,\mathrm{MPa}$$
 (AS 6.1.1.1)

The upper limit of f_{sy} is 500 MPa for all frames (AS 6.2.1, Table 6.2.1).

The code allows use of f'_c and f_{sy} beyond the given limits, provided special care is taken regarding the detailing and ductility (AS 6.1.1, 6.2.1, 19.2.1.1).

ETABS enforces the upper material strength limits for flexure and shear design of slabs. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. The user is responsible for ensuring that the minimum strength is satisfied.

6.4 Strength Reduction Factors

The strength reduction factor, ϕ , is defined as given in AS 2.3(c), Table 2.3:

$\phi = 0.80$ for flexure (tension controlled)	(AS 2.3(c))
$\phi = 0.70$ for shear and torsion	(AS 2.3(c))

These values can be overwritten; however, caution is advised.

6.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method. The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

6.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

6.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab

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may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

6.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete. Note that the flexural reinforcement strength, f_y , is limited to 500MPa (AS 6.2.1), even if the material property is defined using a higher value.

The design procedure is based on the simplified rectangular stress block, as shown in Figure 6-1 (AS 8.1.2.2).

The following assumptions are used for the stress block used to compute the flexural bending capacity of rectangular sections (AS 8.1.2.2).

- The maximum strain in the extreme compression fiber is taken as 0.003.
- A uniform compressive stress of 0.85*f*'_c acts on an area bounded by:
 - The edges of the cross-sections.
 - A line parallel to the neutral axis at the strength limit under the loading concerned, and located at a distance $\gamma k_u d$ from the extreme compression fiber.

The maximum allowable depth of the rectangular compression block, a_{max} , is given by

$$a_{\max} = \gamma k_u d \text{ where,}$$
(AS 8.1.3)
$$\gamma = [0.85 - 0.007(f'_c - 28)]$$
$$0.65 \le \gamma \le 0.85$$
(AS 8.1.2.2)
$$k_u = 0.4$$

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The design procedure used by ETABS for both rectangular and flanged sections (L- and T-shaped sections) is summarized in the following subsections. It is assumed that the design ultimate axial force does not exceed ($A_{sc}f_{sy}$ >0.15 N^*) (AS 10.7.1a); hence, all slabs are designed for major direction flexure, shear, and torsion only.

6.5.1.3 Design of uniform thickness slab

In designing for a factored negative or positive moment, M^* (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 6-1), where,



Figure 6-1 Uniform Thickness Slab Design

where, the value of ϕ is taken as that for a tension controlled section ($k_u \le 0.4$), which by default is 0.80 (AS 2.3) in the preceding and following equations.

• If $a \le a_{\text{max}}$, the area of tension reinforcement is then given by:

$$A_{st} = \frac{M^*}{\phi f_{sy} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M^* is positive, or at the top if M^* is negative.

• If *a* > *a*_{max}, i.e., *k_u* > 0.4, compression reinforcement is required (AS 8.1.3) and is calculated as follows:

The compressive force developed in the concrete alone is given by:

$$C = 0.85 f'_c ba_{\text{max}}$$
 (AS 8.1.2.2)

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{uc} = C \left(d - \frac{a_{\max}}{2} \right) \phi$$

Therefore, the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{us} = M^* - M_{uc}$$

The required compression reinforcement is given by:

$$A_{sc} = \frac{M_{us}}{(f'_s - 0.85f'_c)(d - d')\phi}, \text{ where}$$

$$f'_s = 0.003E_s \left[\frac{c - d'}{c}\right] \le f_{sy}$$
(AS 8.1.2.1, 6.2.2)

The required tension reinforcement for balancing the compression in the concrete is:

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$$A_{s1} = \frac{M_{uc}}{f_{sy} \left[d - \frac{a_{\max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{us}}{f_{sy} \left(d - d' \right) \phi}$$

Therefore, the total tension reinforcement is $A_{st} = A_{s1} + A_{s2}$, and the total compression reinforcement is A_{sc} . A_{st} is to be placed at the bottom and A_{sc} is to be placed at the top if M^* is positive, and vice versa if M^* is negative.

6.5.1.4 Design of nonuniform thickness slab

In designing a flanged shaped section, a simplified stress block, as shown in Figure 6-2, is assumed if the flange is under compression, i.e., if the moment is positive. If the moment is negative, the flange comes under tension, and the flange is ignored. In that case, a simplified stress block similar to that shown in Figure 6-1 is assumed on the compression side (AS 8.1.3).



Figure 6-2 T- Nonuniform Thickness Slab Design

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6.5.1.4.1.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M^* (i.e., designing top reinforcement), the calculation of the reinforcement is exactly the same as above, i.e., no flanged data is used.

6.5.1.4.1.2 Flanged Slab Section Under Positive Moment

If $M^* > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M^*}{0.85f'_c \phi b_f}}$$

where, the value of ϕ is taken as that for $k_u \le 0.4$, which is 0.80 by default (AS 2.3) in the preceding and the following equations.

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = \gamma k_u d$$
 where, $k_u = 0.4$ (AS 8.1.3)

- If $a \le D_s$, the subsequent calculations for A_{st} are exactly the same as previously defined for the uniform thickness slab design. However, in that case, the width of the slkab is taken as b_f . Compression reinforcement is required when $a > a_{\text{max}}$.
- If $a > D_s$, the calculation for A_{st} has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 6-2. C_f is given by:

$$C_f = 0.85 f'_c (b_{ef} - b_w) \times \min(D_s, a_{\max})$$
 (AS 8.1.2.2)

Therefore, $A_{s1} = \frac{C_f}{f_{sy}}$ and the portion of M^* that is resisted by the flange is given by:

$$M_{uf} = \phi C_f \left(d - \frac{\min(D_s, a_{\max})}{2} \right)$$

Therefore, the balance of the moment, M^* to be carried by the web is:

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$$M_{uw} = M^* - M_{uf}$$

The web is a rectangular section of dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{uw}}{0.85f'_c \phi b_w}}$$

• If $a_1 \le a_{\text{max}}$, the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_{uw}}{\phi f_{sy} \left(d - \frac{a_1}{2} \right)}, \text{ and}$$

$$A_{st} = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged slab.

• If $a_1 > a_{\text{max}}$, compression reinforcement is required and is calculated as follows:

The compression force in the web concrete alone is given by:

$$C_w = 0.85 f'_c b_w a_{\text{max}}$$
 (AS 8.1.2.2)

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{uc} = C_w \left(d - \frac{a_{\max}}{2} \right) \phi$$

and the moment resisted by compression and tension reinforcement is:

$$M_{us} = M_{uw} - M_{uc}$$

Therefore, the compression reinforcement is computed as:

$$A_{sc} = \frac{M_{us}}{\left(f'_s - 0.85f'_c\right)\left(d - d'\right)\phi}, \text{ where }$$

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$$f'_{s} = 0.003 E_{s} \left[\frac{c_{\max} - d'}{c_{\max}} \right] \le f_{sy} \text{ (AS}$$

6.2.2)

8.1.2.1

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{uc}}{f_{sy} \left[d - \frac{a_{max}}{2} \right] \phi}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{us}}{f_{sy} \left(d - d' \right) \phi}$$

The total tensile reinforcement is $A_{st} = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A_{sc} . A_{st} is to be placed at the bottom and A_{sc} is to be placed at the top.

6.5.1.5 Minimum and Maximum Reinforcement

The minimum flexural tensile reinforcement required for each direction of a slab is given by the following limits (AS 9.1.1):

 $A_s \ge 0.0025 \ bh$ for flat slabs (AS 9.1.1(a))

 $A_s \ge 0.0020 \ bh$ for slabs supported by beams/walls and slab footings

(AS 9.1.1(b))

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

6.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V^* .
- Determine the shear force, V_{uc} , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

6.5.2.1 Determine Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

6.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_{uc} , is calculated as:

$$V_{uc} = \beta_1 \beta_2 \beta_3 b_w d_o \left[\frac{A_{st} f'_c}{b_w d_o} \right]^{1/3}$$
(AS 8.2.7.1)

where,

$$\beta_1 = 1.1 \left(1.6 - \frac{d_o}{1000} \right) \ge 1.1$$
 (AS 8.2.7.1)

$$\beta_2 = 1, \text{ or}$$
 (AS 8.2.7.1)

 $= 1 - \left(\frac{N^*}{3.5A_g}\right) \ge 0$ for members subject to significant axial tension, or

$$= 1 + \left(\frac{N^*}{14A_g}\right)$$
 for members subject to significant axial compression.

$$\beta_3 = 1$$

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6.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to:

$$V_{u,\min} = V_{uc} + 0.6b_{v}d_{o} \tag{AS 8.2.9}$$

$$V_{u.\text{max}} = 0.2 f'_{c} b d_{o}$$
 (AS 8.2.6)

Given V^* , V_{uc} , and $V_{u.max}$, the required shear reinforcement is calculated as follows, where, ϕ , the strength reduction factor, is 0.6 by default (AS 2.3).

• If
$$V^* \le \phi V_{uc} / 2$$
,

$$\frac{A_{sv}}{s} = 0$$
, if $D \le 750$ mm; otherwise $A_{sv.min}$ shall be provided. (AS 8.2.5).

• If $(\phi V_{uc} / 2) < V^* \le \phi V_{u.\min}$,

 $\frac{A_{sv}}{s} = 0, \text{ if } D < b_w/2 \text{ or } 250 \text{ mm, whichever is greater (AS 8.2.5(c)(i));}$ otherwise $A_{sv,\min}$ shall be provided.

• If
$$\phi V_{u.\min} < V^* \leq \phi V_{u.\max}$$
,

$$\frac{A_{sv}}{s} = \frac{\left(V^* - \phi V_{uc}\right)}{\phi f_{sy.f} d_o \cot \theta_v},$$
(AS 8.2.10)

and greater than $A_{sv.min}$, defined as:

$$\frac{A_{\text{sv.min}}}{s} = \left(0.35 \frac{b_{w}}{f_{\text{sy.}f}}\right) \tag{AS 8.2.8}$$

 θ_v = the angle between the axis of the concrete compression strut and the longitudinal axis of the member, which varies linearly from 30 degrees when $V^* = \phi V_{u,min}$ to 45 degrees when $V^* = \phi V_{u,max}$.

• If
$$V^* > \phi V_{\text{max}}$$
, a failure condition is declared. (AS 8.2.6)

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• If V^* exceeds its maximum permitted value ϕV_{max} , the concrete section size should be increased (AS 8.2.6).

Note that if torsion design is considered and torsion reinforcement is required, the calculated shear reinforcement is ignored. Closed stirrups are designed for combined shear and torsion according to AS 8.3.4(b).

The maximum of all of the calculated A_{sv}/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

6.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

6.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of $d_{om}/2$ from the face of the support (AS 9.2.1.1). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (AS 9.2.1.3). Figure 6-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.

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Figure 6-3Punching Shear Perimeters

6.5.3.2 Determine Concrete Capacity

The shear capacity, f_{cv} , is calculated based on the minimum of the two expressions from AS 3600-01 equation 11-35, as shown, with the d_{om} and u terms removed to convert force to stress.

$$f_{cv} = \min \begin{cases} 0.17 \left(1 + \frac{2}{\beta_h} \right) \sqrt{f'_c} \\ 0.34 \sqrt{f'_c} \end{cases}$$
(AS 9.2.3(a))

where, β_h is the ratio of the longest dimension to the shortest dimension of the critical section.

6.5.3.3 Determine Maximum Shear Stress

The maximum design shear stress is computed along the major and minor axis of column separately using the following equation:

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$$v_{\max} = \frac{V^*}{ud_{om}} \left[1.0 + \frac{uM_v}{8V^* ad_{om}} \right]$$
(AS 9.2.4(a))

6.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

6.5.4 Design Punching Shear Reinforcement

The design guidelines for shear links or shear studs are not available in AS 3600-2001. ETABS uses the NZS 3101-06 guidelines to design shear studs or shear links.

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 150 mm, and not less than 16 times the shear reinforcement bar diameter (NZS 12.7.4.1). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is carried out as described in the subsections that follow.

6.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

6.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\text{max}} = 3 V_{u,\min} = 3*V_u$$
 (AS 92.2.4(a), (d))

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where V_u is computed from AS 9.2.3 or 9.2.4. Given V^* , V_u , and $V_{u,\text{max}}$, the required shear reinforcement is calculated as follows, where, ϕ is the strength reduction factor.

$$\frac{A_{sv}}{s} = \frac{\left(V^* - \phi V_u\right)}{f_{sy} d_{om}},$$
 (AS 8.2.10)

Minimum punching shear reinforcement should be provided such that:

$$V_s \ge \frac{1}{16} \sqrt{f'_c} u d_{om}$$
 (NZS 12.7.4.3)

• If $V^* > \phi V_{\text{max}}$, a failure condition is declared. (NZS 12.7.3.4)

• If V^* exceeds the maximum permitted value of ϕV_{max} , the concrete section should be increased in size.

6.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 6-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2d measured in a direction parallel to the column face (NZS 12.7.4.4).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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Figure 6-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

6.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in NZS 3.11 plus half of the diameter of the flexural reinforcement.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d* and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$s_o \leq 0.5d$	(NZS 12.7.4.4)
$s \leq 0.5d$	(NZS 12.7.4.4)
$g \leq 2d$	(NZS 12.7.4.4)

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Chapter 7 Design for BS 8110-97

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the British code BS 8110-1997 [BSI 1997] is selected. For light-weight concrete and torsion, reference is made to BS 8110-2:1985 [BSI 1985]. Various notations used in this chapter are listed in Table 7-1. For referencing to the pertinent sections of the British code BS 8110-1997 in this chapter, a prefix "BS" followed by the section number is used.

The design is based on user-specified loading combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

7.1 Notations

Table 7-1 List of Symbols Used in the BS 8110-1997 Code

 A_g Gross area of cross-section, mm²

Table 7-1	List of Symbols Used in the BS 8110-1997 Code
A_l	Area of longitudinal reinforcement for torsion, mm ²
A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²
A_{sv}	Total cross-sectional area of links at the neutral axis, mm ²
$A_{sv,t}$	Total cross-sectional area of closed links for torsion, mm ²
A_{sv} / s_v	Area of shear reinforcement per unit length, mm ² /mm
а	Depth of compression block, mm
b	Width or effective width of the section in the compression zone, mm
b_f	Width or effective width of flange, mm
b_w	Average web width of a flanged section, mm
С	Torsional constant, mm ⁴
d	Effective depth of tension reinforcement, mm
d'	Depth to center of compression reinforcement, mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 MPa
f	Punching shear factor considering column location
fcu	Characteristic cube strength at 28 days, MPa
f'_s	Stress in the compression reinforcement, MPa
f_y	Characteristic strength of reinforcement, MPa
f_{yv}	Characteristic strength of shear reinforcement, MPa
h	Overall depth of a section in the plane of bending, mm

7 - 2 Notations

	List of Symbols Used in the BS 8110-1997 Code
h_{f}	Flange thickness, mm
$h_{ m min}$	Smaller dimension of a rectangular section, mm
h_{\max}	Larger dimension of a rectangular section, mm
Κ	Normalized design moment, $\frac{M_u}{bd^2 f_{cu}}$
Κ'	Maximum $\frac{M_u}{bd^2 f_{cu}}$ for a singly reinforced concrete section, taken
	as 0.156 by assuming that moment redistribution is limited to 10%.
k_1	Shear strength enhancement factor for support compression
k_2	Concrete shear strength factor, $[f_{cu}/25]^{\frac{1}{3}}$
<i>k</i> ₃	Shear strength reduction factor for light-weight concrete
М	Design moment at a section, N-mm
$M_{\rm single}$	Limiting moment capacity as singly reinforced slab, N-mm
S_{ν}	Spacing of the links along the length of the strip, mm
Т	Design torsion at ultimate design load, N-mm
и	Perimeter of the punching critical section, mm
V	Design shear force at ultimate design load, N
V	Design shear stress at a slab cross-section or at a punching critical section, MPa
Vc	Design concrete shear stress capacity, MPa
$v_{\rm max}$	Maximum permitted design factored shear stress, MPa

Table 7.4 List of Symbols Lload in the DS 9110 1007 Code

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Vt	Torsional shear stress, MPa
x	Neutral axis depth, mm
$\chi_{\rm bal}$	Depth of neutral axis in a balanced section, mm
Z.	Lever arm, mm
β	Torsional stiffness constant
eta_b	Moment redistribution factor in a member
γf	Partial safety factor for load
γ_m	Partial safety factor for material strength
\mathcal{E}_{c}	Maximum concrete strain, 0.0035
\mathcal{E}_{s}	Strain in tension reinforcement
$\dot{\varepsilon_s}$	Strain in compression reinforcement

Table 7-1 List of Symbols Used in the BS 8110-1997 Code

7.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. The design load combinations are obtained by multiplying the characteristic loads by appropriate partial factors of safety, γ_f (BS 2.4.1.3). For BS 8110-1997, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), and wind (W) loads, and considering that wind forces are reversible, the following load combinations may need to be considered (BS 2.4.3).

1.4D 1.4D + 1.6L	(BS 2.4.3)
1.4D + 1.6(0.75PL)	(BS 2.4.3)
$1.0D \pm 1.4W$ $1.4D \pm 1.4W$ $1.2D + 1.2L \pm 1.2W$	(BS 2.4.3)

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1.4D + 1.6L + 1.6S	
$1.2D + 1.2S \pm 1.2W$	(BS 2 4 3)
$1.2D + 1.2L + 1.2S \pm 1.2W$	(DS 2.4.3)

These are also the default design load combinations in ETABS whenever the BS 8110-1997 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used. Note that the automatic combination, including pattern live load, is assumed and should be reviewed before using for design.

7.3 Limits on Material Strength

The concrete compressive strength, f_{cu} , should not be less than 25 MPa (BS 3.1.7.2). ETABS does not enforce this limit for flexure and shear design of slabs. The input material strengths are used for design even if they are outside of the limits. It is the user's responsibility to use the proper strength values while defining the materials.

7.4 Partial Safety Factors

The design strengths for concrete and reinforcement are obtained by dividing the characteristic strength of the material by a partial safety factor, γ_m . The values of γ_m used in the program are listed in the following table, as taken from BS Table 2.2 (BS 2.4.4.1):

Values of γ_m for the Ultimate Limit State	
Reinforcement	1.15
Concrete in flexure and axial load	1.50
Concrete shear strength without shear reinforcement	1.25

These factors are already incorporated into the design equations and tables in the code. Note that for reinforcement, the default factor of 1.15 is for Grade 500 reinforcement. If other grades are used, this value should be overwritten as necessary. Changes to the partial safety factors are carried through the design equations where necessary, typically affecting the material strength portions of the equations.

7.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

7.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

7.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

7.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding the compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 7-1 (BS 3.4.4.4). Furthermore, it is assumed that moment redistribution in the member does not exceed 10% (i.e., $\beta_b \ge 0.9$; BS 3.4.4.4). The code also places a limitation on the neutral axis depth, $x/d \le 0.5$, to safeguard against non-ductile failures (BS 3.4.4.4). In addition, the area of compression reinforcement is calculated assuming that the neutral axis depth remains at the maximum permitted value.

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped section) is summarized in the subsections that follow. It is assumed that the design ultimate axial force does not exceed $(0.1f_{cu} A_g)$ (BS 3.4.4.1); hence, all slabs are designed for major direction flexure, shear, and torsion only.

Design of uniform thickness slab

For uniform thickness slab, the limiting moment capacity as a singly reinforced slab, M_{single} , is first calculated for a section. The reinforcement is determined based on *M* being greater than, less than, or equal to M_{single} . See Figure 7-1.

• Calculate the ultimate limiting moment of resistance of the section as singly reinforced.

$$M_{\text{single}} = K' f_{cu} b d^2, \text{ where}$$
(BS 3.4.4.4)



Figure 7-1 Uniform Thickness Slab Design

• If $M \le M_{\text{single}}$, the area of tension reinforcement, A_s , is given by:

$$A_s = \frac{M}{0.87 f_y z}$$
, where (BS 3.4.4.4)

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$$z = d \left(0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right) \le 0.95d$$
 (BS 3.4.4.4)

$$K = \frac{M}{f_{cu}bd^2}$$
(BS 3.4.4.4)

This reinforcement is to be placed at the bottom if M is positive, or at the top if M is negative.

• If $M > M_{\text{single}}$, compression reinforcement is required and calculated as follows:

$$A'_{s} = \frac{M - M_{\text{single}}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{c}}\right)\left(d - d'\right)}$$
(BS 3.4.4.4)

where d' is the depth of the compression reinforcement from the concrete compression face, and

$$f'_{s} = 0.87 f_{y} \text{ if } \frac{d'}{d} \le \frac{1}{2} \left[1 - \frac{f_{y}}{800} \right]$$
 (BS 3.4.4.1, 2.5.3, Fig 2.2)

$$f'_{s} = E_{s}\varepsilon_{c}\left[1 - \frac{2d'}{d}\right]$$
 if $d'_{d} > \frac{1}{2}\left[1 - \frac{f_{y}}{800}\right]$ (BS 3.4.4.1, 2.5.3, Fig 2.2)

The tension reinforcement required for balancing the compression in the concrete and the compression reinforcement is calculated as:

$$A_{s} = \frac{M_{\text{single}}}{0.87 f_{y} z} + \frac{M - M_{\text{single}}}{0.87 f_{y} (d - d')}, \text{ where}$$
(BS 3.4.4.4)

$$z = d\left(0.5 + \sqrt{0.25 - \frac{K'}{0.9}}\right) = 0.777d$$
 (BS 3.4.4.4)

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Design of nonuniform thickness slab

7.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

7.5.1.2.2.2 Flanged Slab Section Under Positive Moment

With the flange in compression, the program analyzes the section by considering alternative locations of the neutral axis. Initially the neutral axis is assumed to be located in the flange. Based on this assumption, the program calculates the exact depth of the neutral axis. If the stress block does not extend beyond the flange thickness, the section is designed as a uniform thickness slab of width b_{f} . If the stress block extends beyond the flange depth, the contribution of the web to the flexural strength of the slab is taken into account. See Figure 7-2.



Figure 7-2 Nonuniform Thickness Slab Design

Assuming the neutral axis to lie in the flange, the normalized moment is given by:

$$K = \frac{M}{f_{cu} b_f d^2}$$
(BS 3.4.4.4)

Then the moment arm is computed as:

$$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right\} \le 0.95d$$
 (BS 3.4.4.4)

the depth of the neutral axis is computed as:

$$x = \frac{1}{0.45} (d - z) \tag{BS 3.4.4.4}$$

and the depth of the compression block is given by:

$$a = 0.9x$$
 (BS 3.4.4.4)

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in that case, the width of the slab is taken as b_f . Compression reinforcement is required when K > K'.
- If $a > h_f$, when $M \le \beta_f f_{cu} b d^2$ and $h_f \le 0.45d$, then

$$A_{s} = \frac{M + 0.1 f_{cu} b d \left(0.45 d - h_{f} \right)}{0.87 f_{y} \left(d - 0.5 h_{f} \right)}, \text{ where}$$
(BS 3.4.4.5)

$$\beta_f = 0.45 \frac{h_f}{d} \left(1 - \frac{b_w}{b} \right) \left(1 - \frac{h_f}{2d} \right) + 0.15 \frac{b_w}{b}$$
(BS 3.4.4.5)

Otherwise the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 7-2.

In that case, the ultimate resistance moment of the flange is given by:

$$M_f = 0.45 f_{cu} \left(b_f - b_w \right) h_f \left(d - 0.5 h_f \right)$$
(BS 3.4.4.5)

The moment taken by the web is computed as:

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$$M_{w} = M - M_{f}$$

and the normalized moment resisted by the web is given by:

$$K_{w} = \frac{M_{w}}{f_{cu} b_{w} d^{2}}$$
(BS 3.4.4.4)

• If $K_w \le 0.156$ (BS 3.4.4.4), the slab is designed as a singly reinforced concrete slab. The reinforcement is calculated as the sum of two parts, one to balance compression in the flange and one to balance compression in the web.

$$A_{s} = \frac{M_{f}}{0.87f_{y}(d - 0.5h_{f})} + \frac{M_{w}}{0.87f_{y}z}, \text{ where}$$
$$z = d\left(0.5 + \sqrt{0.25 - \frac{K_{w}}{0.9}}\right) \le 0.95d$$

• If $K_w > K'$ (BS 3.4.4.4), compression reinforcement is required and is calculated as follows:

The ultimate moment of resistance of the web only is given by:

$$M_{uw} = K' f_{cu} b_w d^2$$
 (BS 3.4.4.4)

The compression reinforcement is required to resist a moment of magnitude $M_w - M_{uw}$. The compression reinforcement is computed as:

$$A'_{s} = \frac{M_{w} - M_{uw}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{c}}\right)(d - d')}$$
(BS 3.4.4.4)

where, d' is the depth of the compression reinforcement from the concrete compression face, and

$$f'_{s} = 0.87 f_{y} \text{ if } \frac{d'}{d} \le \frac{1}{2} \left[1 - \frac{f_{y}}{800} \right]$$
 (BS 3.4.4.1, 2.5.3, Fig 2.2)

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$$f'_{s} = E_{s}\varepsilon_{c}\left[1 - \frac{2d'}{d}\right]$$
 if $\frac{d'}{d} > \frac{1}{2}\left[1 - \frac{f_{y}}{800}\right]$ (BS 3.4.4.1, 2.5.3, Fig 2.2)

The area of tension reinforcement is obtained from equilibrium as:

$$A_{s} = \frac{M_{f}}{0.87f_{y}(d-0.5h_{f})} + \frac{M_{uw}}{0.87f_{f}(0.777d)} + \frac{M_{w} - M_{uw}}{0.87f_{y}(d-d')}$$

7.5.1.3 Minimum and Maximum Slab Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (BS 3.12.5.3, BS Table 3.25) with interpolation for reinforcement of intermediate strength:

$$A_{s} \geq \begin{cases} 0.0024bh & \text{if} \quad f_{y} = 250\text{MPa} \\ 0.0013bh & if \quad f_{y} = 500\text{MPa} \end{cases}$$
(BS 3.12.5.3)

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (BS 3.12.6.1).

7.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the shear stress, *v*.
- Determine the shear stress, v_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

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7.5.2.1 Determine Shear Stress

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular strip station are obtained by factoring the corresponding shear forces for different load cases with the corresponding load combination factors. The shear stress is then calculated as:

$$v = \frac{V}{b_w d} \tag{BS 3.4.5.2}$$

The maximum allowable shear stress, v_{max} is defined as:

$$v_{\rm max} = \min(0.8 \sqrt{f_{cu}}, 5 \,\text{MPa})$$
 (BS 3.4.5.2)

For light-weight concrete, v_{max} is defined as:

$$v_{\text{max}} = \min(0.63 \sqrt{f_{cu}}, 4 \text{ MPa})$$
 (BS 8110-2:1985 5.4)

7.5.2.2 Determine Concrete Shear Capacity

The shear stress carried by the concrete, v_c , is calculated as:

$$v'_{c} = v_{c} + 0.6 \frac{NVh}{A_{c}M} \le v_{c} \sqrt{1 + \frac{N}{A_{c}v_{c}}}$$
 (BS 3.4.5.12)

$$v_c = \frac{0.79k_1k_2k_3}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(BS 3.4.5.4, Table 3.8)

 k_1 is the enhancement factor for support compression,

$$k_2 = \left(\frac{f_{cu}}{25}\right)^{\frac{1}{3}}, \ 1 \le k_2 \le \left(\frac{40}{25}\right)^{\frac{1}{3}}$$
 (BS 3.4.5.4, Table 3.8)

$$\gamma_m = 1.25$$
 (BS 2.4.4.1)

However, the following limits also apply:

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$$0.15 \le \frac{100 A_s}{bd} \le 3$$
 (BS 3.4.5.4, Table 3.8)

$$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge 0.67 \text{ (unreinforced) or } \ge 1 \text{ (reinforced)(BS 3.4.5.4, Table 3.8)}$$

$$f_{cu} \le 40$$
 MPa (for calculation purposes only) (BS 3.4.5.4)

$$\frac{Vh}{M} \le 1 \tag{BS 3.4.5.12}$$

 A_s is the area of tension reinforcement.

7.5.2.3 Determine Required Shear Reinforcement

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (BS Table 3.8, BS 3.4.5.3):

• If $v \le (v'_c + 0.4)$,

$$\frac{A_{sv}}{s_v} = \frac{0.4b_w}{0.87f_{yv}}$$
(BS 3.4.5.3, Table 3.7)

• If $(v'_c + 0.4) < v \le v_{\text{max}}$,

$$\frac{A_{sv}}{s_v} = \frac{(v - v'_c)b_w}{0.87f_{yv}}$$
 (BS 3.4.5.3, Table 3.7)

• If $v > v_{\text{max}}$, a failure condition is declared. (BS 3.4.5.2)

In the preceding expressions, a limit is imposed on f_{yv} as:

$$f_{yy} \le 500 \text{ MPa.}$$
 (BS 3.4.5.1)

The maximum of all of the calculated A_{sv}/s_v values, obtained from each load combination, is reported along with the controlling shear force and associated load combination.

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The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

7.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

7.5.3.1 Critical Section for Punching Shear

The punching shear is checked at the face of the column (BS 3.7.6.4) and at a critical section at a distance of 1.5*d* from the face of the support (BS 3.7.7.6). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (BS 3.7.7.1). Figure 7-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 7-3 Punching Shear Perimeters

7.5.3.2 Determine Concrete Capacity

The concrete punching shear factored strength is taken as (BS 3.7.7.4, 3.7.7.6):

$$v_{c} = \frac{0.79k_{1}k_{2}}{\gamma_{m}} \left(\frac{100A_{s}}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(BS 3.4.5.4, Table 3.8)

 k_1 is the enhancement factor for support compression, and is conservatively taken as 1 (BS 3.4.5.8)

$$k_2 = \left(\frac{f_{cu}}{25}\right)^{\frac{1}{3}}, \ 1 \le k_2 \le \left(\frac{40}{25}\right)^{\frac{1}{3}}$$
 (BS 3.4.5.4, Table 3.8)

$$\gamma_m = 1.25$$
 (BS 3.4.5.2)

However, the following limitations also apply:

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$$0.15 \le \frac{100 A_s}{bd} \le 3$$
 (BS 3.4.5.4, Table 3.8)

$$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge 0.67 \text{ (unreinforced) or } \ge 1 \text{ (reinforced)} \tag{BS 3.4.5.4}$$

$$v \le \min(0.8\sqrt{f_{cu}}, 5\text{MPa})$$
 (BS 3.7.6.4)

For light-weight concrete, v_{max} is defined as:

$$v \le \min(0.63\sqrt{f_{cu}}, 4 \text{ MPa})$$
 (BS 8110-2:1985 5.4)

$$f_{cu} \le 40$$
 MPa (for calculation purpose only) (BS 3.4.5.4)

 A_s = area of tension reinforcement, which is taken as the average tension reinforcement of design strips in Layer A and layer B where Layer A and Layer design strips are in orthogonal directions. When design strips are not present in both orthogonal directions then tension reinforcement is taken as zero in the current implementation.

7.5.3.3 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the bending axis, the nominal design shear stress, v_{max} , is calculated as:

$$V_{eff,x} = V \left(f + \frac{1.5M_x}{Vy} \right)$$
(BS 3.7.6.2, 3.7.6.3)
$$V_{eff,y} = V \left(f + \frac{1.5M_y}{Vx} \right)$$
(BS 3.7.6.2, 3.7.6.3)
$$\left(\frac{V_{eff,x}}{u \, d} \right)$$

$$v_{\max} = \max \begin{cases} \boxed{u \, d} \\ \frac{V_{eff,y}}{u \, d} \end{cases}$$
(BS 3.7.7.3)

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where,

- *u* is the perimeter of the critical section
- x and y are the lengths of the sides of the critical section parallel to the axis of bending
- M_x and M_y are the design moments transmitted from the slab to the column at the connection
- V is the total punching shear force
- f is a factor to consider the eccentricity of punching shear force and is taken as:

	1.00	for interior columns	
$f = \langle$	1.25	for edge columns	(BS 3.7.6.2, 3.7.6.3)
	1.25	for corner columns	

7.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

7.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm (BS 3.7.7.5). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is carried out as explained in the subsections that follow.

7.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

7.5.4.2 Determine Required Shear Reinforcement

The shear stress is limited to a maximum of:

$$v_{\rm max} = 2v_c$$
 (BS 3.7.7.5)

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (BS 3.7.7.5).

• If $v \le 1.6v_c$,

$$\frac{A_{\nu}}{s} = \frac{(\nu - \nu_c)ud}{0.87 f_{y\nu}} \ge \frac{0.4ud}{0.87 f_{y\nu}},$$
(BS 3.7.7.5)

• If $1.6v_c \le v < 2.0v_c$,

$$\frac{A_{\nu}}{s} = \frac{5(0.7\nu - \nu_c)ud}{0.87 f_{y\nu}} \ge \frac{0.4ud}{0.87 f_{y\nu}},$$
(BS 3.7.7.5)

• If
$$v > v_{\text{max}}$$
, a failure condition is declared. (BS 3.7.7.5)

If *v* exceeds the maximum permitted value of v_{max} , the concrete section should be increased in size.

7.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 7-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 1.5*d* measured in a direction parallel to the column face (BS 3.7.7.6).

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Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.



Figure 7-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

7.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in BS 3.3 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 10-, 12-, 17-, 16-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 1.5*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$$s_o \le 0.5d$$
 (BS 3.7.7.6)

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$s \leq 0.75d$	(BS 3.7.7.6)
$g \leq 1.5d$	(BS 3.7.7.6)

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Chapter 8 Design for CSA A23.3-14

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Canadian code CSA A23.3-14 [CSA 14] is selected. Various notations used in this chapter are listed in Table 5-1. For referencing to the pertinent sections of the Canadian code in this chapter, a prefix "CSA" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

8.1 Notations

Table 8-1 List of Symbols Used in the CSA A23.3-14 Code

- *A_c* Area enclosed by outside perimeter of concrete cross-section, sq-mm
- A_{ct} Area of concrete on flexural tension side, sq-mm

	List of Symbols Used in the CSA A23.3-14 Code
A_l	Area of longitudinal reinforcement for torsion, sq-mm
A_o	Gross area enclosed by shear flow path, sq-mm
A_{oh}	Area enclosed by centerline of outermost closed transverse tor- sional reinforcement, sq-mm
A_s	Area of tension reinforcement, sq-mm
A'_s	Area of compression reinforcement, sq-mm
$A_{s(required)}$	Area of steel required for tension reinforcement, sq-mm
A_t/s	Area of closed shear reinforcement for torsion per unit length, sq-mm/mm
A_{v}	Area of shear reinforcement, sq-mm
A_v/s	Area of shear reinforcement per unit length, sq-mm/mm
a	Depth of compression block, mm
a_b	Depth of compression block at balanced condition, mm
b	Width of member, mm
b_f	Effective width of flange (flanged section), mm
b_w	Width of web (flanged section), mm
b_0	Perimeter of the punching critical section, mm
b_1	Width of the punching critical section in the direction of bending, mm
b_2	Width of the punching critical section perpendicular to the direc- tion of bending, mm
с	Depth to neutral axis, mm
C_b	Depth to neutral axis at balanced conditions, mm
d	Distance from compression face to tension reinforcement, mm
d_v	Effective shear depth, mm
d'	Distance from compression face to compression reinforcement, mm
h_s	Thickness of slab (flanged section), mm
E_c	Modulus of elasticity of concrete, MPa

Table 8-1 List of Symbols Used in the CSA A23.3-14 Code

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Table 8-1 List of Symbols Used in the CSA A23.3-14 Code		
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 MPa	
f'_c	Specified compressive strength of concrete, MPa	
f'_s	Stress in the compression reinforcement, psi	
f_y	Specified yield strength of flexural reinforcement, MPa	
f_{yt}	Specified yield strength of shear reinforcement, MPa	
h	Overall depth of a section, mm	
I_g	Moment of inertia of gross concrete section about centroidal axis, neglecting reinforcement.	
M_{f}	Factored moment at section, N-mm	
N_{f}	Factored axial force at section, N	
p_c	Outside perimeter of concrete cross-section, mm	
p_h	Perimeter of area Aoh, mm	
S	Spacing of the shear reinforcement along the strip, mm	
S_{z}	Crack spacing parameter	
T_{f}	Factored torsion at section, N-mm	
V_c	Shear resisted by concrete, N	
$V_{r,\max}$	Maximum permitted total factored shear force at a section, N	
V_{f}	Factored shear force at a section, N	
V_s	Shear force at a section resisted by steel, N	
α_l	Ratio of average stress in rectangular stress block to the specified concrete strength	
β	Factor accounting for shear resistance of cracked concrete	
β_l	Factor for obtaining depth of compression block in concrete	
eta_c	Ratio of the maximum to the minimum dimensions of the punch- ing critical section	
\mathcal{E}_{C}	Strain in concrete	
\mathcal{E}_{S}	Strain in reinforcing steel	
\mathcal{E}_{x}	Longitudinal strain at mid-depth of the section	

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Table 8-1 List of Symbols Used in the CSA A23.3-14 Code		
ϕ_c	Strength reduction factor for concrete	
ϕ_s	Strength reduction factor for steel	
ϕ_m	Strength reduction factor for member	
γf	Fraction of unbalanced moment transferred by flexure	
γ_{ν}	Fraction of unbalanced moment transferred by eccentricity of shear	
θ	Angle of diagonal compressive stresses, degrees	
λ	Shear strength factor	

8.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For CSA A23.3-14, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earth-quake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (CSA 8.3.2, Table C.1a)

1.4D	(CSA 8.3.2, Table C.1a Case 1)
$\begin{array}{l} 1.25D+1.5L\\ 1.25D+1.5L+1.0S\\ 1.25D+1.5L\pm0.4W\\ 0.9D+1.5L\\ 0.9D+1.5L+1.0S\\ 0.9D+1.5L\pm0.4W \end{array}$	(CSA 8.3.2, Table C.1a Case 2)
1.25D + 1.5(0.75 PL)	(CSA 13.8.4.3)
$\begin{array}{l} 1.25D + 1.5S \\ 1.25D + 1.5S + 0.5L \\ 1.25D + 1.5S \pm 0.4W \\ 0.9D + 1.5S \\ 0.9D + 1.5S + 0.5L \\ 0.9D + 1.5S \pm 0.4W \end{array}$	(CSA 8.3.2, Table C.1a Case 3)

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```
\begin{array}{l} 1.25D \pm 1.4W \\ 1.25D \pm 0.5L \pm 1.4W \\ 1.25D \pm 0.5S \pm 1.4W \\ 0.9D \pm 1.4W \\ 0.9D \pm 0.5L \pm 1.4W \\ 0.9D \pm 0.5L \pm 1.4W \\ 0.9D \pm 0.5S \pm 1.4W \\ 1.0D \pm 1.0E \\ 1.0D \pm 0.5L \pm 1.0E \\ 1.0D \pm 0.25S \pm 1.0E \end{array} (CSA 8.3.2, Table C.1a Case 5) \\ 1.0D \pm 0.25S \pm 1.0E \\ \end{array}
```

These are also the default design load combinations in ETABS whenever the CSA A23.3-14 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

8.3 Limits on Material Strength

The upper and lower limits of f'_c are 80 MPa and 20 MPa, respectively, for all framing types (CSA 8.6.1.1).

$$20 \text{ MPa} \le f'_c \le 80 \text{ MPa}$$
 (CSA 8.6.1.1)

The upper limit of f_y is 500 MPa for all frames (CSA 8.5.1).

$$f_y \le 500 \text{ MPa}$$
 (CSA 8.5.1)

ETABS enforces the upper material strength limits for flexure and shear design of slabs. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. The user is responsible for ensuring that the minimum strength is satisfied.

8.4 Strength Reduction Factors

The strength reduction factors, ϕ , are material dependent and defined as:

$\phi_c = 0.65$ for concrete	(CSA 8.4.2)
$\phi_s = 0.85$ for reinforcement	(CSA 8.4.3a)

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These values can be overwritten; however, caution is advised.

8.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

8.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

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8.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

8.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 8-1 (CSA 10.1.7). Furthermore, it is assumed that the compression carried by the concrete is less than or equal to that which can be carried at the balanced condition (CSA 10.1.4). When the applied moment exceeds the moment capacity at the balanced condition, the area of compression reinforcement is calculated assuming that the additional moment will be carried by compression and additional tension reinforcement.

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed (0.1 $f'_c A_g$), axial force is ignored; hence, all slabs are designed for major direction flexure, shear, and punching shear only. Axial compression greater than $0.1f'_c A_g$ and axial tensions are always included in flexural and shear design.

8.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive moment, M_f (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 8-1), where,



Figure 8-1 Uniform Thickness Slab Design

$$a = d - \sqrt{d^2 - \frac{2|M_f|}{\alpha_1 f'_c \phi_c b}}$$
(CSA 10.1)

where the value of ϕ_c is 0.65 (CSA 8.4.2) in the preceding and the following equations. The parameters α_l , β_l , and c_b are calculated as:

 $\alpha_l = 0.85 - 0.0015 f'_c \ge 0.67, \tag{CSA 10.1.7}$

$$\beta_I = 0.97 - 0.0025 f'_c \ge 0.67, \tag{CSA 10.1.7}$$

$$c_b = \frac{700}{700 + f_y} d \tag{CSA 10.5.2}$$

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The balanced depth of the compression block is given by:

$$a_b = \beta_l c_b \tag{CSA 10.1.7}$$

• If $a \le a_b$ (CSA 10.5.2), the area of tension reinforcement is given by:

$$A_{s} = \frac{M_{f}}{\phi_{s} f_{y} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M_f is positive, or at the top if M_f is negative.

• If *a* > *a_b* (CSA 10.5.2), compression reinforcement is required and is calculated as follows:

The factored compressive force developed in the concrete alone is given by:

$$C = \phi_c \alpha_1 f'_c b a_b \tag{CSA 10.1.7}$$

and the factored moment resisted by concrete compression and tension reinforcement is:

$$M_{fc} = C\left(d - \frac{a_b}{2}\right)$$

Therefore, the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{fs} = M_f - M_{fc}$$

The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{fs}}{(\phi_{s}f'_{s} - \phi_{c}\alpha_{1}f'_{c})(d - d')}, \text{ where}$$
$$f'_{s} = 0.0035 E_{s} \left[\frac{c - d'}{c}\right] \le f_{y}$$
(CSA 10.1.2, 10.1.3)

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The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{fc}}{f_y \left(d - \frac{a_b}{2}\right)\phi_s}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{fs}}{f_y (d - d') \phi_s}$$

Therefore, the total tension reinforcement, $A_s = A_{sI} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M_f is positive, and vice versa if M_f is negative.

8.5.1.2.2 Design of nonuniform thickness slab

8.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_f (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

8.5.1.2.2.2 Flanged Slab Section Under Positive Moment

• If $M_f > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M_f}{\alpha_1 f'_c \phi_c b_f}}$$
(CSA 10.1)

where, the value of ϕ_c is 0.65 (CSA 8.4.2) in the preceding and the following equations. The parameters α_l , β_l , and c_b are calculated as:

$$\alpha_l = 0.85 - 0.0015 f'_c \ge 0.67, \tag{CSA 10.1.7}$$

$$\beta_I = 0.97 - 0.0025 f'_c \ge 0.67,$$
 (CSA 10.1.7)

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Figure 8-2 Nonuniform Thickness Slab Design

The balanced depth of the compression block is given by:

 $a_b = \beta_l c_b \tag{CSA 10.1.4,10.1.7}$

- If $a \le h_s$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in this case the width of the slab is taken as b_f . Compression reinforcement is required when $a > a_b$.
- If a > h_s, calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f, and the second part is for balancing the compressive force from the web, C_w as shown in Figure 8-2. C_f is given by:

$$C_f = \alpha_1 f'_c \left(b_f - b_w \right) \min\left(h_s, a_b \right)$$
(CSA 10.1.7)

Therefore, $A_{s1} = \frac{C_f \phi_c}{f_y \phi_s}$ and the portion of M_f that is resisted by the flange is given by:

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$$M_{ff} = C_f \left(d - \frac{\min(h_s, a_b)}{2} \right) \phi_c$$

Therefore, the balance of the moment, M_f to be carried by the web is:

$$M_{fw} = M_f - M_{ff}$$

The web is a rectangular section with dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{fw}}{\alpha_1 f'_c \phi_c b_w}}$$
(CSA 10.1)

• If $a_1 \le a_b$ (CSA 10.5.2), the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_{fw}}{\phi_s f_y \left(d - \frac{a_1}{2}\right)}, \text{ and}$$

$$A_s = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged slab.

• If $a_1 > a_b$ (CSA 10.5.2), compression reinforcement is required and is calculated as follows:

The compressive force in the web concrete alone is given by:

$$C = \phi_c \alpha_1 f'_c b_w a_b \tag{CSA 10.1.7}$$

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{fc} = C\left(d - \frac{a_b}{2}\right)$$

and the moment resisted by compression and tension reinforcement is:

$$M_{fs} = M_{fw} - M_{fc}$$

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Therefore, the compression reinforcement is computed as:

$$A'_{s} = \frac{M_{fs}}{\left(\phi_{s}f'_{c} - \phi_{c}\alpha_{1}f'_{c}\right)\left(d - d'\right)}, \text{ where}$$
$$f'_{s} = \varepsilon_{c}E_{s}\left[\frac{c - d'}{c}\right] \le f_{y} \tag{CSA 10.1.2, 10.1.3}$$

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{fc}}{f_y \left(d - \frac{a_b}{2}\right)\phi_s}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{fs}}{f_y \left(d - d' \right) \phi_s}$$

The total tension reinforcement is $A_s = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

8.5.1.3 Minimum and Maximum Reinforcement

The minimum flexural tensile reinforcement required for each direction of a slab is given by the following limit (CSA 13.10.1):

 $A_s \ge 0.002 \ bh \tag{CSA 7.8.1}$

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

8.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V_f.
- Determine the shear force, V_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three subsections describe in detail the algorithms associated with these steps.

8.5.2.1 Determine Factored Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

8.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_c , is calculated as:

$$V_c = \phi_c \lambda \beta \sqrt{f'_c b_w d_v}$$
(CSA 11.3.4)

$$\sqrt{f'_c} \le 8 \text{ MPa}$$
 (CSA 11.3.4)

- ϕ_c is the resistance factor for concrete. By default it is taken as 0.65 (CSA 8.4.2).
- λ is the strength reduction factor to account for low density concrete (CSA 2.2). For normal density concrete, its value is 1 (CSA 8.6.5), which is taken by the program as the default value. For concrete using lower density aggregate, the user can change the value of λ in the material property data. The recommended value for λ is as follows (CSA 8.6.5):

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- 1.00, for normal density concrete,
- 0.85, for semi-low-density concrete
- $\lambda = \{$ in which all of the fine aggregate is natural sand, (CSA 8.6.5)
 - 0.75, for semi-low-density concrete
 - in which none of the fine aggregate is natural sand.
- β is the factor for accounting for the shear resistance of cracked concrete (CSA 2.2) and should be greater or equal to 0.05. Its value is normally between 0.1 and 0.4. It is determined according to CSA 11.3.6, and described further in the following sections.
- b_w is the effective web width. For uniform thickness slab, it is the width of the slab. For flanged-shaped slab, it is the width of the web of the slab.
- d_{ν} is the effective shear depth. It is taken as the greater of 0.9*d* or 0.72*h*(CSA 2.3), where *d* is the distance from the extreme compression fiber to the centroid of the tension reinforcement, and *h* is the overall depth of the cross-section in the direction of the shear force (CSA 2.3).

The value of β is preferably taken as the special value (CSA 11.3.6.2) or it is determined using the simplified method (CSA 11.3.6.3), if applicable. When the conditions of the special value or simplified method do not apply, the general method is used (CSA 11.3.6.4).

If the overall slab depth, *h*, is less than 250 mm or if the depth of a flanged below the slab is not greater than one-half of the width of the web or 350 mm, β is taken as 0.21 (CSA 11.3.6.2).

When the specified yield strength of the longitudinal reinforcing f_y does not exceed 400 MPa, the specified concrete strength f'_c does not exceed 60 MPa, and the tensile force is negligible, β is determined in accordance with the simplified method, as follows (CSA 11.3.6.3):

• When the section contains at least the minimum transverse reinforcement, β is taken as 0.18 (CSA 11.6.3.3a).

$\beta = 0.18$	(CSA 11.3.6.3(a))
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 When the section contains no transverse reinforcement, β is determined based on the specified maximum nominal size of coarse aggregate, a_g.

For a maximum size of coarse aggregate not less than 20 mm, β is taken as:

$$\beta = \frac{230}{1000 + d_v} \tag{CSA 11.3.6.3(b)}$$

where d_{v} is the effective shear depth expressed in millimeters.

For a maximum size of coarse aggregate less than 20 mm, β is taken as:

$$\beta = \frac{230}{1000 + s_{ze}}$$
(CSA 11.3.6.3 c)

where,
$$s_{ze} = \frac{35s_z}{15 + a_e} \ge 0.85s_z$$
 (CSA 11.3.6.3.c)

In the preceding expression, the crack spacing parameter, s_{ze} , shall be taken as the minimum of d_v and the maximum distance between layers of distributed longitudinal reinforcement. However, s_{ze} is conservatively taken as equal to d_v .

In summary, for simplified cases, β can be expressed as follows:

- $\beta = \begin{cases} 0.18, & \text{if minimum transverse reinforcement is provided,} \\ \frac{230}{1000 + d_v}, & \text{if no transverse reinforcement is provided, and } a_g \ge 20\text{mm,} \\ \frac{230}{1000 + S_{ze}}, & \text{if no transverse reinforcement is provided, and } a_g < 20\text{mm.} \end{cases}$
- When the specified yield strength of the longitudinal reinforcing f_y is greater than 400 MPa, the specified concrete strength f'_c is greater than 60 MPa, or tension is not negligible, β is determined in accordance with the general method as follows (CSA 11.3.6.1, 11.3.6.4):

$$\beta = \frac{0.40}{(1+1500\varepsilon_x)} \bullet \frac{1300}{(1000+S_{ze})}$$
(CSA 11.3.6.4)

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In the preceding expression, the equivalent crack spacing parameter, s_{ze} is taken equal to 300 mm if minimum transverse reinforcement is provided (CSA 11.3.6.4). Otherwise it is determined as stated in the simplified method.

$$S_{ze} = \begin{cases} 300 & \text{if minimum transverse reinforcement is provided,} \\ \frac{35}{15 + a_g} S_z \ge 0.85S_z & \text{otherwise.} \end{cases}$$
(CSA 11.3.6.3, 11.3.6.4)

The value of a_g in the preceding equations is taken as the maximum aggregate size for f'_c of 60 MPa, is taken as zero for f'_c of 70 MPa, and linearly interpolated between these values (CSA 11.3.6.4).

The longitudinal strain, ε_x at mid-depth of the cross-section is computed from the following equation:

$$\varepsilon_{x} = \frac{M_{f}/d_{v} + V_{f} + 0.5N_{f}}{2(E_{x}A_{x})}$$
(CSA 11.3.6.4)

In evaluating ε_x the following conditions apply:

• \mathcal{E}_x is positive for tensile action.

• V_f and M_f are taken as positive quantities.	(CSA 11.3.6.4(a))
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- M_f is taken as a minimum of $V_f d_v$. (CSA 11.3.6.4(a))
- N_f is taken as positive for tension. (CSA 2.3)

 A_s is taken as the total area of longitudinal reinforcement in the slab. It is taken as the envelope of the reinforcement required for all design load combinations. The actual provided reinforcement might be slightly higher than this quantity. The reinforcement should be developed to achieve full strength (CSA 11.3.6.3(b)).

If the value of ε_x is negative, it is recalculated with the following equation, in which A_{ct} is the area of concrete in the flexural tensile side of the slab, taken as half of the total area.

$$\varepsilon_{x} = \frac{M_{f}/d_{v} + V_{f} + 0.5N_{f}}{2(E_{s}A_{s} + E_{c}A_{ct})}$$
(CSA 11.3.6.4(c))
$$E_{s} = 200,000 \text{ MPa}$$
(CSA 8.5.4.1)
$$E_{c} = 4500\sqrt{f_{c}} \text{ MPa}$$
(CSA 8.6.2.3)

If the axial tension is large enough to induce tensile stress in the section, the value of ε_x is doubled (CSA 11.3.6.4(e)).

For sections closer than d_v from the face of the support, ε_x is calculated based on M_f and V_f at a section at a distance d_v from the face of the support (CSA 11.3.6.4(d)). This condition currently is not checked by ETABS.

An upper limit on ε_x is imposed as:

$$\varepsilon_x \le 0.003$$
 (CSA 11.3.6.4(f))

In both the simplified and general methods, the shear strength of the section due to concrete, v_c depends on whether the minimum transverse reinforcement is provided. To check this condition, the program performs the design in two passes. In the first pass, it assumes that no transverse shear reinforcement is needed. When the program determines that shear reinforcement is required, the program performs the second pass assuming that at least minimum shear reinforcement is provided.

8.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to $V_{r \max}$ where:

$$V_{r,\max} = 0.25\phi_c f'_c b_w d$$
 (CSA 11.3.3)

Given V_f , V_c , and $V_{r,max}$, the required shear reinforcement is calculated as follows:

• If
$$V_f \leq V_c$$
,

$$\frac{A_v}{s} = 0$$
(CSA 11.3.5.1)

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• If
$$V_c < V_f \leq V_{r,\max}$$
,
$$\frac{A_v}{s} = \frac{(V_f - V_c)\tan\theta}{\phi_s f_{vt} d_v}$$
(CSA 11.3.3, 11.3.5.1)

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• If $V_f > V_{r,max}$, a failure condition is declared. (CSA 11.3.3)

A minimum area of shear reinforcement is provided in the following regions (CSA 11.2.8.1):

- (a) in regions of flexural members where the factored shear force V_f exceeds V_c
- (b) in regions of slab with an overall depth greater than 750 mm.

Where the minimum shear reinforcement is required by CSA 11.2.8.1, or by calculation, the minimum area of shear reinforcement per unit spacing is taken as:

$$\frac{A_{v}}{s} \ge 0.06 \frac{\sqrt{f'_{c}}}{f_{vt}} b_{w}$$
(CSA 11.2.8.2)

In the preceding equations, the term θ is used, where θ is the angle of inclination of the diagonal compressive stresses with respect to the longitudinal axis of the member (CSA 2.3). The θ value is normally between 22 and 44 degrees. It is determined according to CSA 11.3.6.

Similar to the β factor, which was described previously, the value of θ is preferably taken as the special value (CSA 11.3.6.2), or it is determined using the simplified method (CSA 11.3.6.3), whenever applicable. The program uses the general method when conditions for the simplified method are not satisfied (CSA 11.3.6.4).

- If the overall slab depth, h, is less than 250 mm or if the depth of the flanged slab below the slab is not greater than one-half of the width of the web or 350 mm, θ is taken as 42 degrees (CSA 11.3.6.2).
- If the specified yield strength of the longitudinal reinforcing f_y does not exceed 400 MPa, or the specified concrete strength f_c does not exceed 60 MPa, θ is taken to be 35 degree (CSA 11.3.6.3).

$$\theta = 35^{\circ} \text{ for } P_f \le 0 \text{ or } f_y \le 400 \text{ MPa or } f'_c \le 60 \text{ MPa}$$
 (CSA11.3.6.3)

• If the axial force is tensile, the specified yield strength of the longitudinal reinforcing $f_y > 400$ MPa, and the specified concrete strength $f'_c > 60$ MPa, θ is determined using the general method as follows (CSA 11.3.6.4),

$$\theta = 29 + 7000\varepsilon_x \text{ for } P_f < 0, \ f_y > 400 \text{ MPa}, f'_c \le 60 \text{ MPa} \quad (\text{CSA11.3.6.4})$$

where ε_x is the longitudinal strain at the mid-depth of the cross-section for the factored load. The calculation procedure is described in preceding sections.

The maximum of all of the calculated A_v/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

8.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

8.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (CSA 13.3.3.1 and CSA 13.3.3.2). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (CSA 13.3.3.3). Figure 8-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.

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Figure 8-3 Punching Shear Perimeters

8.5.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be $\gamma_f M_u$ and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $\gamma_v M_u$, where

$$\gamma_f = \frac{1}{1 + (2/3)\sqrt{b_1/b_2}}, \text{ and}$$
 (CSA 13.10.2)

$$\gamma_{\nu} = 1 - \frac{1}{1 + (2/3)\sqrt{b_1/b_2}},$$
 (CSA 13.3.5.3)

where b_1 is the width of the critical section measured in the direction of the span, and b_2 is the width of the critical section measured in the direction perpendicular to the span.

8.5.3.3 Determination of Concrete Capacity

The concrete punching shear factored strength is taken as the minimum of the following three limits:

$$v_{v} = \min \begin{cases} \phi_{c} \left(1 + \frac{2}{\beta_{c}}\right) 0.19\lambda \sqrt{f'_{c}} \\ \phi_{c} \left(0.19 + \frac{\alpha_{s}d}{b_{0}}\right) \lambda \sqrt{f'_{c}} \\ \phi_{c} 0.38\lambda \sqrt{f'_{c}} \end{cases}$$
(CSA 13.3.4.1)

where, β_c is the ratio of the minimum to the maximum dimensions of the critical section, b_0 is the perimeter of the critical section, and α_s is a scale factor based on the location of the critical section.

$$\alpha_s = \begin{cases} 4, \text{ for interior columns} \\ 3, \text{ for edge colums, and} \\ 2, \text{ for corner columns.} \end{cases}$$
(CSA 13.3.4.1(b))

The value of $\sqrt{f'_c}$ is limited to 8 MPa for the calculation of the concrete shear capacity (CSA 13.3.4.2).

If the effective depth, *d*, exceeds 300 mm, the value of v_c is reduced by a factor equal to 1300/(1000 + d) (CSA 13.3.4.3).

8.5.3.4 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v_{f} = \frac{V_{f}}{bod} + \frac{\gamma v_{2}[M_{f2} - V_{f}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{f3} - V_{f}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "sides" refers to the sides of the critical section for punching shear Eq. 2

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$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "sides" refers to the sides of the critical section for punching shear Eq. 4

The equations for \overline{I}_{22} , \overline{I}_{33} , and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 2-axis or parallel to the 3-axis. Refer to Figures 8-4.



Figure 8-4 Shear Stress Calculations at Critical Sections

$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for side of critical section parallel to 2-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2$$
, for side of critical section
parallel to 3-axis Eq. 5b

$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - x_3)^2$$
, for side of critical section
parallel to 2-axis Eq. 6a

$$\overline{I}_{33} = Ld(x_2 - x_3)^2$$
, for side of critical section parallel to 3-axis Eq. 6b

$$\overline{I}_{23} = Ld(x_2 - x_3)(y_2 - y_3)$$
, for side of critical section parallel
to 2-axis or 3-axis Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

where,

- b_0 = Perimeter of the critical section for punching shear
- d = Effective depth at the critical section for punching shear based on the average of d for 2 direction and d for 3 direction
- I_{22} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 2-axis
- I_{33} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of inertia of the critical section for punching shear with respect to the 2 and 3 planes
- *L* = Length of the side of the critical section for punching shear currently being considered
- M_{f2} = Moment about the line parallel to the 2-axis at the center of the column (positive in accordance with the right-hand rule)

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- M_{f3} = Moment about the line parallel to the 3-axis at the center of the column (positive in accordance with the right-hand rule)
- V_f = Punching shear stress
- V_f = Shear at the center of the column (positive upward)
- x_1, y_1 = Coordinates of the column centroid
- x_2, y_2 = Coordinates of the center of one side of the critical section for punching shear
- x_3 , y_3 = Coordinates of the centroid of the critical section for punching shear
- x_4 , y_4 = Coordinates of the location where stress is being calculated
- γ_{V2} = Percent of M_{f2} resisted by shear
- γ_{V3} = Percent of M_{f3} resisted by shear

8.5.3.5 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

8.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm (CSA 13.2.1). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed, and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is performed as explained in the subsections that follow.

8.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is taken as:

$$v_c = 0.28\lambda \phi_c \sqrt{f'_c}$$
 for shear studs (CSA 13.3.8.3)

$$v_c = 0.19\lambda \phi_c \sqrt{f'_c}$$
 for shear stirrups (CSA 13.3.9.3)

8.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of $v_{r \max}$, where

$$v_{r,\max} = 0.75\lambda \phi_c \sqrt{f'_c}$$
 for shear studs (CSA 13.3.8.2)

$$v_{r,\max} = 0.55\lambda \phi_c \sqrt{f'_c}$$
 for shear stirrups (CSA 13.3.9.2)

Given v_f , v_c , and $v_{f,max}$, the required shear reinforcement is calculated as follows, where, ϕ_s , is the strength reduction factor.

• If $v_f > v_{r, \max}$,

$$\frac{A_{v}}{s} = \frac{\left(v_{f} - v_{c}\right)}{\phi_{s} f_{yv}} b_{o}$$
(CSA 13.3.8.5, 13.3.9.4)

- If $v_f > v_{r, \max}$, a failure condition is declared. (CSA 13.3.8.2)
- If v_f exceeds the maximum permitted value of v_{rmax}, the concrete section should be increased in size.

8.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 8-5 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

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Figure 8-5 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed

0.4d for shear studs	(CSA 13.3.8.6)
0.25d for shear stirrups	(CSA 13.3.8.6)

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

8.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in CSA 7.9 plus half of the diameter of the flexural reinforcement.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.45*d* to 0.4*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

 $s_o \le 0.4d$ (CSA 13.3.8.6)

$$s \leq \begin{cases} 0.75d \quad v_f \leq 0.56\lambda \phi_c \sqrt{f'_c} \\ 0.50d \quad v_f > 0.56\lambda \phi_c \sqrt{f'_c} \end{cases}$$
(CSA 13.3.8.6)

For shear stirrups,

$$s_o \le 0.25d$$
 (CSA 13.3.9.5)
 $s \le 0.25d$ (CSA 13.3.9.5)

The minimum depth for reinforcement should be limited to 300 mm (CSA 13.3.9.1).

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Chapter 9 Design for CSA A23.3-04

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Canadian code CSA A23.3-04 [CSA 04] is selected. Various notations used in this chapter are listed in Table 9-1. For referencing to the pertinent sections of the Canadian code in this chapter, a prefix "CSA" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

9.1 Notations

Table 9-1 List of Symbols Used in the CSA A23.3-04 Code

- *A_c* Area enclosed by outside perimeter of concrete cross-section, sq-mm
- A_{ct} Area of concrete on flexural tension side, sq-mm

	List of Symbols Used in the CSA A23.3-04 Code
A_l	Area of longitudinal reinforcement for torsion, sq-mm
A_o	Gross area enclosed by shear flow path, sq-mm
A_{oh}	Area enclosed by centerline of outermost closed transverse tor- sional reinforcement, sq-mm
A_s	Area of tension reinforcement, sq-mm
A'_s	Area of compression reinforcement, sq-mm
$A_{s(required)}$	Area of steel required for tension reinforcement, sq-mm
A_t/s	Area of closed shear reinforcement for torsion per unit length, sq-mm/mm
A_{v}	Area of shear reinforcement, sq-mm
A_v/s	Area of shear reinforcement per unit length, sq-mm/mm
a	Depth of compression block, mm
a_b	Depth of compression block at balanced condition, mm
b	Width of member, mm
b_f	Effective width of flange (flanged section), mm
b_w	Width of web (flanged section), mm
b_0	Perimeter of the punching critical section, mm
b_1	Width of the punching critical section in the direction of bending, mm
b_2	Width of the punching critical section perpendicular to the direc- tion of bending, mm
С	Depth to neutral axis, mm
C_b	Depth to neutral axis at balanced conditions, mm
d	Distance from compression face to tension reinforcement, mm
d_v	Effective shear depth, mm
d'	Distance from compression face to compression reinforcement, mm
h_s	Thickness of slab (flanged section), mm
E_c	Modulus of elasticity of concrete, MPa

Table 9-1 List of Symbols Used in the CSA A23.3-04 Code

9-2 Notations

Table 9-1 List of Symbols Used in the CSA A23.3-04 Code		
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 MPa	
f'_c	Specified compressive strength of concrete, MPa	
f'_s	Stress in the compression reinforcement, psi	
f_y	Specified yield strength of flexural reinforcement, MPa	
f_{yt}	Specified yield strength of shear reinforcement, MPa	
h	Overall depth of a section, mm	
I_g	Moment of inertia of gross concrete section about centroidal axis, neglecting reinforcement.	
M_{f}	Factored moment at section, N-mm	
N_{f}	Factored axial force at section, N	
p_c	Outside perimeter of concrete cross-section, mm	
p_h	Perimeter of area Aoh, mm	
S	Spacing of the shear reinforcement along the strip, mm	
S_{z}	Crack spacing parameter	
T_{f}	Factored torsion at section, N-mm	
V_c	Shear resisted by concrete, N	
$V_{r,\max}$	Maximum permitted total factored shear force at a section, N	
V_f	Factored shear force at a section, N	
V_s	Shear force at a section resisted by steel, N	
α_l	Ratio of average stress in rectangular stress block to the specified concrete strength	
β	Factor accounting for shear resistance of cracked concrete	
β_l	Factor for obtaining depth of compression block in concrete	
eta_c	Ratio of the maximum to the minimum dimensions of the punch- ing critical section	
\mathcal{E}_{C}	Strain in concrete	
\mathcal{E}_{s}	Strain in reinforcing steel	
\mathcal{E}_{x}	Longitudinal strain at mid-depth of the section	

Notations 9 - 3

Table 9-1 List of Symbols Used in the CSA A23.3-04 Code		
ϕ_c	Strength reduction factor for concrete	
ϕ_s	Strength reduction factor for steel	
ϕ_m	Strength reduction factor for member	
γf	Fraction of unbalanced moment transferred by flexure	
γ_{ν}	Fraction of unbalanced moment transferred by eccentricity of shear	
θ	Angle of diagonal compressive stresses, degrees	
λ	Shear strength factor	

9.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For CSA A23.3-04, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earth-quake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (CSA 8.3.2, Table C.1)

1.4D	(CSA 8.3.2, Table C.1 Case 1)
1.25D + 1.5L	
1.25D + 1.5L + 0.5S	
$1.25D + 1.5L \pm 0.4W$	
0.9D + 1.5L	(CSA 8.3.2, Table C.1 Case 2)
0.9D + 1.5L + 0.5S	
$0.9D + 1.5L \pm 0.4W$	
1.25D + 1.5(0.75 PL)	(CSA 13.8.4.3)
1.25D + 1.5S	
1.25D + 1.5S + 0.5L	
$1.25D + 1.5S \pm 0.4W$	
0.9D + 1.5S	(CSA 8.3.2, Table C.1 Case 3)
0.9D + 1.5S + 0.5L	
$0.9D + 1.5S \pm 0.4W$	

9 - 4 Design Load Combinations

```
\begin{array}{ll} 1.25D \pm 1.4W \\ 1.25D \pm 0.5L \pm 1.4W \\ 1.25D \pm 0.5S \pm 1.4W \\ 0.9D \pm 1.4W \\ 0.9D \pm 0.5L \pm 1.4W \\ 0.9D \pm 0.5L \pm 1.4W \\ 1.0D \pm 0.5S \pm 1.4W \\ 1.0D \pm 1.0E \\ 1.0D \pm 0.5L \pm 1.0E \\ 1.0D \pm 0.25S \pm 1.0E \end{array} (CSA 8.3.2, Table C.1 Case 5) \\ 1.0D \pm 0.25S \pm 1.0E \\ \end{array}
```

These are also the default design load combinations in ETABS whenever the CSA A23.3-04 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

9.3 Limits on Material Strength

The upper and lower limits of f'_c are 80 MPa and 20 MPa, respectively, for all framing types (CSA 8.6.1.1).

$$20 \text{ MPa} \le f'_c \le 80 \text{ MPa}$$
 (CSA 8.6.1.1)

The upper limit of f_y is 500 MPa for all frames (CSA 8.5.1).

$$f_y \le 500 \text{ MPa} \tag{CSA 8.5.1}$$

ETABS enforces the upper material strength limits for flexure and shear design slabs. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. The user is responsible for ensuring that the minimum strength is satisfied.

9.4 Strength Reduction Factors

The strength reduction factors, ϕ , are material dependent and defined as:

$\phi_c = 0.65$ for concrete	(CSA 8.4.2)
$\phi_s = 0.85$ for reinforcement	(CSA 8.4.3a)

Limits on Material Strength 9 - 5

These values can be overwritten; however, caution is advised.

9.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

9.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

9 - 6 Slab Design

9.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

9.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 9-1 (CSA 10.1.7). Furthermore, it is assumed that the compression carried by the concrete is less than or equal to that which can be carried at the balanced condition (CSA 10.1.4). When the applied moment exceeds the moment capacity at the balanced condition, the area of compression reinforcement is calculated assuming that the additional moment will be carried by compression and additional tension reinforcement.

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed ($0.1 f'_c A_g$), axial force is ignored; hence, all slabs are designed for major direction flexure, shear, and torsion only. Axial compression greater than $0.1 f'_c A_g$ and axial tensions are always included in flexural and shear design.

9.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive moment, M_f (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 9-1), where,



Figure 9-1 Uniform Thickness Slab Design

$$a = d - \sqrt{d^2 - \frac{2\left|M_f\right|}{\alpha_1 f'_c \phi_c b}}$$
(CSA 10.1)

where the value of ϕ_c is 0.65 (CSA 8.4.2) in the preceding and the following equations. The parameters α_l , β_l , and c_b are calculated as:

 $\alpha_l = 0.85 - 0.0015 f'_c \ge 0.67, \tag{CSA 10.1.7}$

$$\beta_I = 0.97 - 0.0025 f'_c \ge 0.67, \tag{CSA 10.1.7}$$

$$c_b = \frac{700}{700 + f_y} d \tag{CSA 10.5.2}$$

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The balanced depth of the compression block is given by:

$$a_b = \beta_l c_b \tag{CSA 10.1.7}$$

• If $a \le a_b$ (CSA 10.5.2), the area of tension reinforcement is given by:

$$A_{s} = \frac{M_{f}}{\phi_{s} f_{y} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M_f is positive, or at the top if M_f is negative.

• If *a* > *a_b* (CSA 10.5.2), compression reinforcement is required and is calculated as follows:

The factored compressive force developed in the concrete alone is given by:

$$C = \phi_c \alpha_1 f'_c b a_b \tag{CSA 10.1.7}$$

and the factored moment resisted by concrete compression and tension reinforcement is:

$$M_{fc} = C\left(d - \frac{a_b}{2}\right)$$

Therefore, the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{fs} = M_f - M_{fc}$$

The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{fs}}{(\phi_{s}f'_{s} - \phi_{c}\alpha_{1}f'_{c})(d - d')}, \text{ where}$$
$$f'_{s} = 0.0035 E_{s} \left[\frac{c - d'}{c}\right] \le f_{y}$$
(CSA 10.1.2, 10.1.3)

The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{fc}}{f_y \left(d - \frac{a_b}{2}\right)\phi_s}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{fs}}{f_y (d - d') \phi_s}$$

Therefore, the total tension reinforcement, $A_s = A_{s1} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M_f is positive, and vice versa if M_f is negative.

9.5.1.2.2 Design of nonuniform thickness slab

9.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_f (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

9.5.1.2.2.2 Flanged Slab Section Under Positive Moment

• If $M_f > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2M_f}{\alpha_1 f'_c \phi_c b_f}}$$
(CSA 10.1)

where, the value of ϕ_c is 0.65 (CSA 8.4.2) in the preceding and the following equations. The parameters α_l , β_l , and c_b are calculated as:

$$\alpha_l = 0.85 - 0.0015 f'_c \ge 0.67, \tag{CSA 10.1.7}$$

$$\beta_l = 0.97 - 0.0025 \, f'_c \ge 0.67, \tag{CSA 10.1.7}$$

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Figure 9-2 Nonuniform Thickness Slab Design

The balanced depth of the compression block is given by:

 $a_b = \beta_1 c_b \tag{CSA 10.1.4, 10.1.7}$

- If $a \le h_s$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in this case the width of the slab is taken as b_f . Compression reinforcement is required when $a > a_b$.
- If $a > h_s$, calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w as shown in Figure 9-2. C_f is given by:

$$C_f = \alpha_1 f'_c \left(b_f - b_w \right) \min\left(h_s, a_b \right)$$
(CSA 10.1.7)

Therefore, $A_{s1} = \frac{C_f \phi_c}{f_y \phi_s}$ and the portion of M_f that is resisted by the flange is given by:

$$M_{ff} = C_f \left(d - \frac{\min(h_s, a_b)}{2} \right) \phi_c$$

Therefore, the balance of the moment, M_f to be carried by the web is:

$$M_{fw} = M_f - M_{ff}$$

The web is a rectangular section with dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_{1} = d - \sqrt{d^{2} - \frac{2M_{fw}}{\alpha_{1} f'_{c} \phi_{c} b_{w}}}$$
(CSA 10.1)

• If $a_1 \le a_b$ (CSA 10.5.2), the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_{fw}}{\phi_s f_y \left(d - \frac{a_1}{2}\right)}, \text{ and}$$

$$A_s = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged slab.

• If $a_1 > a_b$ (CSA 10.5.2), compression reinforcement is required and is calculated as follows:

The compressive force in the web concrete alone is given by:

$$C = \phi_c \alpha_1 f'_c b_w a_b \tag{CSA 10.1.7}$$

Therefore the moment resisted by the concrete web and tension reinforcement is:

$$M_{fc} = C\left(d - \frac{a_b}{2}\right)$$

and the moment resisted by compression and tension reinforcement is:

$$M_{fs} = M_{fw} - M_{fc}$$

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Therefore, the compression reinforcement is computed as:

$$A'_{s} = \frac{M_{fs}}{\left(\phi_{s}f'_{c} - \phi_{c}\alpha_{1}f'_{c}\right)\left(d - d'\right)}, \text{ where}$$
$$f'_{s} = \varepsilon_{c}E_{s}\left[\frac{c - d'}{c}\right] \le f_{y} \tag{CSA 10.1.2, 10.1.3}$$

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{fc}}{f_y \left(d - \frac{a_b}{2}\right)\phi_s}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_{fs}}{f_y \left(d - d' \right) \phi_s}$$

The total tension reinforcement is $A_s = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

9.5.1.3 Minimum and Maximum Reinforcement

The minimum flexural tensile reinforcement required for each direction of a slab is given by the following limit (CSA 13.10.1):

 $A_s \ge 0.002 \ bh \tag{CSA 7.8.1}$

• In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

9.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V_f.
- Determine the shear force, *V_c*, that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three subsections describe in detail the algorithms associated with these steps.

9.5.2.1 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_c , is calculated as:

$$V_c = \phi_c \lambda \beta \sqrt{f'_c b_w d_v}$$
(CSA 11.3.4)

$$\sqrt{f_c'} \le 8 \text{ MPa}$$
 (CSA 11.3.4)

- ϕ_c is the resistance factor for concrete. By default it is taken as 0.65 (CSA 8.4.2).
- λ is the strength reduction factor to account for low density concrete (CSA 2.2). For normal density concrete, its value is 1 (CSA 8.6.5), which is taken by the program as the default value. For concrete using lower density aggregate, the user can change the value of λ in the material property data. The recommended value for λ is as follows (CSA 8.6.5):
 - 1.00, for normal density concrete,
 - 0.85, for semi-low-density concrete

$$\lambda = \begin{cases} \text{ in which all of the fine aggregate is natural sand,} \\ 0.75, \text{ for semi-low-density concrete} \end{cases}$$
 (CSA 8.6.5)

- in which none of the fine aggregate is natural sand.
- β is the factor for accounting for the shear resistance of cracked concrete

(CSA 2.2). Its value is normally between 0.1 and 0.4. It is determined according to CSA 11.3.6, and described further in the following sections.

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- b_w is the effective web width. For uniform thickness slab, it is the width of the slab. For flanged-shaped slab, it is the width of the web of the slab.
- d_{ν} is the effective shear depth. It is taken as the greater of 0.9*d* or 0.72*h*(CSA 2.3), where *d* is the distance from the extreme compression fiber to the centroid of the tension reinforcement, and *h* is the overall depth of the cross-section in the direction of the shear force (CSA 2.3).

The value of β is preferably taken as the special value (CSA 11.3.6.2) or it is determined using the simplified method (CSA 11.3.6.3), if applicable. When the conditions of the special value or simplified method do not apply, the general method is used (CSA 11.3.6.4).

If the overall slab depth, *h*, is less than 250 mm or if the depth of a flanged below the slab is not greater than one-half of the width of the web or 350 mm, β is taken as 0.21 (CSA 11.3.6.2).

When the specified yield strength of the longitudinal reinforcing f_y does not exceed 400 MPa, the specified concrete strength f'_c does not exceed 60 MPa, and the tensile force is negligible, β is determined in accordance with the simplified method, as follows (CSA 11.3.6.3):

• When the section contains at least the minimum transverse reinforcement, β is taken as 0.18 (CSA 11.6.3.3a).

$$\beta = 0.18$$
 (CSA 11.3.6.3(a))

 When the section contains no transverse reinforcement, β is determined based on the specified maximum nominal size of coarse aggregate, a_g.

For a maximum size of coarse aggregate not less than 20 mm, β is taken as:

$$\beta = \frac{230}{1000 + d_v} \tag{CSA 11.3.6.3(b)}$$

where d_v is the effective shear depth expressed in millimeters.

For a maximum size of coarse aggregate less than 20 mm, β is taken as:

$$\beta = \frac{230}{1000 + s_{ze}} \tag{CSA 11.3.6.3 c}$$

ſ

where,
$$s_{ze} = \frac{35s_z}{15 + a_g} \ge 0.85s_z$$
 (CSA 11.3.6.3.c)

In the preceding expression, the crack spacing parameter, s_{ze} , shall be taken as the minimum of d_v and the maximum distance between layers of distributed longitudinal reinforcement. However, s_{ze} is conservatively taken as equal to d_v .

In summary, for simplified cases, β can be expressed as follows:

$$\beta = \begin{cases} 0.18, & \text{if minimum transverse reinforcement is provided,} \\ \frac{230}{1000 + d_v}, & \text{if no transverse reinforcement is provided, and } a_g \ge 20\text{mm,} \\ \frac{230}{1000 + S_{ze}}, & \text{if no transverse reinforcement is provided, and } a_g < 20\text{mm.} \end{cases}$$

• When the specified yield strength of the longitudinal reinforcing f_y is greater than 400 MPa, the specified concrete strength f'_c is greater than 60 MPa, or tension is not negligible, β is determined in accordance with the general method as follows (CSA 11.3.6.1, 11.3.6.4):

$$\beta = \frac{0.40}{(1+1500\varepsilon_x)} \bullet \frac{1300}{(1000+S_{ze})}$$
(CSA 11.3.6.4)

In the preceding expression, the equivalent crack spacing parameter, s_{ze} is taken equal to 300 mm if minimum transverse reinforcement is provided (CSA 11.3.6.4). Otherwise it is determined as stated in the simplified method.

$$S_{ze} = \begin{cases} 300 & \text{if minimum transverse reinforcement is provided,} \\ \frac{35}{15 + a_g} S_z \ge 0.85S_z & \text{otherwise.} \end{cases}$$
(CSA 11.3.6.3, 11.3.6.4)

The value of a_g in the preceding equations is taken as the maximum aggregate size for f'_c of 60 MPa, is taken as zero for f'_c of 70 MPa, and linearly interpolated between these values (CSA 11.3.6.4).

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The longitudinal strain, ε_x at mid-depth of the cross-section is computed from the following equation:

$$\varepsilon_{x} = \frac{M_{f}/d_{v} + V_{f} + 0.5N_{f}}{2(E_{s}A_{s})}$$
(CSA 11.3.6.4)

In evaluating ε_x the following conditions apply:

• ε_x is positive for tensile action.

•	V_f and M_f are taken as positive quantities.	(CSA 11.3.6.4(a))
•	M_f is taken as a minimum of $V_f d_v$.	(CSA 11.3.6.4(a))

• N_f is taken as positive for tension. (CSA 2.3)

 A_s is taken as the total area of longitudinal reinforcement in the slab. It is taken as the envelope of the reinforcement required for all design load combinations. The actual provided reinforcement might be slightly higher than this quantity. The reinforcement should be developed to achieve full strength (CSA 11.3.6.3(b)).

If the value of ε_x is negative, it is recalculated with the following equation, in which A_{ct} is the area of concrete in the flexural tensile side of the slab, taken as half of the total area.

$$\varepsilon_{x} = \frac{M_{f}/d_{v} + V_{f} + 0.5N_{f}}{2(E_{s}A_{s} + E_{c}A_{ct})}$$
(CSA 11.3.6.4(c))

$$E_s = 200,000 \,\mathrm{MPa}$$
 (CSA 8.5.4.1)

$$E_c = 4500\sqrt{f_c}$$
 MPa (CSA 8.6.2.3)

If the axial tension is large enough to induce tensile stress in the section, the value of ε_x is doubled (CSA 11.3.6.4(e)).

For sections closer than d_v from the face of the support, ε_x is calculated based on M_f and V_f at a section at a distance d_v from the face of the support (CSA 11.3.6.4(d)). This condition currently is not checked by ETABS.

An upper limit on ε_x is imposed as:

$$\varepsilon_x \le 0.003$$
 (CSA 11.3.6.4(f))

In both the simplified and general methods, the shear strength of the section due to concrete, v_c depends on whether the minimum transverse reinforcement is provided. To check this condition, the program performs the design in two passes. In the first pass, it assumes that no transverse shear reinforcement is needed. When the program determines that shear reinforcement is required, the program performs the second pass assuming that at least minimum shear reinforcement is provided.

9.5.2.2 Determine Required Shear Reinforcement

The shear force is limited to $V_{r,\max}$ where:

$$V_{r,\max} = 0.25\phi_c f'_c b_w d$$
 (CSA 11.3.3)

Given V_f , V_c , and $V_{r,\max}$, the required shear reinforcement is calculated as follows:

• If $V_f \le V_c$, $\frac{A_v}{s} = 0$ (CSA 11.3.5.1) • If $V_c < V_f \le V_{r \max}$,

$$\frac{A_{v}}{s} = \frac{\left(V_{f} - V_{c}\right)\tan\theta}{\phi_{s}f_{vt}d_{v}}$$
(CSA 11.3.3, 11.3.5.1)

• If $V_f > V_{r,max}$, a failure condition is declared. (CSA 11.3.3)

A minimum area of shear reinforcement is provided in the following regions (CSA 11.2.8.1):

- (a) in regions of flexural members where the factored shear force V_f exceeds V_c
- (b) in regions of slab with an overall depth greater than 750 mm.

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Where the minimum shear reinforcement is required by CSA 11.2.8.1, or by calculation, the minimum area of shear reinforcement per unit spacing is taken as:

$$\frac{A_{v}}{s} \ge 0.06 \frac{\sqrt{f'_{c}}}{f_{yt}} b_{w}$$
(CSA 11.2.8.2)

In the preceding equations, the term θ is used, where θ is the angle of inclination of the diagonal compressive stresses with respect to the longitudinal axis of the member (CSA 2.3). The θ value is normally between 22 and 44 degrees. It is determined according to CSA 11.3.6.

Similar to the β factor, which was described previously, the value of θ is preferably taken as the special value (CSA 11.3.6.2), or it is determined using the simplified method (CSA 11.3.6.3), whenever applicable. The program uses the general method when conditions for the simplified method are not satisfied (CSA 11.3.6.4).

- If the overall slab depth, h, is less than 250 mm or if the depth of the flanged slab below the slab is not greater than one-half of the width of the web or 350 mm, θ is taken as 42 degrees (CSA 11.3.6.2).
- If the specified yield strength of the longitudinal reinforcing f_y does not exceed 400 MPa, or the specified concrete strength f'_c does not exceed 60 MPa, θ is taken to be 35 degree (CSA 11.3.6.3).

$$\theta = 35^{\circ} \text{ for } P_f \le 0 \text{ or } f_y \le 400 \text{ MPa or } f'_c \le 60 \text{ MPa}$$
 (CSA11.3.6.3)

• If the axial force is tensile, the specified yield strength of the longitudinal reinforcing $f_y > 400$ MPa, and the specified concrete strength $f'_c > 60$ MPa, θ is determined using the general method as follows (CSA 11.3.6.4),

$$\theta = 29 + 7000\varepsilon_x$$
 for $P_f < 0$, $f_v > 400$ MPa, $f'_c \le 60$ MPa (CSA11.3.6.4)

where ε_x is the longitudinal strain at the mid-depth of the cross-section for the factored load. The calculation procedure is described in preceding sections.

The maximum of all of the calculated A_v/s values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

9.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

9.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (CSA 13.3.3.1 and CSA 13.3.3.2). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (CSA 13.3.3.3). Figure 9-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 9-3 Punching Shear Perimeters

9.5.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be $\gamma_f M_u$ and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $\gamma_v M_u$, where

$$\gamma_f = \frac{1}{1 + (2/3)\sqrt{b_1/b_2}}$$
, and (CSA 13.10.2)

$$\gamma_{\nu} = 1 - \frac{1}{1 + (2/3)\sqrt{b_1/b_2}},$$
 (CSA 13.3.5.3)

where b_1 is the width of the critical section measured in the direction of the span, and b_2 is the width of the critical section measured in the direction perpendicular to the span.

9.5.3.3 Determination of Concrete Capacity

The concrete punching shear factored strength is taken as the minimum of the following three limits:

$$v_{v} = \min \begin{cases} \phi_{c} \left(1 + \frac{2}{\beta_{c}} \right) 0.19\lambda \sqrt{f'_{c}} \\ \phi_{c} \left(0.19 + \frac{\alpha_{s}d}{b_{0}} \right) \lambda \sqrt{f'_{c}} \\ \phi_{c} 0.38\lambda \sqrt{f'_{c}} \end{cases}$$
(CSA 13.3.4.1)

where, β_c is the ratio of the minimum to the maximum dimensions of the critical section, b_0 is the perimeter of the critical section, and α_s is a scale factor based on the location of the critical section.

$$\alpha_s = \begin{cases} 4, \text{ for interior columns} \\ 3, \text{ for edge colums, and} \\ 2, \text{ for corner columns.} \end{cases} (CSA 13.3.4.1(b))$$

The value of $\sqrt{f'_c}$ is limited to 8 MPa for the calculation of the concrete shear capacity (CSA 13.3.4.2).

If the effective depth, *d*, exceeds 300 mm, the value of v_c is reduced by a factor equal to 1300/(1000 + d) (CSA 13.3.4.3).

9.5.3.4 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v_{f} = \frac{V_{f}}{bod} + \frac{\gamma v_{2}[M_{f2} - V_{f}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{f3} - V_{f}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 2

$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 4

The equations for \overline{I}_{22} , \overline{I}_{33} , and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 2-axis or parallel to the 3-axis. Refer to Figures 9-4.

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$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for side of critical section parallel to 2-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2$$
, for side of critical section
parallel to 3-axis Eq. 5b

$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - x_3)^2$$
, for side of critical section
parallel to 2-axis Eq. 6a

$$\overline{I}_{33} = Ld(x_2 - x_3)^2$$
, for side of critical section parallel to 3-axis Eq. 6b

$$\overline{I}_{23} = Ld(x_2 - x_3)(y_2 - y_3)$$
, for side of critical section parallel
to 2-axis or 3-axis Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

where,

- b_0 = Perimeter of the critical section for punching shear
- d = Effective depth at the critical section for punching shear based on the average of d for 2 direction and d for 3 direction
- I_{22} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 2-axis
- I_{33} = Moment of inertia of the critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of inertia of the critical section for punching shear with respect to the 2 and 3 planes
- *L* = Length of the side of the critical section for punching shear currently being considered
- M_{f2} = Moment about the line parallel to the 2-axis at the center of the column (positive in accordance with the right-hand rule)
- M_{f3} = Moment about the line parallel to the 3-axis at the center of the column (positive in accordance with the right-hand rule)
- V_f = Punching shear stress
- V_f = Shear at the center of the column (positive upward)
- x_1, y_1 = Coordinates of the column centroid
- x_2, y_2 = Coordinates of the center of one side of the critical section for punching shear
- x_3 , y_3 = Coordinates of the centroid of the critical section for punching shear

 x_4 , y_4 = Coordinates of the location where stress is being calculated

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- γ_{V2} = Percent of M_{f2} resisted by shear
- γ_{V3} = Percent of M_{f3} resisted by shear

9.5.3.5 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

9.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm (CSA 13.2.1). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed, and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is performed as explained in the subsections that follow.

9.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is taken as:

$$v_c = 0.28\lambda \phi_c \sqrt{f'_c}$$
 for shear studs (CSA 13.3.8.3)

$$v_c = 0.19\lambda \phi_c \sqrt{f'_c}$$
 for shear stirrups (CSA 13.3.9.3)

9.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of $v_{r \max}$, where

$$v_{r,\text{max}} = 0.75 \lambda \phi_c \sqrt{f'_c}$$
 for shear studs (CSA 13.3.8.2)

$$v_{r,\text{max}} = 0.55\lambda \phi_c \sqrt{f'_c}$$
 for shear stirrups (CSA 13.3.9.2)

Given v_f , v_c , and $v_{f,max}$, the required shear reinforcement is calculated as follows, where, ϕ_s , is the strength reduction factor.

• If $v_f > v_{r, \max}$,

$$\frac{A_v}{s} = \frac{\left(v_f - v_c\right)}{\phi_s f_{yv}} b_o$$
(CSA 13.3.8.5, 13.3.9.4)

- If $v_f > v_{r,\max}$, a failure condition is declared. (CSA 13.3.8.2)
- If v_f exceeds the maximum permitted value of v_{rmax}, the concrete section should be increased in size.

9.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 9-5 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 9-5 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed

0.4d for shear studs	(CSA 13.3.8.6)
0.25d for shear stirrups	(CSA 13.3.8.6)

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

9.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in CSA 7.9 plus half of the diameter of the flexural reinforcement.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.4*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$$s_{o} \leq 0.4d$$
(CSA 13.3.8.6)
$$s \leq \begin{cases} 0.75d \quad v_{f} \leq 0.56\lambda\phi_{c}\sqrt{f'_{c}} \\ 0.50d \quad v_{f} > 0.56\lambda\phi_{c}\sqrt{f'_{c}} \end{cases}$$
(CSA 13.3.8.6)

For shear stirrups,

$$s_o \le 0.25d$$
 (CSA 13.3.9.5)
 $s \le 0.25d$ (CSA 13.3.9.5)

The minimum depth for reinforcement should be limited to 300 mm (CSA 13.3.9.1).

Chapter 10 Design for Eurocode 2-2004

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the European code Eurocode 2-2004 [EN 1992-1-1:2004] is selected. For the load combinations, reference is also made to Eurocode 0 [EN 1990], which is identified with the prefix "EC0." Various notations used in this chapter are listed in Table 10-1. For referencing to the pertinent sections of the Eurocode in this chapter, a prefix "EC2" followed by the section number is used. It also should be noted that this section describes the implementation of the CEN Default version of Eurocode 2-2004, without a country specific National Annex. Where Nationally Determined Parameters [NDPs] are to be considered, this is highlighted in the respective section by the notation [*NDP*].

The design is based on user-specified loading combinations. However, the program provides a set of default load combinations that should satisfy requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

10.1 Notations

Table 10-1	List of Symbols Used in the Eurocode 2-2004
A_c	Area of concrete section, mm ²
A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²
A_{sl}	Area of longitudinal reinforcement for torsion, mm ²
A_{sw}	Total cross-sectional area of links at the neutral axis, mm ²
A_{sw}/s_v	Area of shear reinforcement per unit length, mm ² /mm
A_t/s	Area of transverse reinforcement per unit length for torsion, mm ² /mm
a	Depth of compression block, mm
b	Width or effective width of the section in the compression zone, mm
b_f	Width or effective width of flange, mm
b_w	Average web width of a flanged slab section, mm
d	Effective depth of tension reinforcement, mm
ď	Effective depth of compression reinforcement, mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement
f_{cd}	Design concrete strength = $\alpha_{cc} f_{ck} / \gamma_c$, MPa
f_{ck}	Characteristic compressive concrete cylinder strength at 28 days, MPa
f_{ctm}	Mean value of concrete axial tensile strength, MPa
f_{cwd}	Design concrete compressive strength for shear design = α_{cc}
	f_{cwk} / γ_c , MPa
f_{cwk}	Characteristic compressive cylinder strength for shear design, MPa
f'_s	Compressive stress in compression reinforcement, MPa
f_{yd}	Design yield strength of reinforcement = f_{yk}/γ_s , MPa

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Table 10	-1 List of Symbols Used in the Eurocode 2-2004
f_{yk}	Characteristic strength of shear reinforcement, MPa
f_{ywd}	Design strength of shear reinforcement = f_{ywk}/γ_s , MPa
f_{ywk}	Characteristic strength of shear reinforcement, MPa
h	Overall depth of section, mm
h_{f}	Flange thickness, mm
M_{Ed}	Design moment at a section, N-mm
т	Normalized design moment, $M/bd^2\eta f_{cd}$
$m_{ m lim}$	Limiting normalized moment capacity as a singly reinforced slab
S_{v}	Spacing of the shear reinforcement, mm
T_{Ed}	Torsion at ultimate design load, N-mm
T_{Rdc}	Torsional cracking moment, N-mm
$T_{Rd, \max}$	Design torsional resistance moment, N-mm
и	Perimeter of the punch critical section, mm
V_{Rdc}	Design shear resistance from concrete alone, N
V _{Rd,max}	Design limiting shear resistance of a cross-section, N
V_{Ed}	Shear force at ultimate design load, N
x	Depth of neutral axis, mm
$x_{\rm lim}$	Limiting depth of neutral axis, mm
Z.	Lever arm, mm
$lpha_{cc}$	Coefficient accounting for long-term effects on the concrete com- pressive strength
$lpha_{cw}$	Coefficient accounting for the state of stress in the compression chord
δ	Redistribution factor
\mathcal{E}_{c}	Concrete strain
\mathcal{E}_{S}	Strain in tension reinforcement
, Es	Strain in compression steel
\mathcal{V}_{c}	Partial safety factor for concrete strength

Table 10-1 List of Symbols Used in the Eurocode 2-2004		
γ_s	Partial safety factor for reinforcement strength	
λ	Factor defining the effective depth of the compression zone	
ν	Effectiveness factor for shear resistance without concrete crushing	
η	Concrete strength reduction factor for sustained loading and stress block	
$ ho_l$	Tension reinforcement ratio	
σ_{cp}	Axial stress in the concrete, MPa	
θ	Angle of the concrete compression strut	
ω	Normalized tension reinforcement ratio	
ω'	Normalized compression reinforcement ratio	
$\omega_{\rm lim}$	Normalized limiting tension reinforcement ratio	

10.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be checked. Eurocode 0-2002 allows load combinations to be defined based on EC0 Equation 6.10 or the less favorable of EC0 Equations 6.10a and 6.10b [*NDP*].

$$\sum_{j\geq 1} \gamma_{G,j} G_{k,j} + \gamma_P P + \gamma_{Q,1} Q_{k,1} + \sum_{i>1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}$$
(EC0 Eq. 6.10)

$$\sum_{j \ge 1} \gamma_{G,j} G_{k,j} + \gamma_P P + \gamma_{Q,1} \psi_{0,1} Q_{k,1} + \sum_{i>1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}$$
(EC0 Eq. 6.10a)

$$\sum_{j \ge 1} \xi_j \gamma_{G,j} G_{k,j} + \gamma_P P + \gamma_{Q,1} Q_{k,1} + \sum_{i>1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}$$
(EC0 Eq. 6.10b)

Load combinations considering seismic loading are automatically generated based on EC0 Equation 6.12b.

$$\sum_{j\geq 1} G_{k,j} + P + A_{Ed} + \sum_{i>1} \psi_{2,i} Q_{k,i}$$
 (EC0 Eq. 6.12b)

10 - 4 Design Load Combinations

For this code, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations need to be considered if equation 6.10 is specified for generation of the load combinations (EC0 6.4.3):

$\gamma_{Gj,sup} D$	(EC0 Eq. 6.10)
$\gamma_{Gj,sup}D+\gamma_{Q,1}L$	(EC0 Eq. 6.10)
$\gamma_{Gj,sup}D + (0.75)\gamma_{Q,1}PL$	(EC0 Eq. 6.10)
$\begin{split} \gamma_{Gj,inf} D &\pm \gamma_{Q,1} W \\ \gamma_{Gj,sup} D &\pm \gamma_{Q,1} W \end{split}$	(EC0 Eq. 6.10)
$\begin{split} &\gamma_{Gj,sup}D + \gamma_{Q,1}L \pm \gamma_{Q,i}\psi_{0,i}W \\ &\gamma_{Gj,sup}D + \gamma_{Q,1}L + \gamma_{Q,i}\psi_{0,i}S \\ &\gamma_{Gj,sup}D \pm \gamma_{Q,1}W + \gamma_{Q,i}\psi_{0,i}L \\ &\gamma_{Gj,sup}D \pm \gamma_{Q,1}W + \gamma_{Q,i}\psi_{0,i}S \\ &\gamma_{Gj,sup}D + \gamma_{Q,1}S \pm \gamma_{Q,i}\psi_{0,i}W \\ &\gamma_{Gj,sup}D + \gamma_{Q,1}S + \gamma_{Q,i}\psi_{0,i}L \end{split}$	(EC0 Eq. 6.10)
$\begin{split} \gamma_{Gj,sup} D &+ \gamma_{Q,1} L + \gamma_{Q,i} \psi_{0,i} S \pm \gamma_{Q,i} \psi_{0,i} W \\ \gamma_{Gj,sup} D &\pm \gamma_{Q,1} W + \gamma_{Q,i} \psi_{0,i} L + \gamma_{Q,i} \psi_{0,i} S \\ \gamma_{Gj,sup} D &+ \gamma_{Q,1} S \pm \gamma_{Q,i} \psi_{0,i} W + \gamma_{Q,i} \psi_{0,i} L \end{split}$	(EC0 Eq. 6.10)
$\begin{array}{l} D \pm 1.0E \\ D \pm 1.0E + \psi_{2,i}L \\ D \pm 1.0E + \psi_{2,i}L + \psi_{2,i}S \end{array}$	(EC0 Eq. 6.12b)

If the load combinations are specified to be generated from the max of EC0 Equations 6.10a and 6.10b, the following load combinations from both equations are considered in the program.

$\gamma_{Gj,sup} \mathbf{D}$	(EC0 Eq. 6.10a)
$\xi \gamma_{Gj,sup} \mathbf{D}$	(EC0 Eq. 6.10b)
$\begin{array}{l} \gamma_{Gj,sup}D+\gamma_{Q,1}\psi_{0,1}\;L\\ \xi\;\gamma_{Gj,sup}D+\gamma_{Q,1}L \end{array}$	(EC0 Eq. 6.10a) (EC0 Eq. 6.10b)

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$\begin{array}{l} \gamma_{Gj,sup} D + (0.75) \gamma_{Q,1} \psi_{0,1} PL \\ \xi \gamma_{Gj,sup} D + (0.75) \gamma_{Q,1} PL \end{array}$	(EC0 Eq. 6.10a) (EC0 Eq. 6.10b)
$\begin{split} \gamma_{Gj,inf} D &\pm \gamma_{Q,1} \psi_{0,1} W \\ \gamma_{Gj,sup} D &\pm \gamma_{Q,1} \psi_{0,1} W \\ \gamma_{Gj,inf} D &\pm \gamma_{Q,1} W \\ \xi \gamma_{Gj,sup} D &\pm \gamma_{Q,1} W \end{split}$	(EC0 Eq. 6.10a) (EC0 Eq. 6.10a) (EC0 Eq. 6.10b) (EC0 Eq. 6.10b)
$\begin{split} &\gamma_{Gj,sup}D + \gamma_{Q,1}\psi_{0,1}L \pm \gamma_{Q,i}\psi_{0,i}W \\ &\gamma_{Gj,sup}D + \gamma_{Q,1}\psi_{0,1}L + \gamma_{Q,i}\psi_{0,i}S \\ &\gamma_{Gj,sup}D \pm \gamma_{Q,1}\psi_{0,1}W + \gamma_{Q,i}\psi_{0,i}L \\ &\gamma_{Gj,sup}D \pm \gamma_{Q,1}\psi_{0,1}W + \gamma_{Q,i}\psi_{0,i}S \\ &\gamma_{Gj,sup}D + \gamma_{Q,1}\psi_{0,1}S + \gamma_{Q,i}\psi_{0,i}L \\ &\gamma_{Gj,sup}D + \gamma_{Q,1}\psi_{0,1}S \pm \gamma_{Q,i}\psi_{0,i}W \end{split}$	(EC0 Eq. 6.10a)
$ \begin{array}{l} \xi \ \gamma_{Gj,sup} \ D + \gamma_{Q,1} \ L \pm \gamma_{Q,i} \ \psi_{0,i} \ W \\ \xi \ \gamma_{Gj,sup} \ D + \gamma_{Q,1} \ L + \gamma_{Q,i} \ \psi_{0,i} \ S \\ \xi \ \gamma_{Gj,sup} \ D + \gamma_{Q,1} \ S \pm \gamma_{Q,i} \ \psi_{0,i} \ W \\ \xi \ \gamma_{Gj,sup} \ D + \gamma_{Q,1} \ S + \gamma_{Q,i} \ \psi_{0,i} \ L \\ \gamma_{Gj,inf} \ D \pm \gamma_{Q,1} \ W + \gamma_{Q,i} \ \psi_{0,i} \ S \end{array} $	(EC0 Eq. 6.10b)
$\begin{array}{l} D \pm 1.0E \\ D \pm 1.0E + \psi_{2,i} L \\ D \pm 1.0E + \psi_{2,i} L + \psi_{2,i} S \end{array}$	(EC0 Eq. 6.12b)

For both sets of load combinations, the variable values for the CEN Default version of the load combinations are defined in the list that follows [*NDP*].

γGj,sup	5 = 1.35	(EC0 Table A1.2(B))
γGj,inf	= 1.00	(EC0 Table A1.2(B))
γq,1	= 1.5	(EC0 Table A1.2(B))
γq,i	= 1.5	(EC0 Table A1.2(B))
$\psi_{0,i}$	= 0.7 (live load, assumed not to be storage)	(EC0 Table A1.1)
Ψ0,i	= 0.6 (wind load)	(EC0 Table A1.1)
Ψ0,i	= 0.5 (snow load, assumed H \leq 1,000 m)	(EC0 Table A1.1)

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ξ	= 0.85	(EC0 Table A1.2(B))
$\psi_{2,i}$	= 0.3 (live, assumed office/residential space)	(EC0 Table A1.1)
$\psi_{2,i}$	= 0 (snow, assumed H \leq 1,000 m)	(EC0 Table A1.1)

These are also the default design load combinations in ETABS whenever the Eurocode 2-2004 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

10.3 Limits on Material Strength

The concrete compressive strength, f_{ck} , should not be greater than 90 MPa (EC2 3.1.2(2)). The lower and upper limits of the reinforcement yield strength, f_{yk} , should be 400 and 600 MPa, respectively (EC2 3.2.2(3)).

ETABS enforces the upper material strength limits for flexure and shear design of slabs. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. It is the user's responsibility to ensure that the minimum strength is satisfied.

10.4 Partial Safety Factors

The design strengths for concrete and steel are obtained by dividing the characteristic strengths of the materials by the partial safety factors, γ_s and γ_c as shown here [*NDP*].

$$f_{cd} = \alpha_{cc} f_{ck} / \gamma_c \tag{EC2 3.1.6(1)}$$

$$f_{yd} = f_{yk} / \gamma_s$$
 (EC2 3.2.7(2))

$$f_{ywd} = f_{ywk} / \gamma_s$$
 (EC2 3.2.7(2))

 α_{cc} is the coefficient taking account of long term effects on the compressive strength. α_{cc} is taken as 1.0 by default and can be overwritten by the user (EC2 3.1.6(1)).

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The partial safety factors for the materials and the design strengths of concrete and reinforcement are given in the text that follows (EC2 2.4.2.4(1), Table 2.1N):

Partial safety factor for reinforcement, $\gamma_s = 1.15$

Partial safety factor for concrete, $\gamma_c = 1.5$

These values are recommended by the code to give an acceptable level of safety for normal structures under regular design situations (EC2 2.4.2.4). For accidental and earthquake situations, the recommended values are less than the tabulated values. The user should consider those separately.

These values can be overwritten; however, caution is advised.

10.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

10.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element

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boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

10.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

10.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 10-1 (EC2 3.1.7(3)). The area of the stress block and the depth of the compressive block is taken as:

$$F_c = \eta f_{cd} ab$$
 (EC2 3.1.7(3), Fig 3.5)

$$a = \lambda x$$
 (EC2 3.1.7(3), Fig 3.5)

where *x* is the depth of the neutral axis. The factor λ defining the effective height of the compression zone and the factor η defining the effective strength are given as:

$$\lambda = 0.8$$
 for $f_{ck} \le 50$ MPa (EC2 3.1.7(3))

$$\lambda = 0.8 \left(\frac{f_{ck} - 50}{400} \right) \quad \text{for } 50 < f_{ck} \le 90 \text{ MPa}$$
(EC2 3.1.7(3))

$$\eta = 1.0$$
 for $f_{ck} \le 50$ MPa (EC2 3.1.7(3))

$$\eta = 1.0 - \left(\frac{f_{ck} - 50}{200}\right)$$
 for $50 < f_{ck} \le 90$ MPa (EC2 3.1.7(3))

Furthermore, it is assumed that moment redistribution in the member does not exceed the code-specified limiting value. The code also places a limitation on the neutral axis depth, to safeguard against non-ductile failures (EC2 5.5(4)). When the applied moment exceeds the limiting moment capacity as a singly reinforced slab, the area of compression reinforcement is calculated assuming that the neutral axis depth remains at the maximum permitted value.

The limiting value of the ratio of the neutral axis depth at the ultimate limit state to the effective depth, $(x/d)_{\text{lim}}$, is expressed as a function of the ratio of the redistributed moment to the moment before redistribution, δ , as follows:

$$\left(\frac{x}{d}\right)_{\lim} = \frac{\delta - k_1}{k_2} \text{ for } f_{ck} \le 50 \text{ MPa}$$
(EC2 5.5(4))

$$\left(\frac{x}{d}\right)_{\lim} = \frac{\delta - k_3}{k_4} \text{ for } f_{ck} > 50 \text{ MPa}$$
(EC2 5.5(4))

For reinforcement with $f_{yk} \le 500$ MPa, the following values are used:

$$k_1 = 0.44 [NDP]$$
 (EC 5.5(4))

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$$k_2 = k_4 = 1.25(0.6 + 0.0014/\varepsilon_{cu2}) [NDP]$$
 (EC 5.5(4))

$$k_3 = 0.54 \ [NDP] \tag{EC 5.5(4)}$$

 δ is assumed to be 1

where the ultimate strain, ε_{cu2} [*NDP*], is determined from EC2 Table 3.1 as:

$$\mathcal{E}_{cu2} = 0.0035 \text{ for } f_{ck} < 50 \text{ MPa}$$
 (EC2 Table 3.1)

$$\varepsilon_{cu2} = 2.6 + 35 \left[\left(90 - f_{ck} \right) / 100 \right]^4 \text{ for } f_{ck} \ge 50 \text{ MPa}$$
 (EC2 Table 3.1)

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the subsections that follow.



Figure 10-1 Uniform Thickness Slab Design

10.5.1.2.1 Design of uniform thickness slab

For uniform thinness slab, the normalized moment, m, and the normalized section capacity as a singly reinforce slab, m_{lim} , are obtained first. The reinforcement area is determined based on whether m is greater than, less than, or equal to m_{lim} .

• The normalized design moment, *m*, is calculated as:

$$m = \frac{M}{bd^2 \eta f_{cd}}$$

• The normalized concrete moment capacity as a singly reinforced slab, *m*_{lim}, is calculated as:

$$m_{\rm lim} = \lambda \left(\frac{x}{d}\right)_{\rm lim} \left[1 - \frac{\lambda}{2} \left(\frac{x}{d}\right)_{\rm lim}\right]$$

• If $m \le m_{\text{lim}}$, a singly reinforced slab is designed. The normalized reinforcement ratio is calculated as:

$$\omega = 1 - \sqrt{1 - 2m}$$

The area of tension reinforcement, A_s , is then given by:

$$A_{s} = \omega \left(\frac{\eta f_{cd} b d}{f_{yd}} \right)$$

This reinforcement is to be placed at the bottom if M_{Ed} is positive, or at the top if M_{Ed} is negative.

If m > m_{lim}, both tension and compression reinforcement is designed as follows:

The normalized steel ratios ω' , ω_{lim} , and ω are calculated as:

$$\omega_{\rm lim} = \lambda \left(\frac{x}{d}\right)_{\rm lim} = 1 - \sqrt{1 - 2m_{\rm lim}}$$

$$\omega' = \frac{m - m_{\lim}}{1 - d'/d}$$

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 $\omega = \omega_{\rm lim} + \omega'$

where, d' is the depth to the compression reinforcement from the concrete compression face.

The area of compression and tension reinforcement, A'_s and A_s , are given by:

$$A'_{s} = \omega' \left[\frac{\eta f_{cd} b d}{f'_{s} - \eta f_{cd}} \right]$$
$$A_{s} = \omega \left[\frac{\eta f_{cd} b d}{f_{yd}} \right]$$

where, f'_s is the stress in the compression reinforcement, and is given by:

$$f'_{s} = E_{s}\varepsilon_{cu3}\left[1 - \frac{d'}{x_{\lim}}\right] \le f_{yd}$$
 (EC2 6.1, 3.2.7(4), Fig 3.8)

10.5.1.2.2 Design of nonuniform thickness slab

10.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_{Ed} (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

10.5.1.2.2.2 Flanged Slab Section Under Positive Moment

With the flange in compression, the program analyzes the section by considering alternative locations of the neutral axis. Initially, the neutral axis is assumed to be located within the flange. Based on this assumption, the program calculates the depth of the neutral axis. If the stress block does not extend beyond the flange thickness, the section is designed as a uniform thickness slab of width b_f . If the stress block extends beyond the flange, additional calculation is required. See Figure 10-2.

• The normalized design moment, *m*, is calculated as:

$$m = \frac{M}{bd^2 \eta f_{cd}}$$
(EC2 6.1, 3.1.7(3))

• The limiting values are calculated as:

$$m_{\rm lim} = \lambda \left(\frac{x}{d}\right)_{\rm lim} \left[1 - \frac{\lambda}{2} \left(\frac{x}{d}\right)_{\rm lim}\right]$$
(EC2 5.5(4), 3.1.7(3))
$$\omega_{\rm lim} = \lambda \left(\frac{x}{d}\right)_{\rm lim}$$

$$a_{\rm max} = \omega_{\rm lim} d$$

• The values ω and *a* are calculated as:

$$\omega = 1 - \sqrt{1 - 2m}$$

$$a = \omega d$$



Figure 10-2 Nonuniform Thickness Slab Design

• If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in that case, the width of the slab is taken as b_f . Compression reinforcement is required when $m > m_{\text{lim}}$.

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If a > h_f, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, and the second part is for balancing the compressive force from the web, as shown in Figure 10-2. The reinforcement area required for balancing the flange compression, A_{s2} is given as:

$$A_{s2} = \frac{\left(b_f - b_w\right)h_f\eta f_{cd}}{f_{yd}}$$

and the corresponding resistive moment is given by

$$M_2 = A_{s2} f_{yd} \left(d - \frac{h_f}{2} \right)$$

The reinforcement required for balancing the compressive force from the web, considering a rectangular section of width b_w to resist the moment, $M_1 = M - M_2$, is determined as follows:

$$m_1 = \frac{M_1}{b_w d^2 \eta f_{cd}}$$

• If $m_1 \leq m_{\lim}$,

$$\omega_{1} = 1 - \sqrt{1 - 2m_{1}}$$
$$A_{s1} = \omega_{1} \left[\frac{\eta f_{cd} b_{w} d}{f_{yd}} \right]$$

• If $m_1 > m_{\lim}$,

$$\omega' = \frac{m_{\rm lim} - m_{\rm lim}}{1 - d'/d}$$
$$\omega_{\rm lim} = \lambda \left(\frac{x}{d}\right)_{\rm lim}$$

 $\omega_{\rm l} = \omega_{\rm lim} + \omega'$

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$$A'_{s} = \omega' \left[\frac{\eta f_{cd} b d}{f'_{s} - \eta f_{cd}} \right]$$
$$A_{s1} = \omega_{1} \left[\frac{\eta f_{cd} b_{w} d}{f_{yd}} \right]$$

where, f'_s is given by:

$$f'_{s} = E_{s}\varepsilon_{cu3}\left[1 - \frac{d'}{x_{\lim}}\right] \le f_{yd}$$
 (EC2 6.1, 3.2.7(4), Fig 3.8)

The total tension reinforcement is $A_s = A_{s1} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

10.5.1.3 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (EC2 9.3.1.1) [*NDP*]:

$$A_{s,\min} = 0.26 \frac{f_{ctm}}{f_{yk}} bd$$
(EC2 9.2.1.1(1))

$$A_{s,\min} = 0.0013bd \tag{EC2 9.2.1.1(1)}$$

where f_{ctm} is the mean value of axial tensile strength of the concrete and is computed as:

$$f_{ctm} = 0.30 f_{ck}^{(2/3)} \text{ for } f_{ck} \le 50 \text{ MPa}$$
(EC2 Table 3.1)
$$f_{ctm} = 2.12 ln (1 + f_{cm} / 10) \text{ for } f_{ck} > 50 \text{ MPa}$$
(EC2 Table 3.1)

$$f_{cm} = f_{ck} + 8 \text{ MPa}$$
(EC2 Table 3.1)

The minimum flexural tension reinforcement required for control of cracking should be investigated independently by the user.

An upper limit on the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (EC 9.2.1.1(3)).

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10.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved (EC2 6.2):

- Determine the factored shear force, *V*_{Ed}.
- Determine the shear force, $V_{Rd,c}$, that can be resisted by the concrete.
- Determine the shear reinforcement required.

The following three sections describe in detail the algorithms associated with these steps.

10.5.2.1 Determine Factored Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

10.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, $V_{Rd,c}$, is calculated as:

$$V_{Rd,c} = \left[C_{Rd,c} k \left(100 \rho_1 f_{ck} \right)^{1/3} + k_1 \sigma_{cp} \right] b_w d \qquad (\text{EC2 6.2.2(1)})$$

with a minimum of:

$$V_{Rd,c} = (v_{\min} + k_1 \sigma_{cp}) b_w d$$
 (EC2 6.2.2(1))

where

 f_{ck} is in MPa

$$k = 1 + \sqrt{\frac{200}{d}} \le 2.0$$
 with *d* in mm (EC2 6.2.2(1))

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$$\rho_{l} = \text{tension reinforcement ratio} = \frac{A_{s1}}{b_{w}d} \le 0.02 \qquad (\text{EC2 6.2.2(1)})$$

$$A_{sl} = \text{area of tension reinforcement} \qquad (\text{EC2 6.2.2(1)})$$

$$\sigma_{cp} = N_{Ed} / A_{c} < 0.2 f_{cd} \text{ MPa} \qquad (\text{EC2 6.2.2(1)})$$

The value of $C_{Rd,c}$, v_{min} and k_l for use in a country may be found in its National Annex. The program default values for $C_{Rd,c}$ [*NDP*], v_{min} [*NDP*], and k_l [*NDP*] are given as follows (EC2 6.2.2(1)):

$$C_{Rd,c} = 0.18/\gamma_c$$
 (EC2 6.2.2(1))

$$v_{\min} = 0.035 \, k^{3/2} \, f_{ck}^{1/2} \tag{EC2 6.2.2(1)}$$

$$k_l = 0.15.$$
 (EC2 6.2.2(1))

For light-weight concrete:

$$C_{Rd,c} = 0.18 / \gamma_c$$

$$v_{\min} = 0.03 k^{3/2} f_{ck}^{1/2}$$
(EC2 11.6.1(1))
(EC2 11.6.1(1))

$$k_1 = 0.15.$$
 (EC2 11.6.1(1))

10.5.2.3 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{Rd,\max} = \frac{\alpha_{cw} b_w z v_1 f_{cd}}{\cot \theta + \tan \theta}, \text{ where} \qquad (EC2\ 6.2.3(3))$$

$$\alpha_{cw}$$
 [*NDP*] is conservatively taken as 1. (EC2 6.2.3(3))

The strength reduction factor for concrete cracked in shear, v_1 [*NDP*], is defined as:

$$v_1 = 0.6 \left(1 - \frac{f_{ck}}{250} \right) \tag{EC2 6.2.2(6)}$$

$$z = 0.9d$$
 (EC2 6.2.3(1))

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 θ is optimized by the program and is set to 45° for combinations including seismic loading (EC2 6.2.3(2)).

Given V_{Ed} , V_{Rdc} , and $V_{Rd,max}$, the required shear reinforcement is calculated as follows:

• If $V_{Ed} \leq V_{Rdc}$,

$$\frac{A_{sw}}{s_v} = \frac{A_{sw,\min}}{s}$$

• If $V_{R,dc} < V_{Ed} \le V_{Rd,max}$

$$\frac{A_{sw}}{s} = \frac{V_{Ed}}{zf_{vwd} \cot \theta} \ge \frac{A_{sw,\min}}{s}$$
(EC2 6.2.3(3))

• If $V_{Ed} > V_{Rd,max}$, a failure condition is declared. (EC2 6.2.3(3))

The minimum shear reinforcement is defined as:

$$\frac{A_{sw,\min}}{s} = \frac{0.08\sqrt{f_{ck}}}{f_{yk}}b_w$$
(EC2 9.2.2(5))

The maximum of all of the calculated A_{sw}/s_v values obtained from each load combination is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

10.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the *Key Features and Terminology* manual. Only the code-specific items are described in the following subsections.

10.5.3.1 Critical Section for Punching Shear

The punching shear is checked at the face of the column (EC2 6.4.1(4)) and at a critical section at a distance of 2.0d from the face of the support (EC2 6.4.2(1)). The perimeter of the critical section should be constructed such that its length is minimized. Figure 10-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 10-3 Punching Shear Perimeters

10.5.3.2 Determination of Concrete Capacity

The concrete punching shear stress capacity is taken as:

$$V_{Rd,c} = \left[C_{Rd,c} k \left(100 \rho_1 f_{ck} \right)^{1/3} + k_1 \sigma_{cp} \right]$$
(EC2 6.4.4(1))

with a minimum of:

$$V_{Rd,c} = \left(v_{\min} + k_1 \sigma_{cp} \right)$$
 (EC2 6.4.4(1))

where f_{ck} is in MPa and

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$$k = 1 + \sqrt{\frac{200}{d}} \le 2.0 \text{ with } d \text{ in mm}$$
(EC2 6.4.4(1))
$$\rho_{1} = \sqrt{\rho_{1x}\rho_{1y}} \le 0.02$$
(EC2 6.4.4(1))

where ρ_{1x} and ρ_{1y} are the reinforcement ratios in the *x* and *y* directions respectively, which is taken as the average tension reinforcement ratios of design strips in Layer A and layer B where Layer A and Layer design strips are in orthogonal directions. When design strips are not present in both orthogonal directions then tension reinforcement ratio is taken as zero in the current implementation, and

$$\sigma_{cp} = (\sigma_{cx} + \sigma_{cy})/2$$
 (EC2 6.4.4(1))

where σ_{cx} and σ_{cy} are the normal concrete stresses in the critical section in the *x* and *y* directions respectively, conservatively taken as zeros.

$$C_{Rd,c} = 0.18 / \gamma_c [NDP]$$
 (EC2 6.4.4(1))

$$v_{\min} = 0.035k^{3/2} f_{ck}^{1/2} [NDP]$$
 (EC2 6.4.4(1))

$$k_l = 0.15 \ [NDP].$$
 (EC2 6.4.4(1))

10.5.3.3 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear, the nominal design shear stress, v_{Ed} , is calculated as:

$$v_{Ed} = \frac{V_{Ed}}{ud} \left[1 + k \frac{M_{Ed,2}u_1}{V_{Ed}W_{1,2}} + k \frac{M_{Ed,3}u_1}{V_{Ed}W_{1,3}} \right], \text{ where } (EC2 \ 6.4.4(2))$$

- *k* is the function of the aspect ratio of the loaded area in Table 6.1 of EN 1992-1-1
- u_1 is the effective perimeter of the critical section
- *d* is the mean effective depth of the slab
- M_{Ed} is the design moment transmitted from the slab to the column at the connection along bending axis 2 and 3

- V_{Ed} is the total punching shear force
- W_1 accounts for the distribution of shear based on the control perimeter along bending axis 2 and 3.

10.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

10.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is performed as described in the subsections that follow.

10.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

10.5.4.2 Determine Required Shear Reinforcement

The shear is limited to a maximum of $V_{Rd,max}$ calculated in the same manner as explained previously for slabs.

Given v_{Ed} , $v_{Rd,c}$, and $v_{Rd,max}$, the required shear reinforcement is calculated as follows (EC2 6.4.5).

• If $v_{R,dc} < v_{Ed} \le v_{Rd,\max}$

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$$A_{sw} = \frac{\left(v_{Ed} - 0.75v_{Rd,c}\right)}{1.5f_{ywd,ef}} \left(u_1d\right)s_r$$
(EC2 6.4.5)

- If $v_{Ed} > v_{Rd,\max}$, a failure condition is declared. (EC2 6.2.3(3))
- If v_{Ed} exceeds the maximum permitted value of V_{Rd,max}, the concrete section should be increased in size.

10.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 10-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 10-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed 2*d*. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 1.5d measured in a direction parallel to the column face (EC2 9.4.3(1)).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of

shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

10.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in EC2 4.4.1 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 10-, 12-, 14-, 110-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.3*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 1.5*d* and should not exceed 2*d* at additional perimeters. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$0.3d \le s_o \le 2d$	(EC2 9.4.3(1))
$s \leq 0.75d$	(EC2 9.4.3(1))
$g \leq 1.5d$ (first perimeter)	(EC2 9.4.3(1))
$g \leq 2d$ (additional perimeters)	(EC2 9.4.3(1))

10.6 Nationally Determined Parameters (NDPs)

The Comité Européen de Normalisation (CEN) version of Eurocode 2-2004 specifies a set of clauses in the design code, for which Nationally Determined Parameters [NDPs] are permitted to be adjusted by each member country within their National Annex. Variations in these parameters between countries are considered in the program by choosing the desired country from the **Options menu** > **Preferences** > **Concrete Frame Design** command. This appendix lists the NDPs as adopted in the program for the CEN Default version of the design code. Additional tables are provided that list the NDPs that differ from the CEN Default values for each country supported in the program.

10 - 24 Nationally Determined Parameters (NDPs)

NDP	Clause	Value
γο	2.4.2.4(1)	1.5
γs	2.4.2.4(1)	1.15
άς	3.1.6(1)	1.0
α_{ct}	3.1.6(2)	1.0
$\max f_{yk}$	3.2.2(3)	600MPa
Load Combinations	5.1.3(1)	Combinations from Eq. 6.10
θ_0	5.2(5)	0.005
k1	5.5(4)	0.44
k2	5.5(4)	$1.25(0.6 + 0.0014/\varepsilon_{cu2})$
k3	5.5(4)	0.54
<i>k</i> 4	5.5(4)	$1.25(0.6 + 0.0014/\varepsilon_{cu2})$
$\lambda_{ m lim}$	5.8.3.1(1)	$20 \cdot A \cdot B \cdot C / \sqrt{n}$
$C_{Rd,c}$	6.2.2(1)	0.18/ <i>7c</i>
Vmin	6.2.2(1)	$0.035k^{3/2}f_{\epsilon k}{}^{1/2}$
k1	6.2.2(1)	0.15
θ	6.2.3(2)	45 degrees
VI	6.2.3(3)	$0.6 \left[1 - \frac{f_{ck}}{250} \right]$
$lpha_{\scriptscriptstyle CW}$	6.2.3(3)	1.0

Table 10-2 CEN Default NDPs

Nationally Determined Parameters (NDPs) 10 - 25

NDP	Clause	Value
Beam A _{s,min}	9.2.1.1(1)	$0.26 \frac{f_{ctm}}{f_{yk}} b_t d \ge 0.0013 b_t d$
Beam A _{s,max}	9.2.1.1(3)	0.04Ac
Beam $\rho_{w,\min}$	9.2.2(5)	$\left(0.08\sqrt{f_{ck}} ight)/f_{yk}$
Cl cc	11.3.5(1)	0.85
<i>Clic</i> t	11.3.5(2)	0.85
$C_{IRd,c}$	11.6.1(1)	$0.15/\gamma_c$
VI,min	11.6.1(1)	$0.30k^{3/2} f_{lck}^{1/2}$
k ₁	11.6.1(1)	0.15
ν1	11.6.2(1)	$0.5 \eta_1(1 - f_{lck}/250)$

Table 10-2 CEN Default NDPs

Table 10-3 Denmark NDPs

NDP	Clause	Value
γς	2.4.2.4(1)	1.45
γs	2.4.2.4(1)	1.20
$\operatorname{Max} f_{yk}$	3.2.2(3)	650MPa
Load Combinations	5.1.3(1)	Combinations from Eq. 6.10a/b
$\lambda_{ m lim}$	5.8.3.1(1)	$20 \cdot \sqrt{rac{A_c f_{cd}}{N_{Ed}}}$

10 - 26 Nationally Determined Parameters (NDPs)

NDP	Clause	Value
Beam $\rho_{w,\min}$	9.2.2(5)	$\left(0.063\sqrt{f_{ck}}\right)/f_{yk}$
$lpha_{lcc}$	11.3.5(1)	1.0
$lpha_{lct}$	11.3.5(2)	1.0
Vl,min	11.6.1(1)	$0.03k^{2/3}f_{lck}^{1/2}$

Table 10-3 Denmark NDPs

Table 10-4 Finland NDPs

NDP	Clause	Value
άζες	3.1.6(1)	0.85
$\operatorname{Max} f_{yk}$	3.2.2(3)	700MPa
Load Combinations	5.1.3(1)	Combinations from Eq. 6.10a/b
k2	5.5(4)	1.10
Beam A _{s,max}	9.2.1.1(3)	Unlimited

Table 10-5 Norway NDPs

NDP	Clause	Value
α_{cc}	3.1.6(1)	0.85
α_{ct}	3.1.6(2)	0.85
$\lambda_{ m lim}$	5.8.3.1(1)	$13(2-r_m)A_f$

Nationally Determined Parameters (NDPs) 10 - 27

NDP	Clause	Value
k_1	6.2.2(1)	0.15 for compression 0.3 for tension
$v_{ m min}$	6.2.2(1)	$0.035k^{3/2}f_{ck}^{1/2}$
Beam $\rho_{w,\min}$	9.2.2(5)	$\left(0.1\sqrt{f_{ck}}\right)/f_{yk}$
Vl,min	11.6.1(1)	$0.03k^{2/3}f_{lck}^{1/2}$
k_1	11.6.1(1)	0.15 for compression 0.3 for tension
V1	11.6.2(1)	$0.5(1 - f_{lck}/250)$

Table 10-5 Norway NDPs

Table 10-6 Singapore NDPs

NDP	Clause	Value
α _{cc}	3.1.6(1)	0.85
k_1	5.5(4)	0.4
k ₂	5.5(4)	$0.6 + 0.0014/\varepsilon_{cu2}$
k3	5.5(4)	0.54
<i>k</i> 4	5.5(4)	$0.6 + 0.0014/\varepsilon_{cu2}$
Vlim	5.8.3.1(1)	$0.30k^{3/2}f_{lck}^{1/2}$

Table 10-7 Slovenia NDPs

10 - 28 Nationally Determined Parameters (NDPs)

NDP	Clause	Value
Same As CEN Default		

Table 10-8 Sweden NDPs

NDP	Clause	Value
Beam A _{s,max}	9.2.1.1(3)	Unlimited
Ølcc	11.3.5(1)	1.0
Ωlct	11.3.5(2)	1.0

Table 10-9 United Kingdom NDPs

NDP	Clause	Value
$\psi_{0,i}$ (wind load)	EC0 Combos	0.5
α _{cc}	3.1.6(1)	0.85
k_1	5.5(4)	0.4
k2	5.5(4)	$0.6 + 0.0014/\varepsilon_{cu2}$
<i>k</i> 3	5.5(4)	0.4
<i>k</i> 4	5.5(4)	$0.6 + 0.0014/\epsilon_{cu2}$
Vl,min	11.6.1(1)	$0.30k^{3/2}f_{lck}^{1/2}$

Chapter 11 Design for Hong Kong CP-2013

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Hong Kong limit state code CP-2013 [CP 2013] is selected. The various notations used in this chapter are listed in Table 11-1. For referencing to the pertinent sections of the Hong Kong code in this chapter, a prefix "CP" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

11.1 Notations

Table 11-1 List of Symbols Used in the CP-2013 Code

- A_g Gross area of cross-section, mm²
- A_l Area of longitudinal reinforcement for torsion, mm²
- A_s Area of tension reinforcement, mm²

A_{s}	Area of compression reinforcement, mm ²
A_{sv}	Total cross-sectional area of links at the neutral axis, mm ²
$A_{sv,t}$	Total cross-sectional area of closed links for torsion, mm ²
A_{sv}/s_v	Area of shear reinforcement per unit length, mm ² /mm
а	Depth of compression block, mm
b	Width or effective width of the section in the compression zone, mm
b_{f}	Width or effective width of flange, mm
b_w	Average web width of a flanged shaped section, mm
С	Torsional constant, mm ⁴
d	Effective depth of tension reinforcement, mm
d'	Depth to center of compression reinforcement, mm
E_c	Modulus of elasticity of concrete, N/mm ²
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 N/m
f	Punching shear factor considering column location
fcu	Characteristic cube strength, N/mm ²
f'_s	Stress in the compression reinforcement, N/mm ²
f_y	Characteristic strength of reinforcement, N/mm ²
f_{yv}	Characteristic strength of shear reinforcement, N/mm ²
h	Overall depth of a section in the plane of bending, mm
h_{f}	Flange thickness, mm
$h_{ m min}$	Smaller dimension of a rectangular section, mm
h_{\max}	Larger dimension of a rectangular section, mm
Κ	Normalized design moment, $\frac{M_u}{bd^2 f_{cu}}$
K'	Maximum $\frac{M_u}{bd^2 f_{cu}}$ for a singly reinforced concrete section
k_1	Shear strength enhancement factor for support compression

11 - 2 Notations

Table 11-1 List of Symbols Used in the CP-2013 Code			
Concrete shear strength factor, $[f_{cu}/25]^{\frac{1}{3}}$			
Design moment at a section, N-mm			
Limiting moment capacity as singly reinforced slab section, N-mm			
Spacing of the links along the strip, mm			
Design torsion at ultimate design load, N-mm			
Perimeter of the punch critical section, mm			
Design shear force at ultimate design load, N			
Design shear stress at a slab cross-section or at a punching critical section, $N\!/mm^2$			
Design concrete shear stress capacity, N/mm ²			
Maximum permitted design factored shear stress, N/mm ²			
Torsional shear stress, N/mm ²			
Neutral axis depth, mm			
Depth of neutral axis in a balanced section, mm			
Lever arm, mm			
Torsional stiffness constant			
Moment redistribution factor in a member			
Partial safety factor for load			
Partial safety factor for material strength			
Maximum concrete strain			
Strain in tension reinforcement			
Strain in compression reinforcement			

Design Load Combinations 11.2

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. The design load combinations are obtained by multiplying the characteristic loads by appropriate partial factors of safety, γ_f (CP 2.3.1.3). For CP-2013, if a structure is subjected to dead (G), live

(Q), pattern live (PQ), and wind (W) loads, and considering that wind forces are reversible, the following load combinations may need to be considered. (CP 2.3.2.1, Table 2.1).

1.4G 1.4G + 1.6Q	(CP 2.3.2)
1.4G + 1.6(0.75PQ)	(CP 2.3.2)
$1.0G \pm 1.4W$ $1.4G \pm 1.4W$ $1.2G + 1.2Q \pm 1.2W$	(CP 2.3.2)

These are also the default design load combinations in ETABS whenever the CP-2013 code is used. If roof live load is separately treated or other types of loads are present, other appropriate load combinations should be used. Note that the automatic combination, including pattern live load, is assumed and should be reviewed before using for design.

11.3 Limits on Material Strength

The concrete compressive strength, f_{cu} , should not be less than 20 N/mm² (CP 3.1.3). The program does not enforce this limit for flexure and shear design of slabs. The input material strengths are used for design even if they are outside of the limits. It is the user's responsible to use the proper strength values while defining the materials.

11.4 Partial Safety Factors

The design strengths for concrete and reinforcement are obtained by dividing the characteristic strength of the material by a partial safety factor, γ_m . The values of γ_m used in the program are listed in the following table, as taken from CP Table 2.2 (CP 2.4.3.2):

11 - 4 Limits on Material Strength

Values of γ_m for the Ultimate Limit State			
Reinforcement	1.15		
Concrete in flexure and axial load	1.50		
Concrete shear strength without shear reinforcement	1.25		

These factors are incorporated into the design equations and tables in the code, but can be overwritten.

11.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

11.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

11.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

11.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding the compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 11-1 (CP 6.1.2.4(a)), where $\mathcal{E}_{c,max}$ is defined as:

$$\varepsilon_{c,\max} = \begin{cases} 0.0035 & \text{if } f_{cu} \le 60\text{N/mm}^2\\ 0.0035 - 0.00006 (f_{cu} - 60)^{\frac{1}{2}} & \text{if } f_{cu} > 60\text{N/mm}^2 \end{cases}$$

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Furthermore, it is assumed that moment redistribution in the member does not exceed 10% (i.e., $\beta_b \ge 0.9$; CP 6.1.2.4(b)). The code also places a limitation on the neutral axis depth,

$$\frac{x}{d} \leq \begin{cases} 0.5 & \text{for} & f_{cu} \leq 45 \text{ N/mm}^2 \\ 0.4 & \text{for} & 45 < f_{cu} \leq 70 \text{ N/mm}^2 \\ 0.33 & \text{for} & 70 < f_{cu} \leq 100 \text{ N/mm}^2 \end{cases}$$
(CP 6.1.2.4(b))

to safeguard against non-ductile failures (CP 6.1.2.4(b)). In addition, the area of compression reinforcement is calculated assuming that the neutral axis depth remains at the maximum permitted value.

The depth of the compression block is given by:

$$a = \begin{cases} 0.9x & \text{for} & f_{cu} \le 45 \text{ N/mm}^2 \\ 0.8x & \text{for} & 45 < f_{cu} \le 70 \text{ N/mm}^2 \\ 0.72x & \text{for} & 70 < f_{cu} \le 100 \text{ N/mm}^2 \end{cases}$$
(CP 6.1.2.4(a), Fig 6.1)

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed $(0.1f_{cu}A_g)$ (CP 6.1.2.4(a)), axial force is ignored; hence, all slabs are designed for major direction flexure and shear only. Axial compression greater than $0.1f_{cu}A_g$ and axial tensions are always included in flexural and shear design.

11.5.1.2.1 Design of uniform thickness slab

For uniform thickness slab, the limiting moment capacity as a singly reinforced slab, M_{single} , is obtained first for a section. The reinforcing is determined based on whether *M* is greater than, less than, or equal to M_{single} . See Figure 11-1

Calculate the ultimate limiting moment of resistance of the section as singly reinforced.

$$M_{\text{single}} = K' f_{cu} b d^2$$
, where (CP 6.1.2.4(c), Eqn. 6.8)

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$$K' = \begin{cases} 0.156 \text{ for } f_{cu} \le 45 \text{ N/mm}^2 \\ 0.120 \text{ for } 45 < f_{cu} \le 70 \text{ N/mm}^2 \\ 0.094 \text{ for } 70 < f_{cu} \le 100 \text{ N/mm}^2 \end{cases}$$

• If $M \leq M_{\text{single}}$, the area of tension reinforcement, A_s , is obtained from:

$$A_s = \frac{M}{0.87 f_y z}$$
, where (CP 6.1.2.4(c), Eqn. 6.12)



Figure 11-1 Uniform Thickness Slab Design

$$z = d \left(0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right) \le 0.95d \qquad (CP \ 6.1.2.4(c), \ Eqn. \ 6.10)$$
$$K = \frac{M}{f_{cu}bd^2} \qquad (CP \ 6.1.2.4(c), \ Eqn. \ 6.7)$$

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This reinforcement is to be placed at the bottom if M is positive, or at the top if *M* is negative.

• If $M > M_{\text{single}}$, compression reinforcement is required and calculated as follows:

$$A'_{s} = \frac{M - M_{\text{single}}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{c}}\right)(d - d')}$$
(CP 6.1.2.4(c), , Eqn. 6.15)

where d' is the depth of the compression reinforcement from the concrete compression face, and

$$f'_{s} = E_{s}\varepsilon_{c}\left(1 - \frac{d'}{x}\right) \le 0.87f_{y}, (CP \qquad 6.1.2.4(c), \qquad 3.2.6, Fig. 3.9)$$

$$x = \begin{cases} \frac{d-z}{0.45}, & \text{for} & f_{cu} \le 45 \,\text{N/mm}^2 \\ \frac{d-z}{0.40}, & \text{for} & 45 < f_{cu} \le 70 \,\text{N/mm}^2 & (\text{CP } 6.1.2.4(a), & \text{Fig } 6.1, & \text{Eqn}, \\ \frac{d-z}{0.36}, & \text{for} & 70 < f_{cu} \le 100 \,\text{N/mm}^2 \end{cases}$$
6.11)

$$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right\} \le 0.95d$$
 (CP 6.1.2.4(c))

The tension reinforcement required for balancing the compression in the concrete and the compression reinforcement is calculated as:

$$A_{s} = \frac{M_{\text{single}}}{0.87 f_{y} z} + \frac{M - M_{\text{single}}}{0.87 f_{y} (d - d')}$$
(CP
6.1.2.4(c))

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11.5.1.2.2 Design of nonuniform thickness slab

11.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

11.5.1.2.2.2 Flanged Slab Section Under Positive Moment

With the flange in compression, the program analyzes the section by considering alternative locations of the neutral axis. Initially, the neutral axis is assumed to be located in the flange. On the basis of this assumption, the program calculates the exact depth of the neutral axis. If the stress block does not extend beyond the flange thickness, the section is designed as a uniform thickness slab of width b_{f} . If the stress block extends beyond the flange depth, the contribution of the web to the flexural strength of the slab is taken into account. See Figure 11-2.

Assuming the neutral axis to lie in the flange, the normalized moment is given by:

$$K = \frac{M}{f_{cu} b_f d^2}.$$
 (CP 6.1.2.4(c) , Eqn. 6.7)

Then the moment arm is computed as:

z =
$$d \left\{ 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right\} \le 0.95d$$
, (CP 6.1.2.4(c), Eqn. 6.10)

the depth of the neutral axis is computed as:

$$x = \begin{cases} \frac{d-z}{0.45}, & \text{for} & f_{cu} \le 45 \,\text{N/mm}^2 \\ \frac{d-z}{0.40}, & \text{for} & 45 < f_{cu} \le 70 \,\text{N/mm}^2 & (\text{CP } 6.1.2.4(\text{c}), \text{ Fig } 6.1, \text{, Eqn.} \\ \frac{d-z}{0.36}, & \text{for} & 70 < f_{cu} \le 100 \,\text{N/mm}^2 \end{cases}$$
6.11)

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and the depth of the compression block is given by:

$$a = \begin{cases} 0.9x & \text{for} \qquad f_{cu} \le 45 \text{ N/mm}^2 \\ 0.8x & \text{for} \qquad 45 < f_{cu} \le 70 \text{ N/mm}^2 \\ 0.72x & \text{for} \qquad 70 < f_{cu} \le 100 \text{ N/mm}^2 \end{cases}$$
(CP 6.1.2.4(a), Fig 6.1)

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in that case, the width of the slab is taken as b_f . Compression reinforcement is required when K > K'.
- If $a > h_f$, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 11-2.



Figure 11-2 Nonuniform Thickness Slab Design

In that case, the ultimate resistance moment of the flange is given by:

$$M_f = \frac{0.67}{\gamma_c} f_{cu} \left(b_f - b_w \right) h_f \left(d - 0.5 h_f \right)$$

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The moment taken by the web is computed as:

$$M_{w} = M - M_{f}$$

and the normalized moment resisted by the web is given by:

$$K_w = \frac{M_w}{f_{cu} b_w d^2}$$

• If $K_w \le K'$ (CP 6.1.2.4(c)), the slab is designed as a singly reinforced concrete section. The reinforcement is calculated as the sum of two parts, one to balance compression in the flange and one to balance compression in the web.

$$A_{s} = \frac{M_{f}}{0.87f_{y}(d - 0.5h_{f})} + \frac{M_{w}}{0.87f_{y}z}, \text{ where}$$
$$z = d\left(0.5 + \sqrt{0.25 - \frac{K_{w}}{0.9}}\right) \le 0.95d$$

• If $K_w > K'$, compression reinforcement is required and is calculated as follows:

The ultimate moment of resistance of the web only is given by:

$$M_{uw} = K f_{cu} b_w d^2$$

The compression reinforcement is required to resist a moment of magnitude $M_w - M_{uw}$. The compression reinforcement is computed as:

$$A'_{s} = \frac{M_{w} - M_{uw}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{c}}\right)\left(d - d'\right)}$$

where, d' is the depth of the compression reinforcement from the concrete compression face, and

$$f_s = E_s \varepsilon_c \left(1 - \frac{d}{x} \right) \le 0.87 f_y$$
 (CP 6.1.2.4(c), 3.2.6, Fig 3.9)

The area of tension reinforcement is obtained from equilibrium as:

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$$\begin{split} A_{s} &= \frac{1}{0.87 f_{y}} \Bigg[\frac{M_{f}}{d - 0.5 h_{f}} + \frac{M_{uw}}{z} + \frac{M_{w} - M_{uw}}{d - d} \\ z &= d \Bigg(0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \Bigg) \le 0.95 d \end{split}$$

11.5.1.2.2.3 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required in each direction of a slab is given by the following limits (CP 9.3.1.1), with interpolation for reinforcement of intermediate strength:

$$A_{s} \geq \begin{cases} 0.0024bh & \text{if} \quad f_{y} \leq 250 \text{ MPa} \\ 0.0013bh & \text{if} \quad f_{y} \geq 460 \text{ MPa} \end{cases}$$
(CP 9.3.1.1(a))

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (CP 9.2.1.3).

11.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved (CP 6.1.2.5):

- Determine the shear stress, *v*.
- Determine the shear stress, v_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

11.5.2.1 Determine Shear Stress

In the design of the slab shear reinforcement, the shear stresses for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors:

$$v = \frac{V}{bd}$$
 (CP 6.1.2.5(a))

The maximum allowable shear stress, v_{max} is defined as:

$$v_{\text{max}} = \min(0.8 \sqrt{f_{cu}}, 7 \text{ MPa})$$
 (CP 6.1.2.5(a))

11.5.2.2 Determine Concrete Shear Capacity

The shear stress carried by the concrete, v_c , is calculated as:

$$v'_{c} = v_{c} + 0.6 \frac{NVh}{A_{c}M} \le v_{c} \sqrt{1 + \frac{N}{A_{c}v_{c}}}$$
 (CP 6.1.2.5(k) , Eqn. 6.22)

$$v_c = \frac{0.79k_1k_2}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(CP 6.1.2.5(c), Table 6.3)

 k_1 is the enhancement factor for support compression,

and is conservatively taken as 1 (CP 6.1.2.5(g))

$$k_{2} = \left(\frac{f_{cu}}{25}\right)^{\frac{1}{3}}, \qquad 1 \le k_{2} \le \left(\frac{80}{25}\right)^{\frac{1}{3}} \qquad (CP \ 6.1.2.5(c), \ Table \ 6.3)$$
$$\gamma_{m} = 1.25 \qquad (CP \ 6.1.2.5(c), \ Table \ 6.3)$$

However, the following limitations also apply:

$$0.15 \le \frac{100A_s}{bd} \le 3,$$
 (CP 6.1.2.5(c), Table 6.3)

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$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge \begin{array}{c} 0.67, & \text{Members without shear reinforcement} \\ 1.00, & \text{Members with shear reinforcement} \end{array}$

(CP 6.1.2.5(c), Table 6.3)

$$\frac{Vh}{M} \le 1$$
 (CP 6.1.2.5(k))

11.5.2.3 Determine Required Shear Reinforcement

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (CP Table 6.2, CP 6.1.2.5(b)):

 Calculate the design average shear stress that can be carried by minimum shear reinforcement, v_r, as:

$$v_{r} = \begin{cases} 0.4 & \text{if} \quad f_{cu} \le 40 \,\text{N/mm}^{2} \\ 0.4 \left(\frac{f_{cu}}{40} \right)^{\frac{2}{3}} & \text{if} \ 40 < f_{cu} \le 80 \,\text{N/mm}^{2} \\ 0.4 \left(\frac{80}{40} \right)^{\frac{2}{3}} & \text{if} \quad f_{cu} > 80 \,\text{N/mm}^{2} \end{cases}$$
(CP 6.1.2.5(b), Table 6.2)

• If $v \le v'_c + v_r$, minimum reinforcement is required:

$$\frac{A_s}{s_v} = \frac{v_r b}{0.87 f_{vv}},$$
 (CP 6.1.2.5(b))

• If $v > v'_c + v_r$,

$$\frac{A_{sv}}{s_v} = \frac{(v - v'_c)b}{0.87f_{yv}}$$
(CP 6.1.2.5(b))

• If $v > v_{\text{max}}$, a failure condition is declared. (CP 6.1.2.5(b))

The maximum of all the calculated A_{sv}/s_v values obtained from each load combination is reported along with the controlling shear force and associated load combination.

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The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

11.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

11.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of 1.5d from the face of the support (CP 6.1.5.7(d)). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (CP 6.1.5.7). Figure 11-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 11-3 Punching Shear Perimeters

11.5.3.2 Determine Concrete Capacity

The concrete punching shear factored strength is taken as (CP 6.1.5.7(d), Table 6.3):

$$v_c = \frac{0.79k_1k_2}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(CP 6.1.2.5(d), Table 6.3)

 k_1 is the enhancement factor for support compression,

and is conservatively taken as 1 (CP 6.1.2.5(g), 6.1.5.7(d))

 $k_2 = \left(\frac{f_{cu}}{25}\right)^{\frac{1}{3}} \ 1 \le k_2 \le \left(\frac{80}{25}\right)^{\frac{1}{3}}$ (CP 6.1.2.5(c), Table 6.3)

$$\gamma_m = 1.25$$
 (CP 2.4.3.2, Table 2.2)

However, the following limitations also apply:

$$0.15 \le \frac{100A_s}{bd} \le 3,$$
(CP 6.1.2.5(c), Table 6.3)
$$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge \begin{cases} 0.67, & \text{Members without shear reinforcement} \\ 1.00, & \text{Members with shear reinforcement} \end{cases}$$
(CP 6.1.2.5(c), Table 6.3)

 A_s = area of tension reinforcement, which is taken as the average tension reinforcement of design strips in Layer A and layer B where Layer A and Layer design strips are in orthogonal directions. When design strips are not present in both orthogonal directions then tension reinforcement is taken as zero in the current implementation.

$$v \le \min(0.8\sqrt{f_{cu}}, 7 \text{ MPa})$$
 (CP 6.1.5.7(b))

$$f_{cu} \le 80 \text{ MPa} \text{ (for calculation purpose only)}$$
 (CP Table 6.3)

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11.5.3.3 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the bending axis, the nominal design shear stress, v_{max} , is calculated as:

$$V_{eff,x} = V\left(f + \frac{1.5M_x}{Vy}\right)$$
(CP 6.1.5.6(b), 6.1.5.6(c))
$$V_{eff,y} = V\left(f + \frac{1.5M_y}{Vx}\right)$$
(CP 6.1.5.6(b), 6.1.5.6(c))
$$v_{max} = max \begin{cases} \frac{V_{eff,x}}{u \, d} \\ \frac{V_{eff,y}}{u \, d} \end{cases}$$
(CP 6.1.5.7)

where,

~

- u is the perimeter of the critical section,
- *x* and *y* are the lengths of the sides of the critical section parallel to the axis of bending,
- M_x and M_y are the design moments transmitted from the slab to the column at the connection,
- V is the total punching shear force, and
- f is a factor to consider the eccentricity of punching shear force and is taken as

1.00	for interior columns	
$f = \{1.25\}$	for edge columns	(CP 6.1.5.6(b), 6.1.5.6(c))
1.25	for corner columns	

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11.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

11.5.4 Design Punching Shear Reinforcement

The use of shear links as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm (CP 6.1.5.7(e)). The use of shear studs is not covered in Hong Kong CP 2013. However, program uses the identical clauses for shear studs when CP 20013 code is selected. If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is carried out as described in the subsections that follow.

11.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

11.5.4.2 Determine Required Shear Reinforcement

The shear stress is limited to a maximum of:

$$v_{\rm max} = 2v_c$$
 (CP 6.1.5.7(e))

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (CP 6.1.5.7(e)).

• If $v \le 1.6v_c$,

$$\frac{A_{v}}{s} = \frac{(v - v_{c})ud}{0.87 f_{yv}} \ge \frac{v_{r}ud}{0.87 f_{yv}},$$
(CP 6.1.5.7(e))

• If
$$1.6v_c \le v < 2.0v_c$$
,

$$\frac{A_v}{s} = \frac{5(0.7v - v_c)ud}{0.87 f_{yv}} \ge \frac{v_r ud}{0.87 f_{yv}},$$
(CP 6.1.5.7(e))

$$v_r = \begin{cases} 0.4 \\ 0.4 \left(\frac{f_{cu}}{40}\right)^{2/3} \text{ N/mm}^2 \end{cases}$$
(CP 6.1.5.7, Table 6.2)

• If $v > 2.0v_c$, a failure condition is declared. (CP 6.1.5.7(e))

If *v* exceeds the maximum permitted value of v_{max} , the concrete section should be increased in size.

11.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 11-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 1.5*d* measured in a direction parallel to the column face (CP 6.1.5.7(f)).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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Figure 11-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

11.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in CP 4.2.4 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 10-, 12-, 14-, 16-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 1.5*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$s_o \leq 0.5d$	(CP 6.1.5.7(f))
-----------------	-----------------

$s \leq 0.75d$	(CP 6.1.5.7(f))
----------------	-----------------

 $g \le 1.5d$ (CP 6.1.5.7(f))

Stirrups are only permitted when slab thickness is greater than 200 mm (CP 6.1.5.7(e)).

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Chapter 12 Design for Hong Kong CP-04

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Hong Kong limit state code CP-04 [CP 04], which also incorporates Amendment 1 published in June 2007, is selected. The various notations used in this chapter are listed in Table 12-1. For referencing to the pertinent sections of the Hong Kong code in this chapter, a prefix "CP" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

12.1 Notations

Table 12-1 List of Symbols Used in the CP-04 Code

- A_g Gross area of cross-section, mm²
- A_l Area of longitudinal reinforcement for torsion, mm²

A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²
A_{sv}	Total cross-sectional area of links at the neutral axis, mm ²
$A_{sv,t}$	Total cross-sectional area of closed links for torsion, mm ²
A_{sv}/s_v	Area of shear reinforcement per unit length, mm ² /mm
а	Depth of compression block, mm
b	Width or effective width of the section in the compression zone, mm
b_{f}	Width or effective width of flange, mm
b_w	Average web width of a flanged shaped section, mm
С	Torsional constant, mm ⁴
d	Effective depth of tension reinforcement, mm
d'	Depth to center of compression reinforcement, mm
E_c	Modulus of elasticity of concrete, N/mm ²
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 N/mm ²
f	Punching shear factor considering column location
f_{cu}	Characteristic cube strength, N/mm ²
f'_s	Stress in the compression reinforcement, N/mm ²
f_y	Characteristic strength of reinforcement, N/mm ²
f_{yv}	Characteristic strength of shear reinforcement, N/mm ²
h	Overall depth of a section in the plane of bending, mm
h_{f}	Flange thickness, mm
h_{\min}	Smaller dimension of a rectangular section, mm
h_{\max}	Larger dimension of a rectangular section, mm
Κ	Normalized design moment, $\frac{M_u}{bd^2 f_{uu}}$

K' Maximum
$$\frac{M_u}{bd^2 f_{cu}}$$
 for a singly reinforced concrete section

12 - 2 Notations

Table 12-1 List of Symbols Used in the CP-04 Code		
k_1	Shear strength enhancement factor for support compression	
k_2	Concrete shear strength factor, $\left[f_{cu}/25\right]^{\frac{1}{3}}$	
М	Design moment at a section, N-mm	
$M_{ m single}$	Limiting moment capacity as singly reinforced section, N-mm	
S_{v}	Spacing of the links along the strip, mm	
Т	Design torsion at ultimate design load, N-mm	
и	Perimeter of the punch critical section, mm	
V	Design shear force at ultimate design load, N	
V	Design shear stress at a slab cross-section or at a punching critical section, $N\!/mm^2$	
\mathcal{V}_{C}	Design concrete shear stress capacity, N/mm ²	
$v_{\rm max}$	Maximum permitted design factored shear stress, N/mm ²	
V_t	Torsional shear stress, N/mm ²	
x	Neutral axis depth, mm	
$x_{\rm bal}$	Depth of neutral axis in a balanced section, mm	
Z.	Lever arm, mm	
β	Torsional stiffness constant	
eta_b	Moment redistribution factor in a member	
γf	Partial safety factor for load	
γ_m	Partial safety factor for material strength	
\mathcal{E}_{C}	Maximum concrete strain	
\mathcal{E}_{s}	Strain in tension reinforcement	
\mathcal{E}'_s	Strain in compression reinforcement	

12.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. The design load combinations are obtained by multiplying the characteristic loads by appropriate partial factors of safety, γ_f (CP 2.3.1.3). For CP-04, if a structure is subjected to dead (D), live (L), pattern live (PL), and wind (W) loads, and considering that wind forces are reversible, the following load combinations may need to be considered. (CP 2.3.2.1, Table 2.1).

1.4D 1.4D + 1.6L	(CP 2.3.2)
1.4D + 1.6(0.75PL)	(CP 2.3.2)
$1.0D \pm 1.4W$ $1.4D \pm 1.4W$ $1.2D + 1.2L \pm 1.2W$	(CP 2.3.2)

These are also the default design load combinations in ETABS whenever the CP-04 code is used. If roof live load is separately treated or other types of loads are present, other appropriate load combinations should be used. Note that the automatic combination, including pattern live load, is assumed and should be reviewed before using for design.

12.3 Limits on Material Strength

The concrete compressive strength, f_{cu} , should not be less than 20 N/mm² (CP 3.1.3). The program does not enforce this limit for flexure and shear design of slabs. The input material strengths are used for design even if they are outside of the limits. It is the user's responsible to use the proper strength values while defining the materials.

12.4 Partial Safety Factors

The design strengths for concrete and reinforcement are obtained by dividing the characteristic strength of the material by a partial safety factor, γ_m . The values of γ_m used in the program are listed in the following table, as taken from CP Table 2.2 (CP 2.4.3.2):

12 - 4 Limits on Material Strength

Values of γ_m for the Ultimate Limit State		
Reinforcement	1.15	
Concrete in flexure and axial load	1.50	
Concrete shear strength without shear reinforcement	1.25	

These factors are incorporated into the design equations and tables in the code, but can be overwritten.

12.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

12.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

12.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

12.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding the compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 12-1 (CP 6.1.2.4(a)), where $\mathcal{E}_{c,max}$ is defined as:

$$\varepsilon_{c,\max} = \begin{cases} 0.0035 & \text{if } f_{cu} \le 60\text{N/mm}^2\\ 0.0035 - 0.00006 (f_{cu} - 60)^{\frac{1}{2}} & \text{if } f_{cu} > 60\text{N/mm}^2 \end{cases}$$

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Furthermore, it is assumed that moment redistribution in the member does not exceed 10% (i.e., $\beta_b \ge 0.9$; CP 6.1.2.4(b)). The code also places a limitation on the neutral axis depth,

$$\frac{x}{d} \leq \begin{cases} 0.5 & \text{for} & f_{cu} \leq 45 \text{ N/mm}^2 \\ 0.4 & \text{for} & 45 < f_{cu} \leq 70 \text{ N/mm}^2 \\ 0.33 & \text{for} & 70 < f_{cu} \leq 100 \text{ N/mm}^2 \end{cases}$$
(CP 6.1.2.4(b))

to safeguard against non-ductile failures (CP 6.1.2.4(b)). In addition, the area of compression reinforcement is calculated assuming that the neutral axis depth remains at the maximum permitted value.

The depth of the compression block is given by:

$$a = \begin{cases} 0.9x & \text{for} & f_{cu} \le 45 \text{ N/mm}^2 \\ 0.8x & \text{for} & 45 < f_{cu} \le 70 \text{ N/mm}^2 \\ 0.72x & \text{for} & 70 < f_{cu} \le 100 \text{ N/mm}^2 \end{cases}$$
(CP 6.1.2.4(a), Fig 6.1)

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed $(0.1f_{cu}A_g)$ (CP 6.1.2.4(a)), axial force is ignored; hence, all slabs are designed for major direction flexure and shear only. Axial compression greater than $0.1f_{cu}A_g$ and axial tensions are always included in flexural and shear design.

12.5.1.2.1 Design of uniform thickness slab

For uniform thickness slab, the limiting moment capacity as a singly reinforced section, M_{single} , is obtained first for a section. The reinforcing is determined based on whether *M* is greater than, less than, or equal to M_{single} . See Figure 12-1

Calculate the ultimate limiting moment of resistance of the section as singly reinforced.

$$M_{\text{single}} = K' f_{cu} b d^2, \text{ where} \qquad (\text{CP 6.1.2.4(c)})$$

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$$K' = \begin{cases} 0.156 \text{ for } f_{cu} \le 45 \text{ N/mm}^2 \\ 0.120 \text{ for } 45 < f_{cu} \le 70 \text{ N/mm}^2 \\ 0.094 \text{ for } 70 < f_{cu} \le 100 \text{ N/mm}^2 \end{cases}$$

• If $M \le M_{\text{single}}$, the area of tension reinforcement, A_s , is obtained from:

$$A_s = \frac{M}{0.87 f_y z}$$
, where (CP 6.1.2.4(c))



Figure 12-1 Uniform Thickness Slab Design

$$z = d \left(0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right) \le 0.95d$$
 (CP 6.1.2.4(c))
$$K = \frac{M}{f_{cu}bd^2}$$
 (CP 6.1.2.4(c))

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This reinforcement is to be placed at the bottom if M is positive, or at the top if M is negative.

• If $M > M_{\text{single}}$, compression reinforcement is required and calculated as follows:

$$A'_{s} = \frac{M - M_{\text{single}}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{c}}\right)(d - d')}$$
(CP 6.1.2.4(c))

where d' is the depth of the compression reinforcement from the concrete compression face, and

$$f'_{s} = E_{s}\varepsilon_{c}\left(1 - \frac{d'}{x}\right) \le 0.87f_{y}, (CP \qquad 6.1.2.4(c), \qquad 3.2.6, Fig.$$

$$x = \begin{cases} \frac{d-z}{0.45}, & \text{for} \qquad f_{cu} \le 45 \,\text{N/mm}^2 \\ \frac{d-z}{0.40}, & \text{for} \qquad 45 < f_{cu} \le 70 \,\text{N/mm}^2 \\ \frac{d-z}{0.36}, & \text{for} \qquad 70 < f_{cu} \le 100 \,\text{N/mm}^2 \end{cases}$$
(CP 6.1.2.4(a), Fig 6.1)
$$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right\} \le 0.95d$$
(CP 6.1.2.4(c))

The tension reinforcement required for balancing the compression in the concrete and the compression reinforcement is calculated as:

$$A_{s} = \frac{M_{\text{single}}}{0.87 f_{y} z} + \frac{M - M_{\text{single}}}{0.87 f_{y} (d - d')}$$
(CP
6.1.2.4(c))

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12.5.1.2.2 Design of nonuniform thickness slab

12.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

12.5.1.2.2.2 Flanged Slab Section Under Positive Moment

With the flange in compression, the program analyzes the section by considering alternative locations of the neutral axis. Initially, the neutral axis is assumed to be located in the flange. On the basis of this assumption, the program calculates the exact depth of the neutral axis. If the stress block does not extend beyond the flange thickness, the section is designed as a uniform thickness slab of width b_{f} . If the stress block extends beyond the flange depth, the contribution of the web to the flexural strength of the section is taken into account. See Figure 12-2.

Assuming the neutral axis to lie in the flange, the normalized moment is given by:

$$K = \frac{M}{f_{cu} b_f d^2}.$$
 (CP 6.1.2.4(c))

Then the moment arm is computed as:

z =
$$d \left\{ 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right\} \le 0.95d,$$
 (CP 6.1.2.4(c))

the depth of the neutral axis is computed as:

$$x = \begin{cases} \frac{d-z}{0.45}, & \text{for} \qquad f_{cu} \le 45 \,\text{N/mm}^2 \\ \frac{d-z}{0.40}, & \text{for} \qquad 45 < f_{cu} \le 70 \,\text{N/mm}^2 \\ \frac{d-z}{0.36}, & \text{for} \qquad 70 < f_{cu} \le 100 \,\text{N/mm}^2 \end{cases}$$
(CP 6.1.2.4(c), Fig 6.1)

and the depth of the compression block is given by:

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$$a = \begin{cases} 0.9x & \text{for} & f_{cu} \le 45 \text{ N/mm}^2 \\ 0.8x & \text{for} & 45 \le f_{cu} \le 70 \text{ N/mm}^2 \\ 0.72x & \text{for} & 70 \le f_{cu} \le 100 \text{ N/mm}^2 \end{cases}$$
(CP 6.1.2.4(a), Fig 6.1)

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in that case, the width of the slab is taken as b_f . Compression reinforcement is required when K > K'.
- If a > h_f, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f, and the second part is for balancing the compressive force from the web, C_w, as shown in Figure 12-2.



Figure 12-2 Nonuniform Thickness Slab Design

In that case, the ultimate resistance moment of the flange is given by:

$$M_f = \frac{0.67}{\gamma_c} f_{cu} \left(b_f - b_w \right) h_f \left(d - 0.5 h_f \right)$$

The moment taken by the web is computed as:

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$$M_w = M - M_f$$

and the normalized moment resisted by the web is given by:

$$K_w = \frac{M_w}{f_{cu} b_w d^2}$$

• If $K_w \le K'$ (CP 6.1.2.4(c)), the slab is designed as a singly reinforced concrete slab. The reinforcement is calculated as the sum of two parts, one to balance compression in the flange and one to balance compression in the web.

$$A_{s} = \frac{M_{f}}{0.87f_{y}(d - 0.5h_{f})} + \frac{M_{w}}{0.87f_{y}z}, \text{ where}$$
$$z = d\left(0.5 + \sqrt{0.25 - \frac{K_{w}}{0.9}}\right) \le 0.95d$$

• If $K_w > K'$, compression reinforcement is required and is calculated as follows:

The ultimate moment of resistance of the web only is given by:

$$M_{uw} = K f_{cu} b_w d^2$$

The compression reinforcement is required to resist a moment of magnitude $M_w - M_{uw}$. The compression reinforcement is computed as:

$$A'_{s} = \frac{M_{w} - M_{uw}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{c}}\right)\left(d - d'\right)}$$

where, d' is the depth of the compression reinforcement from the concrete compression face, and

$$f_s = E_s \varepsilon_c \left(1 - \frac{d}{x} \right) \le 0.87 f_y$$
 (CP 6.1.2.4(c), 3.2.6, Fig 3.9)

The area of tension reinforcement is obtained from equilibrium as:

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$$A_{s} = \frac{1}{0.87 f_{y}} \left[\frac{M_{f}}{d - 0.5h_{f}} + \frac{M_{uw}}{z} + \frac{M_{w} - M_{uw}}{d - d'} \right]$$
$$z = d \left(0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right) \le 0.95d$$

12.5.1.2.2.3 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required in each direction of a slab is given by the following limits (CP 9.3.1.1), with interpolation for reinforcement of intermediate strength:

$$A_{s} \geq \begin{cases} 0.0024bh & \text{if} \quad f_{y} \leq 250 \text{ MPa} \\ 0.0013bh & \text{if} \quad f_{y} \geq 460 \text{ MPa} \end{cases}$$
(CP 9.3.1.1(a))

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (CP 9.2.1.3).

12.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved (CP 6.1.2.5):

- Determine the shear stress, *v*.
- Determine the shear stress, v_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

12.5.2.1 Determine Shear Stress

In the design of the slab shear reinforcement, the shear stresses for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors:

$$v = \frac{V}{bd}$$
 (CP 6.1.2.5(a))

The maximum allowable shear stress, v_{max} is defined as:

$$v_{\text{max}} = \min(0.8 \sqrt{f_{cu}}, 7 \text{ MPa})$$
 (CP 6.1.2.5(a))

12.5.2.2 Determine Concrete Shear Capacity

The shear stress carried by the concrete, v_c , is calculated as:

$$v'_{c} = v_{c} + 0.6 \frac{NVh}{A_{c}M} \le v_{c} \sqrt{1 + \frac{N}{A_{c}v_{c}}}$$
 (CP 6.1.2.5(k))

$$v_c = \frac{0.79k_1k_2}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(CP 6.1.2.5(c), Table 6.3)

 k_1 is the enhancement factor for support compression,

and is conservatively taken as 1 (CP 6.1.2.5(g))

$$k_{2} = \left(\frac{f_{cu}}{25}\right)^{\frac{1}{3}}, \qquad 1 \le k_{2} \le \left(\frac{80}{25}\right)^{\frac{1}{3}} \qquad (CP \ 6.1.2.5(c), \ Table \ 6.3)$$
$$\gamma_{m} = 1.25 \qquad (CP \ 6.1.2.5(c), \ Table \ 6.3)$$

However, the following limitations also apply:

$$0.15 \le \frac{100A_s}{bd} \le 3,$$
 (CP 6.1.2.5(c), Table 6.3)

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 $\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge \begin{array}{c} 0.67, & \text{Members without shear reinforcement} \\ 1.00, & \text{Members with shear reinforcement} \end{array}$

(CP 6.1.2.5(c), Table 6.3)

$$\frac{Vh}{M} \le 1$$
 (CP 6.1.2.5(k))

12.5.2.3 Determine Required Shear Reinforcement

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (CP Table 6.2, CP 6.1.2.5(b)):

 Calculate the design average shear stress that can be carried by minimum shear reinforcement, v_r, as:

$$v_{r} = \begin{cases} 0.4 & \text{if} \quad f_{cu} \le 40 \,\text{N/mm}^{2} \\ 0.4 \left(\frac{f_{cu}}{40} \right)^{\frac{2}{3}} & \text{if} \ 40 < f_{cu} \le 80 \,\text{N/mm}^{2} \\ 0.4 \left(\frac{80}{40} \right)^{\frac{2}{3}} & \text{if} \quad f_{cu} > 80 \,\text{N/mm}^{2} \end{cases}$$
(CP 6.1.2.5(b), Table 6.2)

• If $v \le v'_c + v_r$, minimum reinforcement is required:

$$\frac{A_s}{s_v} = \frac{v_r b}{0.87 f_{vv}},$$
 (CP 6.1.2.5(b))

• If $v > v'_c + v_r$,

$$\frac{A_{sv}}{s_v} = \frac{(v - v'_c)b}{0.87f_{yv}}$$
(CP 6.1.2.5(b))

• If $v > v_{\text{max}}$, a failure condition is declared. (CP 6.1.2.5(b))

The maximum of all the calculated A_{sv}/s_v values obtained from each load combination is reported along with the controlling shear force and associated load combination.

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The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

12.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the *Key Features and Terminology* manual. Only the code-specific items are described in the following subsections.

12.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of 1.5d from the face of the support (CP 6.1.5.7(d)). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (CP 6.1.5.7). Figure 12-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 12-3 Punching Shear Perimeters

12.5.3.2 Determine Concrete Capacity

The concrete punching shear factored strength is taken as (CP 6.1.5.7(d), Table 6.3):

$$v_c = \frac{0.79k_1k_2}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(CP 6.1.2.5(d), Table 6.3)

 k_1 is the enhancement factor for support compression,

and is conservatively taken as 1 (CP 6.1.2.5(g), 6.1.5.7(d))

 $k_{2} = \left(\frac{f_{cu}}{25}\right)^{\frac{1}{3}} 1 \le k_{2} \le \left(\frac{80}{25}\right)^{\frac{1}{3}}$ (CP 6.1.2.5(c), Table 6.3) γ

$$v_m = 1.25$$
 (CP 2.4.3.2, Table 2.2)

However, the following limitations also apply:

$$0.15 \le \frac{100A_s}{bd} \le 3,$$
(CP 6.1.2.5(c), Table 6.3)
$$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge \begin{cases} 0.67, & \text{Members without shear reinforcement} \\ 1.00, & \text{Members with shear reinforcement} \end{cases}$$
(CP 6.1.2.5(c), Table 6.3)

 A_s = area of tension reinforcement, which is taken as the average tension reinforcement of design strips in Layer A and layer B where Layer A and Layer design strips are in orthogonal directions. When design strips are not present in both orthogonal directions then tension reinforcement is taken as zero in the current implementation.

$$v \le \min(0.8\sqrt{f_{cu}}, 7 \text{ MPa})$$
 (CP 6.1.5.7(b))

$$f_{cu} \le 80 \text{ MPa} \text{ (for calculation purpose only)}$$
 (CP Table 6.3)

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12.5.3.3 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the bending axis, the nominal design shear stress, v_{max} , is calculated as:

$$V_{eff,x} = V \left(f + \frac{1.5M_x}{Vy} \right)$$
(CP 6.1.5.6(b), 6.1.5.6(c))
$$V_{eff,y} = V \left(f + \frac{1.5M_y}{Vx} \right)$$
(CP 6.1.5.6(b), 6.1.5.6(c))
$$v_{max} = \max \begin{cases} \frac{V_{eff,x}}{u \, d} \\ \frac{V_{eff,y}}{u \, d} \end{cases}$$
(CP 6.1.5.7)

where,

~

- u is the perimeter of the critical section,
- *x* and *y* are the lengths of the sides of the critical section parallel to the axis of bending,
- M_x and M_y are the design moments transmitted from the slab to the column at the connection,
- V is the total punching shear force, and
- f is a factor to consider the eccentricity of punching shear force and is taken as

1.00	for interior columns	
$f = \{1.25\}$	for edge columns	(CP 6.1.5.6(b), 6.1.5.6(c))
1.25	for corner columns	

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12.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

12.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm (CP 6.1.5.7(e)). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is carried out as described in the subsections that follow.

12.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

12.5.4.2 Determine Required Shear Reinforcement

The shear stress is limited to a maximum of:

$$v_{\rm max} = 2v_c$$
 (CP 6.1.5.7(e))

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (CP 6.1.5.7(e)).

• If $v \leq 1.6v_c$,

$$\frac{A_{v}}{s} = \frac{(v - v_{c})ud}{0.87 f_{yv}} \ge \frac{v_{r}ud}{0.87 f_{yv}},$$
(CP 6.1.5.7(e))

• If
$$1.6v_c \le v < 2.0v_c$$
,

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$$\frac{A_{v}}{s} = \frac{5(0.7v - v_{c})ud}{0.87 f_{yv}} \ge \frac{v_{r}ud}{0.87 f_{yv}},$$
(CP 6.1.5.7(e))
$$v_{r} = \begin{cases} 0.4 \\ 0.4 \left(\frac{f_{cu}}{40}\right)^{2/3} \text{ N/mm}^{2} \end{cases}$$
(CP 6.1.5.7, Table 6.2)

• If $v > 2.0v_c$, a failure condition is declared. (CP 6.1.5.7(e))

If *v* exceeds the maximum permitted value of v_{max} , the concrete section should be increased in size.

12.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 12-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 1.5*d* measured in a direction parallel to the column face (CP 6.1.5.7(f)).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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Figure 12-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

12.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in CP 4.2.4 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 10-, 12-, 14-, 16-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 1.5*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$s_o \leq 0.5d$	(CP 6.1.5.7(f))
-----------------	-----------------

$s \leq 0.75d$	(CP 6.1.5.7(f))
----------------	-----------------

 $g \le 1.5d$ (CP 6.1.5.7(f))

Stirrups are only permitted when slab thickness is greater than 200 mm (CP 6.1.5.7(e)).

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Chapter 13 Design for IS 456-2000

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Indian Code IS 456-2000 [IS 2000] is selected. Various notations used in this chapter are listed in Table 13-1. For referencing to the pertinent sections of the Indian code in this chapter, a prefix "IS" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

13.1 Notations

A_c	Area of concrete, mm ²
A_{cv}	Area of section for shear resistance, mm ²
A_g	Gross cross-sectional area of a frame member, mm ²

A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²
A_{sv}	Total cross-sectional area of links at the neutral axis, mm ²
A_{sv}/s_v	Area of shear reinforcement per unit length, mm ² /mm
а	Depth to the center of the compression block, mm
<i>a</i> 1	Width of the punching critical section in the direction of bending, mm
a_2	Width of the punching critical section perpendicular to the direc- tion of bending, mm
b	Width or effective width of the section in the compression zone, mm
b_f	Width or effective width of flange, mm
b_w	Average web width of a flanged section, mm
d	Effective depth of tension reinforcement, mm
d'	Effective depth of compression reinforcement, mm
D	Overall depth of a slab, mm
D_{f}	Flange thickness in a flanged shaped-section, mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 MPa
f_{cd}	Design concrete strength = f_{ck} / γ_c , MPa
f_{ck}	Characteristic compressive strength of concrete, MPa
f_{sc}	Compressive stress in compression steel, MPa
f_{yd}	Design yield strength of reinforcement = f_y / γ_s , MPa
f_y	Characteristic strength of reinforcement, MPa
f_{ys}	Characteristic strength of shear reinforcement, MPa
k	Enhancement factor of shear strength for depth of the slab
$M_{ m single}$	Design moment resistance of a section as a singly reinforced sec- tion, N-mm
M_u	Ultimate factored design moment at a section, N-mm

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Table 13-1 List of Symbols Used in the IS 456-2000 Code		
M_t	Equivalent factored bending moment due to torsion at a section, N-mm	
M_{e1}	Equivalent factored moment including moment and torsion effects ($M_{e1} = M_u + M_i$) at a section, N-mm	
M_{e2}	Residual factored moment when $M_t > M_u$ at a section applied in the opposite sense of M_{el} at a section, N-mm	
т	Normalized design moment, $M/bd^2 \alpha f_{ck}$	
S_{V}	Spacing of the shear reinforcement along the strip, mm	
T_u	Factored torsional moment at a section, N-mm	
V_u	Factored shear force at a section, N	
V_e	Equivalent factored shear force including torsion effects, N	
Vc	Allowable shear stress in punching shear mode, N	
x_u	Depth of neutral axis, mm	
$x_{u,\max}$	Maximum permitted depth of neutral axis, mm	
Z.	Lever arm, mm	
α	Concrete strength reduction factor for sustained loading, as well as reinforcement over strength factor for computing capacity mo- ment at a section	
β	Factor for the depth of compressive force resultant of the concrete stress block	
eta_c	Ratio of the minimum to maximum dimensions of the punching critical section	
γ_c	Partial safety factor for concrete strength	
γf	Partial safety factor for load, and fraction of unbalanced moment transferred by flexure	
γ_m	Partial safety factor for material strength	
γ_s	Partial safety factor for reinforcement strength	
δ	Enhancement factor of shear strength for compression	
$\mathcal{E}_{c,\max}$	Maximum concrete strain in the slab (= 0.0035)	

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Table 13-1 List of Symbols Used in the IS 456-2000 Code		
\mathcal{E}_{s}	Strain in tension steel	
\mathcal{E}_{s}'	Strain in compression steel	
$ au_{v}$	Average design shear stress resisted by concrete, MPa	
$ au_c$	Basic design shear stress resisted by concrete, MPa	
$ au_{c,\max}$	Maximum possible design shear stress permitted at a section, MPa	
$ au_{cd}$	Design shear stress resisted by concrete, MPa	

Table 13-1 List of Symbols Used in the IS 456-2000 C	Code

Design Load Combinations 13.2

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For IS 456-2000, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (IS 36.4, Table 18):

1.5D	(IS 36.4.1)
1.5D + 1.5L 1.5D + 1.5S	(IS 36.4.1)
1.5D + 1.5(0.75 PL)	(IS 31.5.2.3)
$\begin{array}{l} 1.5D \pm 1.5W \\ 0.9D \pm 1.5W \\ 1.2D + 1.2L \pm 1.2W \\ 1.5D + 1.5L \pm 1.0W \end{array}$	(IS 36.4.1)
$1.5D \pm 1.5E$ $0.9D \pm 1.5E$ $1.2D + 1.2L \pm 1.2E$ $1.5D + 1.5L \pm 1.0E$	(IS 36.4.1)

13 - 4 Design Load Combinations

 $\begin{array}{l} 1.5D + 1.5L + 1.5S \\ 1.2D + 1.2S \pm 1.2W \\ 1.2D + 1.2L + 1.2S \pm 1.2W \\ 1.2D + 1.2S \pm 1.2E \\ 1.2D + 1.2L + 1.2S \pm 1.2E \end{array} \tag{IS 36.4.1}$

These are also the default design load combinations in ETABS whenever the IS 456-2000 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

13.3 Partial Safety Factors

The design strength for concrete and reinforcement is obtained by dividing the characteristic strength of the material by a partial safety factor, γ_m . The values of γ_m used in the program are as follows:

Partial safety factor for reinforcement, $\gamma_s = 1.15$	(IS 36.4.2.1)
Partial safety factor for concrete, $\gamma_c = 1.5$	(IS 36.4.2.1)

These factors are already incorporated into the design equations and tables in the code. These values can be overwritten; however, caution is advised.

13.4 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

13.4.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

13.4.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

13.4.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding compression

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reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified parabolic stress block shown in Figure 13-1 (IS 38.1). The area of the stress block, c, and the depth of the center of the compressive force from the extreme compression fiber, a, are taken as

$$c = \alpha f_{\rm ck} x_u \tag{IS 38.1}$$

$$a = \beta x_{\rm u} \tag{IS 38.1}$$



Figure 13-1 Uniform Thickness Slab Design

where x_u is the depth of the neutral axis, and α and β are taken as:

$$\alpha = 0.36$$
 (IS 38.1)

$$\beta = 0.42$$
 (IS 38.1)

where α is the reduction factor to account for sustained compression and the partial safety factor for concrete and is generally taken to be 0.36 for the assumed parabolic stress block (IS 38.1). The β factor considers the depth to the center of the compressive force.

Furthermore, it is assumed that moment redistribution in the member does not exceed the code-specified limiting value. The code also places a limitation on the neutral axis depth, as shown in the following table, to safeguard against non-ductile failures (IS 38.1). ETABS uses interpolation between these three values.

f_y (MPa)	$x_{u,\max}/d$
250	0.53
415	0.48
500	0.46

When the applied moment exceeds the moment capacity of the slab as a singly reinforced section, the area of compression reinforcement is calculated assuming that the neutral axis depth remains at the maximum permitted value. The maximum fiber compression is taken as:

$$\varepsilon_{c,\max} = 0.0035$$
 (IS 38.1)

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the subsections that follow. It is assumed that the design ultimate axial force can be neglected; hence all slabs are designed for major direction flexure and shear only.

13.4.1.3 Design of uniform thickness slab

For uniform thickness slab, the limiting depth of the neutral axis, $x_{u,max}$, and the moment capacity as a singly reinforced section, M_{single} , are obtained first. The reinforcement area is determined based on whether M_u is greater than, less than, or equal to M_{single} .

• Calculate the limiting depth of the neutral axis.

$$\frac{x_{u,\max}}{d} = \begin{cases} 0.53 & \text{if} \quad f_y \le 250 \text{ MPa} \\ 0.53 - 0.05 \frac{f_y - 250}{165} & \text{if} \quad 250 < f_y \le 415 \text{ MPa} \\ 0.48 - 0.02 \frac{f_y - 415}{85} & \text{if} \quad 415 < f_y \le 500 \text{ MPa} \\ 0.46 & \text{if} \quad f_y \ge 500 \text{ MPa} \end{cases}$$
(IS 38.1)

• Calculate the limiting ultimate moment of resistance as a singly reinforced section.

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$$M_{\text{single}} = \alpha \frac{x_{u,\text{max}}}{d} \left(1 - \beta \frac{x_{u,\text{max}}}{d} \right) b d^2 f_{ck}$$
(IS G-1.1)

• Calculate the depth of the neutral axis as:

$$\frac{x_u}{d} = \frac{1 - \sqrt{1 - 4\beta m}}{2\beta}$$

where the normalized design moment, m, is given by

$$m = \frac{M_u}{bd^2 \alpha f_{ck}}$$

- If $M_u \leq M_{\text{single}}$ the area of tension reinforcement, A_s , is obtained from

$$A_s = \frac{M_u}{\left(f_y / \gamma_s\right) z}, \text{ where} \qquad (\text{IS G-1.1})$$

$$z = d\left\{1 - \beta \frac{x_u}{d}\right\}.$$
 (IS 38.1)

This reinforcement is to be placed at the bottom if M_u is positive, or at the top if M_u is negative.

- If $M_u > M_{single}$, the area of compression reinforcement, A'_s , is given by:

$$A'_{s} = \frac{M_{u} - M_{\text{single}}}{\left(f_{sc} - \frac{0.67f_{ck}}{\gamma_{m}}\right)(d - d')}$$
(IS G-1.2)

where d' is the depth of the compression reinforcement from the concrete compression face, and

$$f_{sc} = \varepsilon_{c,\max} E_s \left[1 - \frac{d'}{x_{u,\max}} \right] \le \frac{f_y}{\gamma_s}$$
(IS G-1.2)

The required tension reinforcement is calculated as:

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$$A_{s} = \frac{M_{\text{single}}}{\left(f_{y}/\gamma_{s}\right)z} + \frac{M_{u} - M_{\text{single}}}{\left(f_{y}/\gamma_{s}\right)\left(d - d'\right)}, \text{ where}$$
(IS G-1.2)

$$z = d \left\{ 1 - \beta \frac{x_{u,\max}}{d} \right\}$$
 (IS 38.1)

 A_s is to be placed at the bottom and A'_s is to be placed at the top if M_u is positive, and vice versa if M_u is negative.

13.4.1.4 Design of nonuniform thickness slab

13.4.1.4.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_u (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

13.4.1.4.2 Flanged Slab Section Under Positive Moment

With the flange in compression, the program analyzes the section by considering alternative locations of the neutral axis. Initially the neutral axis is assumed to be located within the flange. On the basis of this assumption, the program calculates the depth of the neutral axis. If the stress block does not extend beyond the flange thickness, the section is designed as a uniform thickness slab of width $b_{f.}$. If the stress block extends beyond the flange depth, the contribution of the web to the flexural strength of the slab is taken into account. See Figure 13-2.



Figure 13-2 Nonuniform Thickness Slab Design

Assuming the neutral axis lies in the flange, the depth of the neutral axis is calculated as:

$$\frac{x_u}{d} = \frac{1 - \sqrt{1 - 4\beta m}}{2\beta}$$

where the normalized design moment, m, is given by

$$m = \frac{M_u}{b_f d^2 \alpha f_{ck}}$$

• If $\left(\frac{x_u}{d}\right) \le \left(\frac{D_f}{d}\right)$, the neutral axis lies within the flange and the subsequent

calculations for A_s are exactly the same as previously defined for the uniform thickness slab design (IS G-2.1). However, in this case, the width of the slab is taken as b_f . Compression reinforcement is required when $M_u > M_{\text{single}}$.

• If $\left(\frac{x_u}{d}\right) > \left(\frac{D_f}{d}\right)$, the neutral axis lies below the flange and the calculation for

 A_s has two parts. The first part is for balancing the compressive force from the

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flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 13-2.

- Calculate the ultimate resistance moment of the flange as:

$$M_f = 0.45 f_{ck} \left(b_f - b_w \right) \gamma_f \left(d - \frac{\gamma_f}{2} \right)$$
 (IS G-2.2)

where γ_f is taken as:

$$\gamma_f = \begin{cases} D_f & \text{if } D_f \le 0.2d \\ 0.15x_u + 0.65D_f & \text{if } D_f > 0.2d \end{cases}$$
(IS G-2.2)

- Calculate the moment taken by the web as

$$M_w = M_u - M_f.$$

- Calculate the limiting ultimate moment of resistance of the web for tension reinforcement as:

$$M_{w,\text{single}} = \alpha f_{ck} b_w d^2 \frac{x_{u,\text{max}}}{d} \left[1 - \beta \frac{x_{u,\text{max}}}{d} \right] \text{ where} \qquad \text{(IS G-1.1)}$$

$$\frac{x_{u,\text{max}}}{d} = \begin{cases} 0.53 & \text{if} \quad f_y \le 250 \text{ MPa} \\ 0.53 - 0.05 \frac{f_y - 250}{165} & \text{if} \quad 250 < f_y \le 415 \text{ MPa} \\ 0.48 - 0.02 \frac{f_y - 415}{85} & \text{if} \quad 415 < f_y \le 500 \text{ MPa} \\ 0.46 & \text{if} \qquad f_y \ge 500 \text{ MPa} \end{cases}$$

• If $M_w \le M_{w,\text{single}}$, the slab is designed as a singly reinforced concrete slab. The area of reinforcement is calculated as the sum of two parts, one to balance compression in the flange and one to balance compression in the web.

$$A_{s} = \frac{M_{f}}{\left(f_{y}/\gamma_{s}\right)\left(d - 0.5 y_{f}\right)} + \frac{M_{w}}{\left(f_{y}/\gamma_{s}\right)z}, \text{ where }$$

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$$z = d \left\{ 1 - \beta \frac{x_u}{d} \right\}$$
$$\frac{x_u}{d} = \frac{1 - \sqrt{1 - 4\beta m}}{2\beta}$$
$$m = \frac{M_w}{b_w d^2 \alpha f_{ck}}$$

• If $M_w > M_{w,single}$, the area of compression reinforcement, A'_s , is given by:

$$A'_{s} = \frac{M_{w} - M_{w,\text{single}}}{\left(f'_{s} - \frac{0.67f_{ck}}{\gamma_{m}}\right)(d - d')}$$

where d' is the depth of the compression reinforcement from the concrete compression face, and

$$f_{sc} = \varepsilon_{c,\max} E_s \left[1 - \frac{d'}{x_{u,\max}} \right] \le \frac{f_y}{\gamma_s}$$
(IS G-1.2)

The required tension reinforcement is calculated as:

$$A_{s} = \frac{M_{f}}{\left(f_{y}/\gamma_{s}\right)\left(d-0.5\gamma_{f}\right)} + \frac{M_{w,\text{single}}}{\left(f_{y}/\gamma_{s}\right)z} + \frac{M_{w}-M_{w,\text{single}}}{\left(f_{y}/\gamma_{s}\right)\left(d-d'\right)} \text{ where}$$
$$z = d\left\{1 - \beta \frac{x_{u,\text{max}}}{d}\right\}$$

13.4.1.5 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (IS 26.5.2):

$$A_{s} \leq \begin{cases} 0.0015bD & \text{if} \quad f_{y} < 415 \text{ MPa} \\ 0.0012bD & \text{if} \quad f_{y} \ge 415 \text{ MPa} \end{cases}$$
(IS 26.5.2.1)

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In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (IS 26.5.1.1).

13.4.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved (IS 40.1):

- Determine the design shear stress
- Determine the shear stress that can be resisted by the concrete
- Determine the shear reinforcement required to carry the balance

Determine the design nominal shear stress as follows.

For prismatic sections

$$\tau_v = \frac{V_u}{bd} \tag{IS 40.1}$$

• For non-prismatic sections (slab with varying depth)

$$\tau_v = \frac{V_u \pm \frac{M_u}{d} \tan \beta}{bd}, \text{ where}$$
(IS 40.1.1)

 β = angle between the top and bottom edges of the slab

 M_u is the moment at the section, and the negative sign is considered when the numerical value of the moment increases in the same direction as the depth, *d*, and the positive sign is considered when the numerical value of the moment decreases in the same direction as the depth increases.

$$\tau_{v} \leq \tau_{c,\max} \tag{IS 40.2.3, Table 20}$$

The maximum nominal shear stress, $\tau_{c,\max}$ is given in IS Table 20 as follows:

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Maximum Shear Stress, τ _{c,max} (MPa) (IS 40.2.3, IS Table 20)						
Concrete Grade	M15	M20	M25	M30	M35	M40
$\tau_{c,\max}$ (MPa)	2.5	2.8	3.1	3.5	3.7	4.0

The maximum nominal shear stress, $\tau_{c,max}$, is computed using linear interpolation for concrete grades between those indicated in IS Table 20.

Determine the design shear stress that can be carried by the concrete, as:

$$\tau_{cd} = k \delta \lambda \tau_c, \tag{IS 40.2}$$

where k is the enhancement factor for the depth of the section, taken as 1.0 for slabs, and is computed as follows for other slabs:

$$k = 1$$
 (IS 40.2.1.1)

 δ is the enhancement factor for compression and is given as:

$$\delta = \begin{cases} 1 + 3 \frac{P_u}{A_g f_{ck}} \le 1.5 & \text{if } P_u > 0, \text{ Under Compression} \\ 1 & \text{if } P_u \le 0, \text{ Under Tension} \end{cases}$$
(IS 40.2.2)

 δ is always taken as 1

 λ is the factor for light-weight concrete, and

 τ_c is the basic design shear strength for concrete, which is given by:

$$\tau_c = 0.64 \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{f_{ck}}{25}\right)^{\frac{1}{4}}$$
(IS 40.2.1)

The preceding expression approximates IS Table 19. It should be noted that the value of γ_c has already been incorporated in IS Table 19 (see note in IS 36.4.2.1). The following limitations are enforced in the determination of the design shear strength as is the case in the Table.

$$0.15 \le \frac{100 A_s}{bd} \le 3$$
 (IS 40.2.1, Table 19)

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 $f_{ck} \le 40$ MPa (for calculation purpose only) (IS 40.2.1, Table 19)

Determine required shear reinforcement:

- If $\tau_v \le \tau_{cd} + 0.4$, $\frac{A_{sv}}{s_v} = \frac{0.4 \, b}{0.87 \, f_y}$ (IS 40.3, 26.5.1.6)
- If $\tau_{cd} + 0.4 < \tau_v \leq \tau_{c,\max}$,

$$\frac{A_{sv}}{s_{v}} = \frac{(\tau_{v} - \tau_{cd})b}{0.87 f_{y}}$$
(IS 40.4(a))

$$\frac{A_{sv}}{s_{v}} \ge \frac{0.4b}{0.87 f_{y}}$$
(IS 40.4(a))

• If $\tau_v > \tau_{c,\max}$, a failure condition is declared. (IS 40.2.3)

In calculating the shear reinforcement, a limit is imposed on the f_y as:

$$f_y \le 415 \text{ MPa}$$
 (IS 40.4)

The maximum of all of the calculated A_{sv}/s_v values, obtained from each load combination, is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

13.4.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

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13.4.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (IS 31.6.1). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (IS 31.6.1). Figure 13-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner), and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 13-3 Punching Shear Perimeters

13.4.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be αM_u and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $(1 - \alpha) M_u$ (IS 31.6.2.2), where:

$$\alpha = \frac{1}{1 + (2/3)\sqrt{a_1/a_2}}$$
(IS 31.3.3)

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and a_1 is the width of the critical section measured in the direction of the span and a_2 is the width of the critical section measured in the direction perpendicular to the span.

13.4.3.3 Determine Concrete Capacity

The concrete punching shear factored strength is taken as:

$$v_c = k_s \tau_c$$
 (IS 31.6.3.1)

$$k_s = 0.5 + \beta_c \le 1.0 \tag{IS 31.6.3.1}$$

$$\tau_c = 0.25 \sqrt{f_{ck}}$$
 (IS 31.6.3.1)

 β_c = ratio of the minimum to the maximum dimensions of the support section.

13.4.3.4 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v_{U} = \frac{V_{U}}{b_{0}d} + \frac{\gamma v_{2}[M_{U2} - V_{U}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{U3} - V_{U}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 2

$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "sides" refers to the sides of the critical section for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "sides" refers to the sides of the critical section for punching shear Eq. 4

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Figure 13-4 Shear Stress Calculations at Critical Sections

The equations for \overline{I}_{22} , \overline{I}_{33} and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 2-axis or parallel to the 3-axis. Refer to Figures 13-4.

$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for side of critical section parallel to 2-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2$$
, for side of critical section
parallel to 3-axis Eq. 5b

$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - x_3)^2$$
, for side of critical section
parallel to 2-axis Eq. 6a

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$\overline{I}_{33} = Ld(x_2 - x_3)^2$, for side of critical section parallel to 3-axis	Eq. 6b
$\overline{I}_{23} = Ld(x_2 - x_3)(y_2 - y_3)$, for side of critical section	
parallel to 2-axis or 3-axis	Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

where,

- b_0 = Perimeter of critical section for punching shear
- d = Effective depth at critical section for punching shear based on the average of d for the 2 direction and d for the 3 direction
- I_{22} = Moment of inertia of critical section for punching shear about an axis that is parallel to the local 2-axis
- I_{33} = Moment of inertia of critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of inertia of critical section for punching shear with respect to the 2 and 3 planes
- *L* = Length of side of critical section for punching shear currently being considered
- M_{U2} = Moment about line parallel to 2-axis at center of column (positive in accordance with the right-hand rule)
- M_{U3} = Moment about line parallel to 3-axis at center of column (positive in accordance with the right-hand rule)
- v_U = Punching shear stress
- V_U = Shear at center of column (positive upward)
- x_1, y_1 = Coordinates of column centroid
- x_2, y_2 = Coordinates of center of one side of critical section for punching shear

 x_3, y_3 = Coordinates of centroid of critical section for punching shear

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- x_4 , y_4 = Coordinates of location where you are calculating stress
- γ_{V2} = Percent of M_{U2} resisted by shear
- γ_{V3} = Percent of M_{U3} resisted by shear

13.4.3.5 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

13.4.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is completed as described in the subsections that follow.

13.4.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined, but limited to:

$$v_c \le 1.5\tau_c$$
 (IS 31.6.3.2)

13.4.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$V_{\rm max} = 0.5 \,\tau_c \, b_o d \tag{IS 31.6.3.2}$$

Given V_u , V_c , and V_{max} , the required shear reinforcement is calculated as follows (IS 31.6.3.2).

$$A_{v} = \frac{\left(V_{u} - 0.5V_{c}\right)S}{0.87f_{y}d}$$
(IS 31.6.3.2, 40.4(a))

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- If $V_u > V_{\text{max}}$, a failure condition is declared. (IS 31.6.3.2)
- If V_u exceeds the maximum permitted value of V_{max} , the concrete section should be increased in size.

13.4.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 13-5 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 13-6 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2d measured in a direction parallel to the column face.

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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13.4.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in IS 26.4 plus half of the diameter of the flexural reinforcement.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

 $s_o \le 0.5d$ $s \le 0.5d$ $g \le 2d$

Chapter 14 Design for Italian NTC 2008

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Italian code NTC2008 [D.M. 14/01/2008] is selected. For the load combinations, reference is also made to NTC2008. Various notations used in this chapter are listed in Table 14-1.

The design is based on user-specified loading combinations. However, the program provides a set of default load combinations that should satisfy requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

14.1 Notations

Table 14-1 List of Symbols Used in the NTC2008

A_c	Area of concrete section, mm ²
A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²

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	List of Symbols Used in the NTC2008
$\overline{A_{sl}}$	Area of longitudinal reinforcement for torsion, mm ²
A_{sw}	Total cross-sectional area of links at the neutral axis, mm ²
A_{sw}/s_v	Area of shear reinforcement per unit length, mm ² /mm
A_t/s	Area of transverse reinforcement per unit length for torsion, mm ² /mm
а	Depth of compression block, mm
b	Width or effective width of the section in the compression zone, mm
b_f	Width or effective width of flange, mm
b_w	Average web width of a flanged shaped-section, mm
d	Effective depth of tension reinforcement, mm
d'	Effective depth of compression reinforcement, mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement
f_{cd}	Design concrete strength = $\alpha_{cc} f_{ck} / \gamma_c$, MPa
f_{ck}	Characteristic compressive concrete cylinder strength at 28 days, MPa
f_{ctm}	Mean value of concrete axial tensile strength, MPa
f_{cwd}	Design concrete compressive strength for shear design = α_{cc} $\frac{f_{cwk}}{\gamma_c}$, MPa
f_{cwk}	Characteristic compressive cylinder strength for shear design, MPa
f'_s	Compressive stress in compression reinforcement, MPa
f_{yd}	Design yield strength of reinforcement = f_{yk}/γ_s , MPa
f_{yk}	Characteristic strength of shear reinforcement, MPa
f_{ywd}	Design strength of shear reinforcement = f_{ywk}/γ_s , MPa
f_{ywk}	Characteristic strength of shear reinforcement, MPa
h	Overall depth of section, mm

Table 14-1 List of Symbols Used in the NTC2008

Table 14-1	List of Symbols Used in the NTC2008
h_{f}	Flange thickness, mm
M_{Ed}	Design moment at a section, N-mm
m	Normalized design moment, $M/bd^2\eta f_{cd}$
$m_{ m lim}$	Limiting normalized moment capacity as a singly reinforced sec- tion
S_{V}	Spacing of the shear reinforcement, mm
T_{Ed}	Torsion at ultimate design load, N-mm
T_{Rdc}	Torsional cracking moment, N-mm
$T_{Rd,\max}$	Design torsional resistance moment, N-mm
и	Perimeter of the punch critical section, mm
V_{Rdc}	Design shear resistance from concrete alone, N
$V_{Rd,\max}$	Design limiting shear resistance of a cross-section, N
V_{Ed}	Shear force at ultimate design load, N
x	Depth of neutral axis, mm
$x_{\rm lim}$	Limiting depth of neutral axis, mm
Z.	Lever arm, mm
$lpha_{cc}$	Coefficient accounting for long-term effects on the concrete com- pressive strength
$lpha_{cw}$	Coefficient accounting for the state of stress in the compression chord
δ	Redistribution factor
\mathcal{E}_{c}	Concrete strain
\mathcal{E}_{s}	Strain in tension reinforcement
, Es	Strain in compression steel
γ_c	Partial safety factor for concrete strength
γs	Partial safety factor for reinforcement strength
λ	Factor defining the effective depth of the compression zone

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V	Effectiveness factor for shear resistance without concrete crushing	
η	Concrete strength reduction factor for sustained loading and stress block	
$ ho_l$	Tension reinforcement ratio	
σ_{cp}	Axial stress in the concrete, MPa	
θ	Angle of the concrete compression strut	
ω	Normalized tension reinforcement ratio	
ω'	Normalized compression reinforcement ratio	
$\omega_{ m lim}$	Normalized limiting tension reinforcement ratio	

Table 14-1 List of Symbols Used in the NTC2008

14.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be checked. NTC2008 allows load combinations to be defined based on NTC2008 Equation 2.5.1.

$$\sum_{j\geq 1} \gamma_{G1,j} G_{1k,j} + \sum_{l\geq 1} \gamma_{G2k,l} G_{2k,l} + P + \gamma_{Q,1} Q_{k,1} + \sum_{i>1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}$$
(Eq. 2.5.1)

Load combinations considering seismic loading are automatically generated based on NTC2008 Equation 2.5.5.

$$\sum_{j\geq 1} G_{1k,j} + \sum_{l\geq 1} G_{2k,l} + P + E + \sum_{i>1} \psi_{2,i} Q_{k,i}$$
(Eq. 2.5.5)

For both sets of load combinations, the variable values are defined in the list that follows.

 $\gamma_{G1,sup} = 1.30$ (NTC2008 Table 2.6.I)

$$\gamma_{G1,inf} = 1.00$$
 (NTC2008 Table 2.6.I)

$$\gamma_{G2,sup} = 1.50$$
 (NTC2008 Table 2.6.I)

$$\gamma_{G2,inf} = 0.00$$
 (NTC2008 Table 2.6.I)

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γq,1,suj	_p = 1.5	(NTC2008 Table 2.6.I)
γq,1,inf	= 0.0	(NTC2008 Table 2.6.I)
γq,I,sup	5 = 1.5	(NTC2008 Table 2.6.I)
γQ,I,inf	= 0.0	(NTC2008 Table 2.6.I)
Ψ0,i	= 0.7 (live load, assumed not to be storage)	(Table 2.5.I)
Ψ0,i	= 0.6 (wind load)	(Table 2.5.I)
$\psi_{0,i}$	= 0.5 (snow load, assumed H \leq 1,000 m)	(Table 2.5.I)
Ψ2,i	= 0.3 (live, assumed office/residential space	e) (Table 2.5.I)
Ψ2,i	= 0 (snow, assumed H \leq 1,000 m)	(Table 2.5.I)

If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used.

14.3 Limits on Material Strength

The concrete compressive strength, f_{ck} , should not be greater than 90 MPa (NTC2008 Tab. 4.1.I). The reinforcement material should be B450C or B450A (NTC2008 §11.3.2).

NTC Table 11.3.Ia:		
fy,nom	450 N/mm ²	
ft,nom	540 N/mm ²	

NTC Table 11.3.lb: Material TYPE B450	2 Properties
---------------------------------------	--------------

Properties	Prerequisite	Fracture %	
Characteristic yield stress, f _{yk}	$\geq f_{y,\text{nom}}$	5.0	
Characteristic rupture stress, f_{tk}	$\geq f_{y,\text{nom}}$	5.0	

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$(f_{t'} f_y)_k$	≥ 1.15 < 1.35	10.0
Elongation at rupture		
$(f_{y/} f_{y,nom})_k$	< 1.25	10.0
$(A_{gt})_k$	\geq 7.5 %	10.0

NTC Table 11.3.Ic: Material TYPE B450A Properties

Properties	Prerequisite	Fracture %
Characteristic yield stress, f_{yk}	$\geq f_{y,nom}$	5.0
Characteristic rupture stress, f_{tk}	$\geq f_{y,nom}$	5.0
$(\mathbf{f}_{t'} \mathbf{f}_{y})_k$	≥ 1.05 < 1.25	10.0
$\begin{array}{l} Elongation \ at \ rupture \\ (f_{y\!/} \ f_{y,nom})_k \\ (A_{gt})_k \end{array}$	< 1.25 ≥ 2.5 %	10.0 10.0

14.4 Partial Safety Factors

The design strengths for concrete and steel are obtained by dividing the characteristic strengths of the materials by the partial safety factors, γ_s and γ_c as shown here.

$$f_{cd} = \alpha_{cc} f_{ck} / \gamma_c$$
 (NTC Eq. 4.1.4)
$$f_{yd} = f_{yk} / \gamma_s$$
 (NTC Eq. 4.1.6)

$$f_{ywd} = f_{ywk} / \gamma_s \tag{NTC Eq. 4.1.6}$$

 α_{cc} is the coefficient taking account of long term effects on the compressive strength. α_{cc} is taken as 0.85 (NTC2008 4.1.2.1.1.1) by default and can be overwritten by the user.

14 - 6 Partial Safety Factors

The partial safety factors for the materials and the design strengths of concrete and reinforcement are given in the text that follows (NTC2008 4.1.2.1.1.1-3):

Partial safety factor for reinforcement, $\gamma_s = 1.15$

Partial safety factor for concrete, $\gamma_c = 1.5$

These values can be overwritten; however, caution is advised.

14.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

14.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

Determine factored axial loads and moments for each slab strip.

- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

14.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

14.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user can avoid the need for compression reinforcement by increasing the effective depth, the width, or the grade of concrete.

The design procedure is based on a simplified rectangular stress block, as shown in Figure 14-1 (NTC Fig. 4.1.3). When the applied moment exceeds the moment capacity, the area of compression reinforcement is calculated on the assumption that the additional moment will be carried by compression and additional tension reinforcement.

The design procedure used by the program for both rectangular and flanged sections (T-shaped section) is summarized in the following subsections. . For reinforced concrete design where design ultimate axial compression load does not

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exceed $(0.1 f_{cd} A_g)$, axial force is ignored; hence, all slabs are designed for major direction flexure, shear, and torsion only. Axial compression greater than $(0.1 f_{cd} A_g)$ and axial tensions are always included in flexural and shear design.



Figure 14-1 Uniform Thickness Slab Design

In designing for a factored negative or positive moment, M_{Ed} (i.e., designing top or bottom steel), the effective strength and depth of the compression block are given by $\alpha_{cc}f_{cd}$ and βx (see Figure 14-1) respectively, where:

$$\beta = 0.8$$
 (NTC § 4.1.2.1.2.2)
 $\alpha_{cc} = 0.85$ (NTC § 4.1.2.1.2.2)
 $f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c}$ if $f_{ck} \le 50N / mm^2$
 $\alpha_{cc} = 0.85$
 $\gamma_c = 1.5$

if $f_{ck} > 50N / mm^2$ NTC 2008 refer to Eurocode 2:

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$$f_{cd} = \alpha_{cc} \eta \frac{f_{ck}}{\gamma_c}$$

$$\eta = 1.0 - (f_{ck} - 50)/200 \text{ for } 50 < f_{ck} \le 90 \text{ MPa}$$
(EC2 Eq. 3.22)

For the design of the slab, a ductility criterion, suggested in Eurocode 2 § 5.5, is followed.

The limiting value of the ratio of the neutral axis depth at the ultimate limit state to the effective depth, $(x/d)_{\text{lim}}$, is expressed as a function of the ratio of the redistributed moment to the moment before redistribution, δ , as follows:

$$(x/d)_{\text{lim}} = (\delta - k_1)/k_2 \text{ for } f_{ck} \le 50 \text{ MPa}$$
 (EC2 Eq. 5.10a)

$$(x/d)_{\text{lim}} = (\delta - k_3)/k_4 \text{ for } f_{ck} > 50 \text{ MPa}$$
 (EC2 Eq. 5.10b)

No redistribution is assumed, such that δ is assumed to be 1. The four factors, k_1 , k_2 , k_3 , and k_4 are defined as:

$$k_I = 0.44$$
 (EC2 5.5(4))

$$k_2 = 1.25(0.6 + 0.0014/\varepsilon_{cu})$$
 (EC2 5.5(4))

$$k_3 = 0.54$$
 (EC2 5.5(4))

$$k_4 = 1.25 (0.6 + 0.0014 / \varepsilon_{cu}) \tag{EC2 5.5(4)}$$

where the ultimate strain, ε_{cu2} , is determined from EC2 Table 3.1 as:

$$\varepsilon_{cu2} = 0.0035$$
 for $f_{ck} < 50$ MPa (NTC § 4.1.2.1.2.2)

$$\varepsilon_{cu2} = 2.6 + 35 \left[\left(90 - f_{ck} \right) / 100 \right]^4 \text{ for } f_{ck} \ge 50 \text{ MPa}$$
 (NTC § 4.1.2.1.2.2)

14.5.1.2.1 Uniform Thickness Slab Flexural Reinforcement

For uniform thickness slab, the normalized moment, m, and the normalized section capacity as a singly reinforced section, m_{lim} , are determined as:

$$m = \frac{M}{bd^2 f_{cd}}$$

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$$m_{\rm lim} = \beta \left(\frac{x}{d}\right)_{\rm lim} \left[1 - \frac{\beta}{2} \left(\frac{x}{d}\right)_{\rm lim}\right]$$

The reinforcing steel area is determined based on whether m is greater than, less than, or equal to m_{lim} .

If *m* ≤ *m*_{lim}, a singly reinforced slab will be adequate. Calculate the normalized steel ratio, *ω*, and the required area of tension reinforcement, *A_s*, as:

$$\omega = 1 - \sqrt{1 - 2m}$$
$$A_s = \omega \left[\frac{f_{cd}bd}{f_{yd}} \right]$$

This area of reinforcing steel is to be placed at the bottom if M_{Ed} is positive, or at the top if M_{Ed} is negative.

If m > m_{lim}, compression reinforcement is required. Calculate the normalized steel ratios, ω', ω_{lim}, and ω, as:

$$\omega_{lim} = \beta \left(\frac{x}{d}\right)_{lim} = 1 - \sqrt{1 - 2m_{lim}}$$

$$\omega' = \frac{m - m_{\lim}}{1 - d'/d}$$

 $\omega = \omega_{\lim} + \omega'$

where d' is the depth to the compression steel, measured from the concrete compression face.

Calculate the required area of compression and tension reinforcement, A_s' and A_s , as:

$$A_{s}' = \omega' \left[\frac{f_{cd}bd}{f_{s}'} \right]$$

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$$A_s = \omega \left[\frac{f_{cd} b d}{f_{yd}} \right]$$

where f_{s}' , the stress in the compression steel, is calculated as:

$$f_{s}' = E_{s} \varepsilon_{c} \left[1 - \frac{d'}{x_{lim}} \right] \leq f_{yd}$$

 A_s is to be placed at the bottom and $A_{s'}$ is to be placed at the top if M_{Ed} is positive, and $A_{s'}$ is to be placed at the bottom and A_s is to be placed at the top if M_{Ed} is negative.

14.5.1.2.2 Nonuniform Thickness Slab Flexural Reinforcement

In designing a T-shaped slab section, a simplified stress block, as shown in Figure 14-2, as assumed if the flange is in compression, i.e., if the moment is positive. If the moment is negative, the flange is in tension, and therefore ignored. In that case, a simplified stress block, similar to that shown in Figure 14-2, is assumed on the compression side.

14.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_{Ed} (i.e., designing top steel), the calculation of the reinforcing steel area is exactly the same as described for a uniform thickness slab, i.e., no specific flanged data is used.

14.5.1.2.2.2 Flanged Slab Section Under Positive Moment

In designing for a factored positive moment, M_{Ed} , the program analyzes the section by considering the depth of the stress block. If the depth of the stress block is less than or equal to the flange thickness, the section is designed as a uniform thickness with a width b_f . If the stress block extends into the web, additional calculation is required.

For flanged-shaped section, the normalized moment, m, and the normalized section capacity as a singly reinforced section, m_{lim} , are calculated as:

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$$m = \frac{M}{b_f d^2 f_{cd}}$$
$$m_{\rm lim} = \beta \left(\frac{x}{d}\right)_{\rm lim} \left[1 - \frac{\beta}{2} \left(\frac{x}{d}\right)_{\rm lim}\right]$$

Calculate the normalized steel ratios ω_{lim} and ω , as:

$$\omega_{\rm lim} = \beta \left(\frac{x}{d}\right)_{\rm lim}$$
$$\omega = 1 - \sqrt{1 - 2m}$$

Calculate the maximum depth of the concrete compression block, x_{max} , and the effective depth of the compression block, x, as:

$$x_{\max} = \omega_{\lim} d$$
$$x = \omega d$$

The reinforcing steel area is determined based on whether *m* is greater than, less than, or equal to m_{lim} .

- If x ≤ h_f, the subsequent calculations for A_s are exactly the same as previously defined for uniform thickness slab design. However, in this case, the width of the slab is taken as b_f, as shown in Figure 14-2. Compression reinforcement is required if m>m_{lim}.
- If $x > h_f$, the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, and the second part is for balancing the compressive force from the web, as shown in Figure 14-2.
- The required reinforcing steel area, A_{s2}, and corresponding resistive moment, M₂, for equilibrating compression in the flange outstands are calculated as:

$$A_{s2} = \frac{\left(b_f - b_w\right)h_f f_{cd}}{f_{yd}}$$

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Figure 14-2 Nonuniform Thickness Slab Design

Now calculate the required reinforcing steel area A_{s1} for the rectangular section of width b_w to resist the remaining moment $M_1 = M_{Ed} - M_2$. The normalized moment, m_1 is calculated as:

$$m_1 = \frac{M_1}{b_w d^2 f_{cd}}$$

The reinforcing steel area is determined based on whether m_1 is greater than, less than, or equal to m_{lim} .

If m₁ ≤ m_{lim}, a singly reinforced section will be adequate. Calculate the normalized steel ratio, ω₁, and the required area of tension reinforcement, A_{s1}, as:

$$\omega_{l} = 1 - \sqrt{1 - 2m}$$
$$A_{sl} = \omega_{1} \left[\frac{f_{cd}bd}{f_{yd}} \right]$$

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If *m₁ > m_{lim}*, compression reinforcement is required. Calculate the normalized steel ratios, ω', ω_{lim}, and ω, as:

$$\omega_{\rm lim} = \beta \left(\frac{x}{d}\right)_{\rm lim}$$
$$\omega' = \frac{m - m_{\rm lim}}{1 - d'/d}$$
$$\omega_1 = \omega_{\rm lim} + \omega'$$

where d' is the depth to the compression steel, measured from the concrete compression face.

Calculate the required area of compression and tension reinforcement, A_s' and A_s , as:

$$A_{s'} = \omega' \left[\frac{f_{cd}bd}{f_{s'}} \right]$$
$$A_{sI} = \omega_1 \left[\frac{f_{cd}bd}{f_{yd}} \right]$$

where f_{s}' , the stress in the compression steel, is calculated as:

$$f_{s}' = E_{s}\varepsilon_{c} \left[1 - \frac{d'}{x_{\lim}}\right] \leq f_{yd}$$

The total tensile reinforcement is $A_s = A_{sI} + A_{s2}$, and the total compression reinforcement is A_s' . A_s is to be placed at the bottom and $A_{s'}$ is to be placed at the top of the section.

14.5.1.3 Minimum and Maximum Tensile Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits:

$$A_{s,\min} = 0.26 \frac{f_{ctm}}{f_{yk}} bd$$
 (NTC Eq. 4.1.43)
 $A_{s,\min} = 0.0013bd$ (NTC Eq. 4.1.43)

where f_{ctm} is the mean value of axial tensile strength of the concrete and is computed as:

$$f_{ctm} = 0.30 f_{ck}^{(2/3)} \text{ for } f_{ck} \le 50 \text{ MPa}$$
(NTC Eq. 11.2.3a)
$$f_{ctm} = 2.12 ln (1 + f_{cm} / 10) \text{ for } f_{ck} > 50 \text{ MPa}$$
(NTC Eq. 11.2.3b)
$$f_{cm} = f_{ck} + 8 \text{ MPa}$$
(NTC Eq. 11.2.2)

The minimum flexural tension reinforcement required for control of cracking should be investigated independently by the user.

An upper limit on the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (NTC § 4.1.6.1.1).

14.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved.

- Determine the design forces acting on the section, N_{Ed} and V_{Ed} . Note that N_{Ed} is needed for the calculation of V_{Red} .
- Determine the maximum design shear force that can be carried without crushing of the notional concrete compressive struts, V_{Rcd}.
- Determine the required shear reinforcement as area per unit length, A_{sw}/s .

The following three sections describe in detail the algorithms associated with this process.

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14.5.2.1 Determine Design Shear Force

In the design of the slab shear reinforcement, the shear forces and moments for a particular design load combination at a particular strip are obtained by factoring the associated shear forces and moments with the corresponding design load combination factors.

14.5.2.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, $V_{Rd,c}$, is calculated as:

$$V_{Rd,c} = \left[C_{Rd,c} k \left(100 \rho_1 f_{ck} \right)^{1/3} + k_1 \sigma_{cp} \right] b_w d \qquad (\text{EC2 6.2.2(1)})$$

with a minimum of:

$$V_{Rd,c} = \left(v_{\min} + k_1 \sigma_{cp}\right) b_w d$$
 (EC2 6.2.2(1))

where

 f_{ck} is in MPa

$$k = 1 + \sqrt{\frac{200}{d}} \le 2.0$$
 with *d* in mm (EC2 6.2.2(1))

$$\rho_I = \text{tension reinforcement ratio} = \frac{A_{s1}}{b_w d} \le 0.02$$
(EC2 6.2.2(1))

 A_{sl} = area of tension reinforcement (EC2 6.2.2(1))

$$\sigma_{cp} = N_{Ed} / A_c < 0.2 f_{cd} \text{ MPa}$$
 (EC2 6.2.2(1))

The value of $C_{Rd,c}$, v_{\min} and k_1 for use in a country may be found in its National Annex. The program default values for $C_{Rd,c}$, v_{\min} , and k_1 are given as follows (EC2 6.2.2(1)):

$$C_{Rd,c} = 0.18/\gamma_c$$
 (EC2 6.2.2(1))

$$v_{\min} = 0.035 \, k^{3/2} f_{ck}^{1/2} \tag{EC2 6.2.2(1)}$$

 $k_1 = 0.15.$ (EC2 6.2.2(1))

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For light-weight concrete:

$$C_{Rd,c} = 0.18 / \gamma_c$$
(EC2 11.6.1(1))

$$v_{\min} = 0.03 k^{3/2} f_{ck}^{1/2}$$
(EC2 11.6.1(1))

$$k_l = 0.15.$$
(EC2 11.6.1(1))

14.5.2.3 Determine Maximum Design Shear Force

To prevent crushing of the concrete compression struts, the design shear force V_{Ed} is limited by the maximum sustainable design shear force, V_{Rcd} . If the design shear force exceeds this limit, a failure condition occurs. The maximum sustainable shear force is defined as:

$$V_{Rcd} = 0.9 \cdot d \cdot b_w \cdot \alpha_c f_{cd} \cdot \frac{\cot \alpha + \cot \vartheta}{1 + \cot^2 \vartheta}$$
(NTC Eq. 4.1.19)

 $\alpha_c = 1$ for members not subjected to axial compression

$$=1 + \frac{\sigma_{cp}}{f_{cd}} \text{ for } 0 \le \sigma_{cp} \le 0.25 f_{cd}$$
$$=1.25 \text{ for } 0.25 f_{cd} \le \sigma_{cp} \le 0.5 f_{cd}$$
$$=2.5 \left(1 + \frac{\sigma_{cp}}{f_{cd}}\right) \text{ for } 0.5 f_{cd} \le \sigma_{cp} \le f_{cd}$$

 $f_{cd} = 0.5 f_{cd}$

- α angle between the shear reinforcement and the column axis. In the case of vertical stirrups $\alpha = 90$ degrees
- θ angle between the concrete compression struts and the column axis. NTC 2008 allows θ to be taken between 21.8 and 45 degrees.

14.5.2.4 Determine Required Shear Reinforcement

If V_{Ed} is less than V_{Rcd} , the required shear reinforcement in the form of stirrups or ties per unit spacing, A_{sw}/s , is calculated as:

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$$\frac{A_{sw}}{s} = \frac{V_{Ed}}{0.9d \cdot f_{ywd}} \cdot \frac{1}{\left(\cot\alpha + \cot\theta\right)\sin\alpha}$$
(NTC Eq. 4.1.18)

with $\alpha = 90$ degrees and ϑ given in the previous section.

The maximum of all of the calculated A_{sw}/s values, obtained from each design load combination, is reported for the major direction of the slab, along with the controlling combination name.

The calculated shear reinforcement must be greater than the minimum reinforcement:

$$A_{_{SW,\min}} = 1.5 \cdot b$$

with *b* in millimeters and $A_{sw, min}$ in mm²/mm.

The slab shear reinforcement requirements reported by the program are based purely on shear strength consideration. Any minimum stirrup requirements to satisfy spacing considerations or transverse reinforcement volumetric considerations must be investigated independently by the user.

14.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

NTC2008 for the punching shear check refers to Eurocode2-2004.

14.5.3.1 Critical Section for Punching Shear

The punching shear is checked at the face of the column (EC2 6.4.1(4)) and at a critical section at a distance of 2.0d from the face of the support (EC2 6.4.2(1)). The perimeter of the critical section should be constructed such that its length is minimized. Figure 6-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.

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Figure 6-3 Punching Shear Perimeters

14.5.3.2 Determination of Concrete Capacity

The concrete punching shear stress capacity is taken as:

$$V_{Rd,c} = \left[C_{Rd,c} k \left(100 \rho_1 f_{ck} \right)^{1/3} + k_1 \sigma_{cp} \right]$$
(EC2 6.4.4(1))

with a minimum of:

$$V_{Rd,c} = \left(v_{\min} + k_1 \sigma_{cp} \right)$$
 (EC2 6.4.4(1))

where f_{ck} is in MPa and

$$k = 1 + \sqrt{\frac{200}{d}} \le 2.0$$
 with *d* in mm (EC2 6.4.4(1))

$$\rho_{\rm l} = \sqrt{\rho_{\rm lx} \rho_{\rm ly}} \le 0.02 \tag{EC2 6.4.4(1)}$$

where ρ_{1x} and ρ_{1y} are the reinforcement ratios in the *x* and *y* directions respectively, conservatively taken as zeros, and

$$\sigma_{cp} = (\sigma_{cx} + \sigma_{cy})/2 \qquad (\text{EC2 6.4.4(1)})$$

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where σ_{cx} and σ_{cy} are the normal concrete stresses in the critical section in the *x* and *y* directions respectively, conservatively taken as zeros.

$$C_{Rd,c} = 0.18/\gamma_c$$
 (EC2 6.4.4(1))

$$v_{\min} = 0.035k^{3/2} f_{ck}^{1/2}$$
(EC2 6.4.4(1))

$$k_1 = 0.15$$
 (EC2 6.4.4(1))

14.5.3.3 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear, the nominal design shear stress, v_{Ed} , is calculated as:

$$v_{Ed} = \frac{V_{Ed}}{ud} \left[1 + k \frac{M_{Ed,2}u_1}{V_{Ed}W_{1,2}} + k \frac{M_{Ed,3}u_1}{V_{Ed}W_{1,3}} \right], \text{ where } (EC2 \ 6.4.4(2))$$

- *k* is the function of the aspect ratio of the loaded area in Table 14.1 of EN 1992-1-1
- u_1 is the effective perimeter of the critical section
- *d* is the mean effective depth of the slab
- M_{Ed} is the design moment transmitted from the slab to the column at the connection along bending axis 2 and 3
- V_{Ed} is the total punching shear force
- W_1 accounts for the distribution of shear based on the control perimeter along bending axis 2 and 3.

14.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.
14.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is performed as described in the subsections that follow.

14.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

14.5.4.2 Determine Required Shear Reinforcement

The shear is limited to a maximum of V_{Rcd} calculated in the same manner as explained previously for slabs.

Given v_{Ed} , $v_{Rd,c}$, and v_{Rcd} , the required shear reinforcement is calculated as follows (EC2 6.4.5).

• If $v_{R,dc} < v_{Ed} \leq v_{Rcd}$

$$A_{sw} = \frac{\left(v_{Ed} - 0.75v_{Rd,c}\right)}{1.5f_{ywd,ef}} \left(u_{1}d\right)s_{r}$$
(EC2 6.4.5)

- If $v_{Ed} > v_{Rcd}$, a failure condition is declared. (EC2 6.2.3(3))
- If v_{Ed} exceeds the maximum permitted value of V_{Rcd} the concrete section should be increased in size.

14.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 6-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

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Figure 6-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed 2*d*. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 1.5d measured in a direction parallel to the column face (EC2 9.4.3(1)).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

14.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in EC2 4.4.1 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 10-, 12-, 14-, 16-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.3*d*. The spacing

between adjacent shear studs, g, at the first peripheral line of studs shall not exceed 1.5d and should not exceed 2d at additional perimeters. The limits of s_o and the spacing, s, between the peripheral lines are specified as:

$0.3d \le s_o \le 2d$	(EC2 9.4.3(1))
$s \leq 0.75d$	(EC2 9.4.3(1))
$g \leq 1.5d$ (first perimeter)	(EC2 9.4.3(1))
$g \leq 2d$ (additional perimeters)	(EC2 9.4.3(1))

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Chapter 15 Design for NZS 3101-06

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the New Zealand code NZS 3101-06 [NZS 06] is selected. Various notations used in this chapter are listed in Table 15-1. For referencing to the pertinent sections of the New Zealand code in this chapter, a prefix "NZS" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

15.1 Notations

Table 15-1 List of Symbols Used in the NZS 3101-06 Code

A_{co}	Area enclosed by perimeter of the section, sq-mm
A_{cv}	Area of concrete used to determine shear stress, sq-mm
A_g	Gross area of concrete, sq-mm

A_l	Area of longitudinal reinforcement for torsion, sq-mm
A_o	Gross area enclosed by shear flow path, sq-mm
A_s	Area of tension reinforcement, sq-mm
A'_s	Area of compression reinforcement, sq-mm
$A_{s(required)}$	Area of steel required for tension reinforcement, sq-mm
A_t/s	Area of closed shear reinforcement per unit length for torsion, sq-mm/mm
A_v	Area of shear reinforcement, sq-mm
A_v/s	Area of shear reinforcement per unit length, sq-mm/mm
a	Depth of compression block, mm
a_b	Depth of compression block at balanced condition, mm
a_{\max}	Maximum allowed depth of compression block, mm
b	Width of member, mm
b_f	Effective width of flange (flanged section), mm
b_w	Width of web (flanged section), mm
b_0	Perimeter of the punching critical section, mm
b_1	Width of the punching critical section in the direction of bending, mm
b_2	Width of the punching critical section perpendicular to the direc- tion of bending, mm
С	Distance from extreme compression fiber to the neutral axis, mm
Cb	Distance from extreme compression fiber to neutral axis at bal- anced condition, mm
d	Distance from extreme compression fiber to tension reinforce- ment, mm
d'	Distance from extreme compression fiber to compression rein- forcement, mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 MPa

Table 15-1 List of Symbols Used in the NZS 3101-06 Code

l able 15-1	List of Symbols Used in the NZS 3101-06 Code
f'_c	Specified compressive strength of concrete, MPa
f'_s	Stress in the compression reinforcement, psi
f_y	Specified yield strength of flexural reinforcement, MPa
f_{yt}	Specified yield strength of shear reinforcement, MPa
h	Overall depth of sections, mm
h_{f}	Thickness of slab or flange, mm
k _a	Factor accounting for influence of aggregate size on shear strength
<i>k</i> _d	Factor accounting for influence of member depth on shear strength
M^{*}	Factored design moment at a section, N-mm
p_c	Outside perimeter of concrete section, mm
p_o	Perimeter of area A_o , mm
S	Spacing of shear reinforcement along the strip, mm
T^{*}	Factored design torsion at a section, N-mm
t_c	Assumed wall thickness of an equivalent tube for the gross section, mm
t_o	Assumed wall thickness of an equivalent tube for the area enclosed by the shear flow path, mm
V_c	Shear force resisted by concrete, N
V^{*}	Factored shear force at a section, N
v^{*}	Average design shear stress at a section, MPa
$\mathcal{V}_{\mathcal{C}}$	Design shear stress resisted by concrete, MPa
$v_{\rm max}$	Maximum design shear stress permitted at a section, MPa
V_{tn}	Shear stress due to torsion, MPa
α_s	Punching shear factor accounting for column location
α_l	Concrete strength factor to account for sustained loading and equivalent stress block
β_l	Factor for obtaining depth of compression block in concrete

Table 15-1 List of Symbols Used in the NZS 3101-06 Code

Table 15-1 List of Symbols Used in the NZS 3101-06 Code				
eta_c	Ratio of the maximum to the minimum dimensions of the punch- ing critical section			
\mathcal{E}_{C}	Strain in concrete			
$\mathcal{E}_{c,\max}$	Maximum usable compression strain allowed in the extreme concrete fiber, (0.003 in/in)			
\mathcal{E}_{s}	Strain in reinforcement			
ϕ_b	Strength reduction factor for bending			
ϕ_s	Strength reduction factor for shear and torsion			
Υf	Fraction of unbalanced moment transferred by flexure			
γv	Fraction of unbalanced moment transferred by eccentricity of shear			

15.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For NZS 3101-06, if a structure is subjected to dead (D), live (L), pattern live (PL), snow (S), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (AS/NZS 1170.0, 4.2.2):

1.35D	(AS/NZS 1170.0, 4.2.2(a))
1.2D + 1.5L	(AS/NZS 1170.0, 4.2.2(b))
1.2D + 1.5(0.75 PL)	(AS/NZS 1170.0, 4.2.2(b))
1.2D + 0.4L + 1.0S	(AS/NZS 1170.0, 4.2.2(g))
$1.2D \pm 1.0W$ $0.9D \pm 1.0W$ $1.2D + 0.4L \pm 1.0W$	(AS/NZS 1170.0, 4.2.2(d)) (AS/NZS 1170.0, 4.2.2(e)) (AS/NZS 1170.0, 4.2.2(d))
$1.0D \pm 1.0E$ $1.0D + 0.4L \pm 1.0E$	(AS/NZS 1170.0, 4.2.2(f)) (AS/NZS 1170.0, 4.2.2(f))

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Note that the 0.4 factor on the live load in three of the combinations is not valid for live load representing storage areas. These are also the default design load combinations in ETABS whenever the NZS 3101-06 code is used. If roof live load is treated separately or if other types of loads are present, other appropriate load combinations should be used.

15.3 Limits on Material Strength

The upper and lower limits of f'_c shall be as follows:

 $25 \le f'_c \le 100 \,\mathrm{MPa}$ (NZS 5.2.1)

The lower characteristic yield strength of longitudinal reinforcement, f_y , should be equal to or less than 500 MPa for all frames (NZS 5.3.3). The lower characteristic yield strength of transverse (stirrup) reinforcement, f_{yt} , should not be greater than 500 MPa for shear or 800 MPa for confinement (NZS 5.3.3).

The code allows use of f'_c and f_y beyond the given limits, provided special study is conducted (NZS 5.2.1).

ETABS enforces the upper material strength limits for flexure and shear design of slabs. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. The user is responsible for ensuring that the minimum strength is satisfied.

15.4 Strength Reduction Factors

The strength reduction factors, ϕ , are applied to the specified strength to obtain the design strength provided by a member. The ϕ factors for flexure, shear, and torsion are as follows:

$\phi_b = 0.85$ for flexure	(NZS)	2.3.2.2)

$\phi_s = 0.75$ for shear and torsion ((NZS	2.3	3.2	2	2)
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These values can be overwritten; however, caution is advised.

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15.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

Design flexural reinforcement

Design shear reinforcement

Punching check

15.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

Determine factored axial loads and moments for each slab strip.

Design flexural reinforcement for the strip.

These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

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15.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

15.5.3.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding the compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 15-1 (NZS 7.4.2.7). Furthermore, it is assumed that the compression carried by the concrete is 0.75 times that which can be carried at the balanced condition (NZS 9.3.8.1). When the applied moment exceeds the moment capacity at the balanced condition, the area of compression reinforcement is calculated assuming that the additional moment will be carried by compression reinforcement and additional tension reinforcement.



Figure 15-1 Uniform Thickness Slab Design

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed ($0.1 f'_c A_g$), axial force is ignored; hence, all slabs are designed for major direction flexure, shear, and torsion only. Axial compression greater than $0.1 f'_c A_g$ and axial tensions are always included in flexural and shear design.

15.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive M^* (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 15-1), where,

$$a = d - \sqrt{d^2 - \frac{2|M^*|}{\alpha_1 f'_c \phi_b b}}$$
 (NZS 7.4.2)

where the default value of ϕ_b is 0.85 (NZS 2.3.2.2) in the preceding and following equations. The factor α_1 is calculated as follows (NZS 7.4.2.7):

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$$\alpha_1 = 0.85$$
 for $f'_c \le 55$ MPa
 $\alpha_1 = 0.85 - 0.004(f'_c - 55)$ for $f'_c \ge 55$ MPa, $0.75 \le \alpha_1 \le 0.85$

The value β_1 and c_b are calculated as follows:

$$\beta_1 = 0.85 \quad \text{for } f'_c \le 30,$$
 (NZS 7.4.2.7)

$$\beta_1 = 0.85 - 0.008(f'_c - 30), \quad 0.65 \le \beta_1 \le 0.85$$
 (NZS 7.4.2.7)

$$c_b = \frac{\varepsilon_c}{\varepsilon_c + f_y / E_s} d \tag{NZS 7.4.2.8}$$

The maximum allowed depth of the rectangular compression bloack, a_{max} , is given by:

$$a_{\max} = 0.75 \beta_l c_b$$
 (NZS 7.4.2.7, 9.3.8.1)

If $a \le a_{\text{max}}$ (NZS 9.3.8.1), the area of tension reinforcement is given by:

$$A_{s} = \frac{M^{*}}{\phi_{b} f_{y} \left(d - \frac{a}{2} \right)}$$

The reinforcement is to be placed at the bottom if M^* is positive, or at the top if M^* is negative.

• If $a > a_{\text{max}}$ (NZS 9.3.8.1), compression reinforcement is required (NZS 7.4.2.9) and is calculated as follows:

The compressive force developed in the concrete alone is given by:

$$C = \alpha_1 f'_c b a_{\text{max}}$$
(NZS 7.4.2.7)

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{c}^{*} = C\left(d - \frac{a_{max}}{2}\right)\phi_{b}$$

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Therefore the moment required to be resisted by compression reinforcement and tension reinforcement is:

 $M^*_{s} = M^* - M^*_{c}$

The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{s}^{*}}{\left(f'_{s} - \alpha_{1}f'_{c}\right)\left(d - d'\right)\phi_{b}}, \text{ where}$$
$$f'_{s} = \varepsilon_{c,max}E_{s}\left[\frac{c - d'}{c}\right] \le f_{y} \qquad (\text{NZS 7.4.2.2, 7.4.2.4})$$

The required tension reinforcement for balancing the compression in the concrete is:

$$A_{sl} = \frac{M_c^*}{f_y \left(d - \frac{a_{max}}{2}\right) \phi_b}$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_s^*}{f_y(d-d')\phi_b}$$

Therefore, the total tension reinforcement, $A_s = A_{s1} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M^* is positive, and vice versa if M^* is negative.

15.5.1.2.2 Design of nonuniform thickness slab

15.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M^* (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

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15.5.1.2.2.2 Flanged Slab Section Under Positive Moment If $M^* > 0$, the depth of the compression block is given by:

$$a = d - \sqrt{d^2 - \frac{2|M^*|}{\alpha_1 f_c \phi_b b_f}}$$
 (NZS 7.4.2)

The maximum allowable depth of the rectangular compression block, a_{max} , is given by:

$$a_{\max} = 0.75\beta_l c_b \tag{NZS 7.4.2.7, 9.3.8.1}$$

If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in this case the width of the sl;ab is taken as b_f . Compression reinforcement is required when $a > a_{\text{max}}$.

If $a > h_f$, calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 15-2.



Figure 15-2 Nonuniform Thickness Slab Design

 C_f is given by:

$$C_f = \alpha_1 f'_c (b_f - b_w) h_f$$
 (NZS 7.4.2.7)

Therefore, $A_{sI} = \frac{C_f}{f_y}$ and the portion of M^* that is resisted by the flange is

given by:

$$M_f^* = C_f \left(d - \frac{d_s}{2} \right) \phi_b$$

Therefore, the balance of the moment, M^* , to be carried by the web is:

$$M_{w}^{*} = M^{*} - M_{f}^{*}$$

The web is a rectangular section with dimensions b_w and d, for which the depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_w^*}{\alpha_1 f'_c \phi_b b_w}}$$
 (NZS 7.4.2)

• If $a_1 \le a_{\text{max}}$ (NZS 9.3.8.1), the area of tension reinforcement is then given by:

$$A_{s2} = \frac{M_w^*}{\phi_b f_y \left(d - \frac{a_1}{2}\right)}, \text{ and}$$

$$A_s = A_{s1} + A_{s2}$$

This reinforcement is to be placed at the bottom of the flanged section.

• If $a_1 > a_{\text{max}}$ (NZS 9.3.8.1), compression reinforcement is required and is calculated as follows:

The compressive force in the web concrete alone is given by:

$$C_{\rm w} = \alpha_1 f_c' b_{\rm w} a_{\rm max} \tag{NZS 7.4.2.7}$$

and the moment resisted by the concrete web and tension reinforcement is:

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$$M_c^* = C_w \left(d - \frac{a_{\max}}{2} \right) \phi_b$$

The moment resisted by compression and tension reinforcement is:

$$M^*_{s} = M^*_{w} - M^*_{c}$$

Therefore, the compression reinforcement is computed as:

$$A'_{s} = \frac{M^{*}_{s}}{\left(f'_{s} - \alpha_{1}f'_{c}\right)\left(d - d'\right)\phi_{b}}, \text{ where}$$
$$f'_{s} = \varepsilon_{c,\max}E_{s}\left[\frac{c - d'}{c}\right] \le f_{y} \qquad (\text{NZS 7.4.2.2, 7.4.2.4})$$

The tension reinforcement for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_c^*}{f_y \left(d - \frac{a_{\max}}{2}\right) \phi_b}$$

and the tension reinforcement for balancing the compression reinforcement is:

$$A_{s3} = \frac{M_s^*}{f_y(d-d')\phi_b}$$

Total tension reinforcement is $A_s = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom, and A'_s is to be placed at the top.

15.5.3.2 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limit (NZS 12.5.6.2, 8.8, 2.4.4):

$$A_{s} \geq \begin{cases} \frac{0.7}{f_{y}} bh & f_{y} < 500 \text{ MPa} \\ 0.0014bh & f_{y} \ge 500 \text{ MPa} \end{cases}$$
 (NZS 12.5.6.2, 8.8.1)

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In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

The slab reinforcement requirements reported by the program do not consider crack control. Any minimum requirements to satisfy crack limitations must be investigated independently of the program by the user.

15.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V^* .
- Determine the shear force, V_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

15.5.3.2 Determine Shear Force and Moment

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular slab section are obtained by factoring the corresponding shear forces for different load cases with the corresponding load combination factors.

15.5.3.2 Determine Concrete Shear Capacity

The shear force carried by the concrete, V_c , is calculated as:

$$V_c = v_c A_{cv}$$
 (NZS 9.3.9.3.4)

The allowable shear stress capacity is given by:

$$v_c = k_d k_a k_n v_b \tag{NZS 9.3.9.3.4}$$

The basic shear strength for a rectangular section is computed as,

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$$v_b = \left[0.07 + 10 \frac{A_s}{b_w d} \right] \lambda \sqrt{f'_c} , \text{ where} \qquad (\text{NZS } 9.3.9.3.4)$$

$$f'_c \le 50$$
 MPa, and (NZS 9.3.9.3.4)

$$0.08 \lambda \sqrt{f'_c} \le v_b \le 0.2 \lambda \sqrt{f'_c}$$
 (NZS 9.3.9.3.4)

where

$$\lambda = \begin{cases} 1.0, & \text{normal concrete} \\ 0.85, & \text{sand light-weight concrete} \\ 0.75, & \text{all light-weight concrete} \end{cases}$$
(NZS 9.3.9.3.5)

The factor k_a allows for the influence of maximum aggregate size on shear strength. For concrete with a maximum aggregate size of 20 mm or more, k_a shall be taken as 1.0. For concrete where the maximum aggregate size is 10 mm or less, the value of k_a shall be taken as 0.85. Interpolation is used between these limits. The program default for k_a is 1.0.

$$k_{a} = \begin{cases} 0.85, & a_{g} \le 10 \,\mathrm{mm} \\ 0.85 + 0.15 \left(\frac{a_{g} - 10}{20}\right), & a_{g} < 20 \,\mathrm{mm} \\ 1.00, & a_{g} \ge 20 \,\mathrm{mm} \end{cases}$$
(NZS 9.3.9.3.4)

The factor k_d allows for the influence of member depth on strength and it shall be calculated from the following conditions:

For members with shear reinforcement equal to or greater than the nominal shear reinforcement given in NZS 9.3.9.4.15, $k_d = 1.0$

For members with an effective depth equal to or smaller than 400 mm, $k_d = 1.0$ (NZS 9.3.9.3.4)

For members with an effective depth greater than 400, $k_d = (400/d)^{0.25}$ where *d* is in mm (NZS 9.3.9.3.4)

The factor k_n allows for the influence of axial loading (NZS 10.3.10.3.1).

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$$k_{n} = \begin{cases} 1, & N^{*} = 0\\ 1 + 3\left(\frac{N^{*}}{A_{g}f_{c}^{'}}\right), & N^{*} > 0\\ 1 + 12\left(\frac{N^{*}}{A_{g}f_{c}^{'}}\right), & N^{*} < 0 \end{cases}$$
(NZS 10.3.10.3.1)

15.5.3.2 Determine Required Shear Reinforcement

The average shear stress is computed for rectangular and flanged sections as:

$$v^* = \frac{V}{b_w d} \tag{NZS 7.5.1}$$

The average shear stress is limited to a maximum of,

$$v_{\text{max}} = \min\{0.2f'_{c}, 8 \text{ MPa}\}$$
 (NZS 7.5.2, 9.3.9.3.3)

The shear reinforcement is computed as follows:

• If $v^* \le \phi_s (v_c/2)$ or $h \le \max(300 \text{ mm}, 0.5b_w)$, $\frac{A_v}{s} = 0$ (NZS 9.3.9.4.13) • If $\phi_s (v_c/2) < v^* \le \phi_s v_c$, $\frac{A_v}{s} = \frac{1}{16} \sqrt{f'_c} \frac{b_w}{f_{yt}}$ (NZS 7.5.10, 9.3.9.4.15) • If $\phi_s v_c < v^* \le \phi_s v_{max}$, (NZS 9.3.9.4.2) $\frac{A_v}{s} = \frac{(v^* - \phi_s v_c)}{\phi_s f_{yt} d}$

• If
$$v^* > v_{\text{max}}$$
, a failure condition is declared. (NZS 7.5.2, 9.3.9.3.3)

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If the slab depth *h* is less than the minimum of 300 mm and $0.5b_w$, no shear reinforcement is required (NZS 9.3.9.4.13).

The maximum of all of the calculated A_{ν}/s values, obtained from each load combination, is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

15.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the *Key Features and Terminology* manual. Only the code-specific items are described in the following.

15.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (NZS 12.7.1(b)). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (NZS 12.7.1(b)). Figure 15-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 15-3 Punching Shear Perimeters

15.5.3.2 Transfer of Unbalanced Moment

The fraction of unbalanced moment transferred by flexure is taken to be $\gamma_f M^*$ and the fraction of unbalanced moment transferred by eccentricity of shear is taken to be $\gamma_v M^*$, where

$$\gamma_{f} = \frac{1}{1 + (2/3)\sqrt{b_{1}/b_{2}}}$$
(NZS 12.7.7.2)

$$\gamma_{\nu} = 1 - \frac{1}{1 + (2/3)\sqrt{b_{1}/b_{2}}}$$
(NZS 12.7.7.1)

where b_1 is the width of the critical section measured in the direction of the span and b_2 is the width of the critical section measured in the direction perpendicular to the span.

15.5.3.3 Determination of Concrete Capacity

The concrete punching shear factored strength is taken as the minimum of the following three limits:

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$$v_{c} = \min \begin{cases} \frac{1}{6} \left(1 + \frac{2}{\beta_{c}}\right) \sqrt{f'_{c}} \\ \frac{1}{6} \left(1 + \frac{\alpha_{s}d}{b_{0}}\right) \sqrt{f'_{c}} \\ \frac{1}{3} \sqrt{f'_{c}} \end{cases}$$
(NZS 12.7.3.2)

where, β_c is the ratio of the maximum to the minimum dimension of the critical section (NZS 12.1, 12.7.3.2(a)), b_0 is the perimeter of the critical section, and α_s is a scale factor based on the location of the critical section.

$$\alpha_s = \begin{cases} 20 & \text{for interior columns,} \\ 15 & \text{for edge columns,} \\ 10 & \text{for corner columns.} \end{cases}$$
(NZS 12.7.3.2(b))

A limit is imposed on the value of $\sqrt{f'_c}$ as follows:

$$\lambda \sqrt{f'_c} \le \sqrt{100}$$
 (NZS 9.3.9.3.5(6))

15.5.3.4 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section.

$$v^{*} = \frac{V^{*}}{bod} + \frac{\gamma v_{2}[M_{2}^{*} - V^{*}(y_{3} - y_{1})][I_{33}(y_{4} - y_{3}) - I_{23}(x_{4} - x_{3})]}{I_{22}I_{33} - I_{23}^{2}} - \frac{\gamma v_{3}[M_{3}^{*} - V^{*}(x_{3} - x_{1})][I_{22}(x_{4} - x_{3}) - I_{23}(y_{4} - y_{3})]}{I_{22}I_{33} - I_{23}^{2}}$$
Eq. 1

$$I_{22} = \sum_{sides=1}^{n} \overline{I}_{22}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 2

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$$I_{33} = \sum_{sides=1}^{n} \overline{I}_{33}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 3

$$I_{23} = \sum_{sides=1}^{n} \overline{I}_{23}$$
, where "*sides*" refers to the sides of the critical section for punching shear Eq. 4

The equations for \overline{I}_{22} , \overline{I}_{33} , and \overline{I}_{23} are different depending on whether the side of the critical section for punching shear being considered is parallel to the 2-axis or parallel to the 3-axis. Refer to Figures 15-4.

$$\overline{I}_{22} = Ld(y_2 - y_3)^2$$
, for side of critical section parallel to 2-axis Eq. 5a

$$\overline{I}_{22} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(y_2 - y_3)^2$$
, for the side of the critical section parallel to the 3-axis Eq. 5b

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$$\overline{I}_{33} = \frac{Ld^3}{12} + \frac{dL^3}{12} + Ld(x_2 - y_3)^2$$
, for the side of the critical section parallel to the 2-axis Eq. 6

$$I_{33} = Ld(x_2 - x_3)^2$$
, for the side of the critical section
parallel to the 3-axis Eq. 6b

$$I_{23} = Ld(x_2 - x_3)(y_2 - y_3)$$
, for the side of the critical section
parallel to the 2-axis or 3-axis Eq. 7

NOTE: \overline{I}_{23} is explicitly set to zero for corner condition.

where,

- b_0 = Perimeter of critical section for punching shear
- d = Effective depth at critical section for punching shear based on average of d for 2 direction and d for 3 direction
- I_{22} = Moment of inertia of critical section for punching shear about an axis that is parallel to the local 2-axis
- I_{33} = Moment of inertia of critical section for punching shear about an axis that is parallel to the local 3-axis
- I_{23} = Product of inertia of critical section for punching shear with respect to the 2 and 3 planes
- *L* = Length of the side of the critical section for punching shear currently being considered
- M_2^* = Moment about line parallel to 2-axis at center of column (positive per right-hand rule)
- M_3^* = Moment about line parallel to 3-axis at center of column (positive per right-hand rule)
- V^* = Punching shear stress
- V^* = Shear at center of column (positive upward)
- x_1, y_1 = Coordinates of column centroid
- x_2 , y_2 = Coordinates of center of one side of critical section for punching shear
- x_3, y_3 = Coordinates of centroid of critical section for punching shear
- x_4 , y_4 = Coordinates of location where you are calculating stress
- γ_{V2} = Percent of M_{U2} resisted by shear
- γ_{V3} = Percent of M_{U3} resisted by shear

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15.5.3.5 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

15.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 150 mm, and not less than 16 times the shear reinforcement bar diameter (NZS 12.7.4.1). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is performed as described in the subsections that follow.

15.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is determined as:

$$v_c = \frac{1}{6}\sqrt{f'_c}$$
 (NZS 12.7.3.5)

15.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$v_{\rm max} = 0.5 \sqrt{f_c'}$$
 (NZS 12.7.3.4)

Given v^* , v_c , and v_{max} , the required shear reinforcement is calculated as follows, where, ϕ , is the strength reduction factor.

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$$\frac{A_{v}}{s} = \frac{(v_{n} - v_{c})}{\phi f_{vv} d}$$
(NZS 12.7.4.2(a))

Minimum punching shear reinforcement should be provided such that:

$$V_s \ge \frac{1}{16} \sqrt{f'_c} b_o d$$
 (NZS 12.7.4.3)

- If $v_n > \phi v_{\text{max}}$, a failure condition is declared. (NZS 12.7.3.4)
- If v_n exceeds the maximum permitted value of ϕv_{max} , the concrete section should be increased in size.

15.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 15-5 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 15-5 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the

first line (perimeter) of shear reinforcement shall not exceed 2d measured in a direction parallel to the column face (NZS 12.7.4.4).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

15.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in NZS 3.11 plus half of the diameter of the flexural reinforcement.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d* and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$s_o \leq 0.5d$	(NZS 12.7.4.4)
$s \leq 0.5d$	(NZS 12.7.4.4)
$g \leq 2d$	(NZS 12.7.4.4)

Chapter 16 Design for Singapore CP 65-99

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the Singapore standard, Structural Use of Concrete code CP 65-99 [CP 99], is selected. The program also includes the recommendations of BC 2:2008 Design Guide of High Strength Concrete to Singapore Standard CP65 [BC 2008]. Various notations used in this chapter are listed in Table 16-1. For referencing to the pertinent sections of the Singapore code in this chapter, a prefix "CP" followed by the section number is used.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

16.1 Notations

Table 16-1 List of Symbols Used in the CP 65-99 Code

 A_g Gross area of cross-section, mm²

A_l	Area of longitudinal reinforcement for torsion, mm ²
A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²
A_{sv}	Total cross-sectional area of links at the neutral axis, mm ²
A_{sv}/s_v	Area of shear reinforcement per unit length of the member, mm ² /mm
a	Depth of compression block, mm
b	Width or effective width of the section in the compression zone, mm
b_f	Width or effective width of flange, mm
b_w	Average web width of a flanged section, mm
С	Torsional constant, mm ⁴
d	Effective depth of tension reinforcement, mm
d'	Depth to center of compression reinforcement, mm
E_c	Modulus of elasticity of concrete, MPa
E_s	Modulus of elasticity of reinforcement, assumed as 200,000 MPa
f	Punching shear factor considering column location
fcu	Characteristic cube strength, MPa
f'_s	Stress in the compression reinforcement, MPa
f_y	Characteristic strength of reinforcement, MPa
f_{yv}	Characteristic strength of shear reinforcement, MPa (< 460 MPa)
h	Overall depth of a section in the plane of bending, mm
h_{f}	Flange thickness, mm
h_{\min}	Smaller dimension of a rectangular section, mm
h_{\max}	Larger dimension of a rectangular section, mm
Κ	Normalized design moment, $M_u/bd^2 f_{cu}$
<i>K</i> ′	Maximum $\frac{M_u}{L d^2 f}$ for a singly reinforced concrete section

Table 16-1 List of Symbols Used in the CP 65-99 Code

K' Maximum
$$\frac{M_u}{bd^2 f_{cu}}$$
 for a singly reinforced concrete section

16 - 2 Notations

Table 16-1 List of Symbols Used in the CP 65-99 Code				
k_1	Shear strength enhancement factor for support compression			
k_2	Concrete shear strength factor, $[f_{cu}/30]^{\frac{1}{3}}$			
M	Design moment at a section, N-mm			
$M_{ m single}$	Limiting moment capacity as singly reinforced section, N-mm			
S_{V}	Spacing of the links along the strip, mm			
Т	Design torsion at ultimate design load, N-mm			
и	Perimeter of the punching critical section, mm			
V	Design shear force at ultimate design load, N			
v	Design shear stress at a slab cross-section or at a punching critical section, MPa			
v_c	Design concrete shear stress capacity, MPa			
$v_{\rm max}$	Maximum permitted design factored shear stress, MPa			
v_t	Torsional shear stress, MPa			
x	Neutral axis depth, mm			
x_{bal}	Depth of neutral axis in a balanced section, mm			
Z.	Lever arm, mm			
β	Torsional stiffness constant			
eta_b	Moment redistribution factor in a member			
γf	Partial safety factor for load			
γ_m	Partial safety factor for material strength			
\mathcal{E}_{c}	Maximum concrete strain			
\mathcal{E}_{s}	Strain in tension reinforcement			
\mathcal{E}'_s	Strain in compression reinforcement			

Table 16.1 List of Symbols Lload in the CD 65.00 Cod

16.2 Design Load Combinations

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. The design load combinations are obtained by multiplying the characteristic loads by appropriate partial factors of safety, γ_f (CP 2.4.1.3). If a structures is subjected to dead (D), live (L), pattern live (PL), and wind (W) loads, and considering that wind forces are reversible, the following load combinations may need to be considered (CP 2.4.3).

1.4D 1.4D + 1.6L	(CP 2.4.3)
1.4D + 1.6(0.75PL)	(CP 2.4.3)
$1.0D \pm 1.4W$ $1.4D \pm 1.4W$ $1.2D + 1.2L \pm 1.2W$	(CP 2.4.3)

These are also the default design load combinations in ETABS whenever the CP 65-99 code is used. If roof live load is treated separately or other types of loads are present, other appropriate load combinations should be used. Note that the automatic combination, including pattern live load, is assumed and should be reviewed before using for design.

16.3 Limits on Material Strength

The concrete compressive strength, f_{cu} , should not be less than 30 MPa (CP 3.1.7.2).

The program does not enforce this limit for flexure and shear design of slabs. The input material strengths are used for design even if they are outside of the limits. It is the user's responsible to use the proper strength values while defining the materials.

16.4 Partial Safety Factors

The design strengths for concrete and reinforcement are obtained by dividing the characteristic strength of the material by a partial safety factor, γ_m . The

16 - 4 Design Load Combinations

values of γ_m used in the program are listed in the table that follows and are taken from CP Table 2.2 (CP 2.4.4.1):

Values of γ_m for the Ultimate Limit State	
Reinforcement	1.15
Concrete in flexure and axial load	1.50
Concrete shear strength without shear reinforcement	1.25

These factors are incorporated into the design equations and tables in the code, but can be overwritten.

16.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

- Design flexural reinforcement
- Design shear reinforcement
- Punching check

16.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element

boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

16.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

16.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding the compression reinforcement by increasing the effective depth, the width, or the strength of the concrete.

The design procedure is based on the simplified rectangular stress block shown in Figure 16-1 (CP 3.4.4.4), where ε_c is defined as:

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$$\varepsilon_{c} = \begin{cases} 0.0035 & \text{if } f_{cu} \le 60 \text{MPa} \\ 0.0035 - \frac{(f_{cu} - 60)}{50000} & \text{if } f_{cu} > 60 \text{MPa} \end{cases}$$
(CP 2.5.3, BC 2.2)

Furthermore, it is assumed that moment redistribution in the member does not exceed 10% (i.e., $\beta_b \ge 0.9$; CP 3.4.4.4). The code also places a limitation on the neutral axis depth,

$$\frac{x}{d} \le \begin{cases} 0.5 & \text{for} & f_{cu} \le 60 \,\text{N/mm}^2 \\ 0.4 & \text{for} & 60 < f_{cu} \le 75 \,\text{N/mm}^2 \\ 0.33 & \text{for} & 75 < f_{cu} \le 105 \,\text{N/mm}^2 \end{cases}$$
(CP 3.4.4.4, BC 2.2)

to safeguard against non-ductile failures (CP 3.4.4.4). In addition, the area of compression reinforcement is calculated assuming that the neutral axis depth remains at the maximum permitted value.

The depth of the compression block is given by:

$$a = \begin{cases} 0.9x & \text{for} & f_{cu} \le 60 \text{ N/mm}^2 \\ 0.8x & \text{for} & 60 < f_{cu} \le 75 \text{ N/mm}^2 \\ 0.72x & \text{for} & 75 < f_{cu} \le 105 \text{ N/mm}^2 \end{cases}$$
(CP 3.4.4.4, BC 2.2)

The design procedure used by ETABS, for both rectangular and flanged sections (L- and T-shaped sections), is summarized in the text that follows. For reinforced concrete design where design ultimate axial compression load does not exceed $(0.1f_{cu}A_g)$ (CP 3.4.4.1), axial force is ignored; hence, all slabs are designed for major direction flexure and shear only. Axial compression greater than $0.1f_{cu}A_g$ and axial tensions are always included in flexural and shear design.

16.5.1.2.1 Design of uniform thickness slab

For uniform thickness slab, the limiting moment capacity as a singly reinforced slab, M_{single} , is first calculated for a section. The reinforcement is determined based on whether *M* is greater than, less than, or equal to M_{single} . See Figure 16-1.

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Calculate the ultimate limiting moment of resistance of the section as singly reinforced.



Figure 16-1 Uniform Thickness Slab Design

 $K' = \begin{cases} 0.156 \text{ for } f_{cu} \le 60 \text{ N/mm}^2 \\ 0.120 \text{ for } 60 < f_{cu} \le 75 \text{N/mm}^2 \\ 0.094 \text{ for } 75 < f_{cu} \le 105 \text{N/mm}^2 \text{ and no moment redistribution.} \end{cases}$

• If $M \le M_{\text{single}}$, the area of tension reinforcement, A_s , is given by:

$$A_s = \frac{M}{0.87 f_y z}$$
, where (CP 3.4.4.4)

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$$z = d \left(0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right) \le 0.95d \tag{CP 3.4.4.4}$$

$$K = \frac{M}{f_{cu}bd^2}$$
 (CP 3.4.4.4)

This reinforcement is to be placed at the bottom if M is positive, or at the top if M is negative.

• If $M > M_{\text{single}}$, compression reinforcement is required and calculated as follows:

$$A'_{s} = \frac{M - M_{\text{single}}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{m}}\right)(d - d')}$$
(CP 3.4.4.4)

where d' is the depth of the compression reinforcement from the concrete compression face, and

$$f'_{s} = 0.87 f_{y} \qquad \text{if } \frac{d'}{d} \le \frac{1}{2} \left[1 - \frac{f_{y}}{800} \right] \quad (\text{CP 3.4.4.1, 2.5.3, Fig 2.2})$$

$$f'_{s} = E_{s} \varepsilon_{c} \left[1 - \frac{2d'}{d} \right] \text{if } \frac{d'}{d} > \frac{1}{2} \left[1 - \frac{f_{y}}{800} \right] \quad (\text{CP 3.4.4.4, 2.5.3, Fig 2.2})$$

The tension reinforcement required for balancing the compression in the concrete and the compression reinforcement is calculated as:

$$A_{s} = \frac{M_{\text{single}}}{0.87 f_{y} z} + \frac{M - M_{\text{single}}}{0.87 f_{y} (d - d')}, \text{ where}$$
(CP 3.4.4.4)

$$z = d \left(0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right) \le 0.95d \tag{CP 3.4.4.4}$$

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16.5.1.2.2 Design of nonuniform thickness slab

16.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

16.5.1.2.2.2 Flanged Slab Section Under Positive Moment

With the flange in compression, the program analyzes the section by considering alternative locations of the neutral axis. Initially the neutral axis is assumed to be located in the flange. On the basis of this assumption, the program calculates the exact depth of the neutral axis. If the stress block does not extend beyond the flange thickness, the section is designed as a uniform thickness slab of width b_{f} . If the stress block extends beyond the flange width, the contribution of the web to the flexural strength of the slab is taken into account. See Figure 16-2.



Figure 16-2 Nonuniform Thickness Slab Design

Assuming the neutral axis to lie in the flange, the normalized moment is given by:

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$$K = \frac{M}{f_{cu} b_f d^2}$$
(CP 3.4.4.4)

Then the moment arm is computed as:

$$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right\} \le 0.95d$$
 (CP 3.4.4.4)

the depth of neutral axis is computed as:

$$x = \begin{cases} \frac{d-z}{0.45}, & \text{for} & f_{cu} \le 60 \,\text{N/mm}^2 \\ \frac{d-z}{0.40}, & \text{for} & 60 < f_{cu} \le 75 \,\text{N/mm}^2 \\ \frac{d-z}{0.36}, & \text{for} & 75 < f_{cu} \le 105 \,\text{N/mm}^2 \end{cases}$$
(CP 3.4.4.4, BC 2.2, Fig 2.3)

and the depth of the compression block is given by:

$$a = \begin{cases} 0.9x & \text{for} & f_{cu} \le 60 \text{ N/mm}^2 \\ 0.8x & \text{for} & 60 < f_{cu} \le 75 \text{ N/mm}^2 \\ 0.72x & \text{for} & 75 < f_{cu} \le 105 \text{ N/mm}^2 \end{cases}$$
(CP 3.4.4.4, BC 2.2, Fig 2.3)

- If $a \le h_f$, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab design. However, in this case the width of the slab is taken as b_f . Compression reinforcement is required when K > K'.
- If $a > h_{f}$,

If $M \leq \beta_f f_{cu} b d^2$ and $h_f \leq 0.45 d$ then,

$$A_{s} = \frac{M + 0.1 f_{cu} b d (0.45d - h_{f})}{0.87 f_{y} (d - 0.5h_{f})}, \text{ where}$$
(BS 3.4.4.5)

$$\beta_f = 0.45 \frac{h_f}{d} \left(1 - \frac{b_w}{b} \right) \left(1 - \frac{h_f}{2d} \right) + 0.15 \frac{b_w}{b}$$
(BS 3.4.4.5)

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Otherwise the calculation for A_s has two parts. The first part is for balancing the compressive force from the flange, C_f , and the second part is for balancing the compressive force from the web, C_w , as shown in Figure 16-2.

In that case, the ultimate resistance moment of the flange is given by:

$$M_f = 0.45 f_{cu} (b_f - b_w) h_f (d - 0.5 h_f)$$
(CP 3.4.4.5)

The moment taken by the web is computed as:

$$M_{w} = M - M_{f}$$

and the normalized moment resisted by the web is given by:

$$K_w = \frac{M_w}{f_{cu} b_w d^2}$$
(CP 3.4.4.4)

If K_w ≤ 0.156 (CP 3.4.4.4), the slab is designed as a singly reinforced concrete slab. The reinforcement is calculated as the sum of two parts, one to balance compression in the flange and one to balance compression in the web.

$$A_{s} = \frac{M_{f}}{0.87 f_{y} (d - 0.5 h_{f})} + \frac{M_{w}}{0.87 f_{y} z}, \text{ where}$$
$$z = d \left(0.5 + \sqrt{0.25 - \frac{K_{w}}{0.9}} \right) \le 0.95 d$$

If K_w > K' (CP 3.4.4.4), compression reinforcement is required and is calculated as follows:

The ultimate moment of resistance of the web only is given by:

$$M_{uw} = K' f_{cu} b_w d^2$$
(CP 3.4.4.4)

The compression reinforcement is required to resist a moment of magnitude $M_w - M_{uw}$. The compression reinforcement is computed as:

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$$A'_{s} = \frac{M_{w} - M_{uw}}{\left(f'_{s} - \frac{0.67f_{cu}}{\gamma_{m}}\right)\left(d - d'\right)}$$

where, d' is the depth of the compression reinforcement from the concrete compression face, and

$$f'_{s} = 0.87 f_{y} \qquad \text{if } \frac{d'}{d} \le \frac{1}{2} \left[1 - \frac{f_{y}}{800} \right] \quad (\text{CP 3.4.4.4, 2.5.3, Fig 2.2})$$

$$f'_{s} = E_{s} \varepsilon_{c} \left[1 - \frac{2d'}{d} \right] \text{ if } \frac{d'}{d} > \frac{1}{2} \left[1 - \frac{f_{y}}{800} \right] \quad (\text{CP 3.4.4.4, 2.5.3, Fig 2.2})$$

The area of tension reinforcement is obtained from equilibrium as:

$$A_{s} = \frac{1}{0.87 f_{y}} \left[\frac{M_{f}}{d - 0.5h_{f}} + \frac{M_{uw}}{z} + \frac{M_{w} - M_{uw}}{d - d'} \right]$$
$$z = d \left(0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right) \le 0.95d$$

16.5.1.3 Minimum and Maximum Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limit (CP 3.12.5.3, CP Table 3.25) with interpolation for reinforcement of intermediate strength:

$$A_{s} \geq \begin{cases} 0.0024bh & \text{if } f_{y} = 250 \text{ MPa} \\ 0.0013bh & \text{if } f_{y} = 460 \text{ MPa} \end{cases}$$
(CP 3.12.5.3)

For $f_{cu} > 40$ N/mm², the preceding minimum reinforcement shall be multiplied by $(f_{cu}/40)^{2/3}$.

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area (CP 3.12.6.1).

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16.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved (CP 3.4.5):

- Determine the shear stress, *v*.
- Determine the shear stress, v_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

16.5.2.1 Determine Shear Stress

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular strip station are obtained by factoring the corresponding shear forces for different load cases with the corresponding load combination factors. The shear stress is then calculated as:

$$v = \frac{V}{b_w d} \tag{CP 3.4.5.2}$$

The maximum allowable shear stress, v_{max} is defined as:

$$v_{\text{max}} = \min(0.8\sqrt{f_{cu}}, 7 \text{ MPa}).$$
 (CP 3.4.5.2)

For light-weight concrete, v_{max} is defined as:

$$v_{\rm max} = \min(0.63 \sqrt{f_{cu}}, 4 \text{ MPa})$$
 (CP Part 2 5.4)

16.5.2.2 Determine Concrete Shear Capacity

The shear stress carried by the concrete, v_c , is calculated as:

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$$v'_{c} = v_{c} + 0.6 \frac{NVh}{A_{c}M} \le v_{c} \sqrt{1 + \frac{N}{A_{c}v_{c}}}$$
 (CP 3.4.5.12)
 $0.84k_{1}k_{2} (100A_{s})^{\frac{1}{3}} (400)^{\frac{1}{4}}$ (CP 3.4.5.4 Texts 2.0)

$$v_c = \frac{0.84k_1k_2}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{/3} \left(\frac{400}{d}\right)^{/4}$$
(CP 3.4.5.4, Table 3.9)

$$k_1$$
 is the enhancement factor for support compression,

and is conservatively taken as 1 (CP 3.4.5.8)

$$k_2 = \left(\frac{f_{cu}}{30}\right)^{\frac{1}{3}}, 1 \le k_2 \le \left(\frac{80}{30}\right)^{\frac{1}{3}}$$
 (CP 3.4.5.4)

$$\gamma_m = 1.25$$
 (CP 2.4.4.1)

However, the following limitations also apply:

$$0.15 \le \frac{100 A_s}{bd} \le 3$$
 (CP 3.4.5.4, Table 3.9)

$$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge 0.67 \text{ (unreinforced) or } \ge 1 \text{ (reinforced)(CP 3.4.5.4, Table 3.9)}$$

 $f_{cu} \le 80$ MPa (for calculation purpose only) (CP 3.4.5.4, Table 3.9)

$$\frac{Vh}{M} \le 1$$
 (CP 3.4.5.12)

 A_s is the area of tension reinforcement

16.5.2.3 Determine Required Shear Reinforcement

Given v, v'_c , and v_{max} , the required shear reinforcement is calculated as follows (CP Table 3.8, CP 3.4.5.3):

 Calculate the design average shear stress that can be carried by minimum shear reinforcement, v_r, as:

•
$$v_r = \begin{cases} 0.4 & \text{if } f_{cu} \le 40 \text{N/mm}^2 \\ 0.4 \left(\frac{f_{cu}}{40} \right)^{\frac{2}{3}} & \text{if } 40 < f_{cu} \le 80 \text{N/mm}^2 \end{cases}$$
 (CP 3.4.5.3, Table 3.8)

$$f_{cu} \le 80$$
 N/mm² (for calculation purpose only) (CP 3.4.5.3, Table 3.8)

• If
$$v \leq v'_c + v_r$$
,

$$\frac{A_s}{s_v} = \frac{v_r b}{0.87 f_{yv}},$$
 (CP 3.4.5.3, Table 3.8)

• If $v > v'_c + v_r$,

$$\frac{A_{sv}}{s_v} = \frac{(v - v'_c)b}{0.87f_{yv}}$$
 (CP 3.4.5.3, Table 3.8)

• If $v > v_{\text{max}}$, a failure condition is declared. (CP 3.4.5.2)

In the preceding expressions, a limit is imposed on the f_{yv} as

$$f_{yy} \le 460 \text{ MPa}$$
 (CP 3.4.5.1)

The maximum of all of the calculated A_{sv}/s_v values, obtained from each load combination, is reported along with the controlling shear force and associated load combination.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

16.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

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16.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of 1.5*d* from the face of the support (CP 3.7.7.4, 3.7.7.6). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (CP 3.7.7.1). Figure 16-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.

16.5.3.2 Determination of Concrete Capacity

The concrete punching shear factored strength is taken as (CP 3.7.7.4, 3.7.7.6):

$$v_c = \frac{0.84k_1k_2}{\gamma_m} \left(\frac{100A_s}{bd}\right)^{\frac{1}{3}} \left(\frac{400}{d}\right)^{\frac{1}{4}}$$
(CP 3.4.5.4, Table 3.9)

 k_1 is the enhancement factor for support compression, and is conservatively taken as 1 (CP 3.4.5.8)



Figure 16-3 Punching Shear Perimeters

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$$k_{2} = \left(\frac{f_{cu}}{30}\right)^{\frac{1}{3}} 1 \le k_{2} \le \left(\frac{80}{30}\right)^{\frac{1}{3}}$$
(CP 3.4.5.4, Table 3.9)
$$\gamma_{m} = 1.25$$
(CP 3.4.5.2)

However, the following limitations also apply:

$$0.15 \le \frac{100 A_s}{bd} \le 3$$
 (CP 3.4.5.4, Table 3.9)

$$\left(\frac{400}{d}\right)^{\frac{1}{4}} \ge 0.67 \text{ (unreinforced) or} \ge 1 \text{ (reinforced)(CP 3.4.5.4, Table 3.9)}$$

For light-weight concrete, v_{max} is defined as:

$$v \le \min(0.63 \sqrt{f_{cu}}, 4 \text{ MPa})$$
 (CP Part 2 5.4)
 $v \le \min(0.8 \sqrt{f_{cu}}, 7 \text{ MPa})$ (CP 3.4.5.2, Table 3.9)

 $f_{cu} \le 80$ MPa (for calculation purpose only) (CP 3.4.5.4, Table 3.9)

 A_s = area of tension reinforcement, which is taken as the average tension reinforcement of design strips in Layer A and layer B where Layer A and Layer design strips are in orthogonal directions. When design strips are not present in both orthogonal directions then tension reinforcement is taken as zero in the current implementation.

16.5.3.3 Determine Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the nominal design shear stress, v, is calculated as:

$$V_{eff,x} = V\left(f + \frac{1.5M_x}{V_y}\right)$$
 (CP 3.7.6.2, 3.7.6.3)

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$$V_{eff,y} = V\left(f + \frac{1.5M_y}{V_x}\right)$$
(CP 3.7.6.2, 3.7.6.3)
$$v_{max} = \max\begin{cases} \frac{V_{eff,x}}{u\,d} \\ \frac{V_{eff,y}}{u\,d} \end{cases}$$
(CP 3.7.7.3)

where,

- *u* is the perimeter of the critical section,
- *x* and *y* are the lengths of the sides of the critical section parallel to the axis of bending
- M_x and M_y are the design moments transmitted from the slab to the column at the connection
- V is the total punching shear force
- f is a factor to consider the eccentricity of punching shear force and is taken as:

$$f = \begin{cases} 1.00 & \text{for interior columns,} \\ 1.25 & \text{for edge columns, and} \\ 1.25 & \text{for corner columns.} \end{cases}$$
(CP 3.7.6.2, 3.7.6.3)

16.5.3.4 Determine Capacity Ratio

The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

16.5.4 Design Punching Shear Reinforcement

The use of shear links as shear reinforcement in slabs is permitted, provided that the effective depth of the slab is greater than or equal to 200 mm (CP 3.7.7.5). If

the slab thickness does not meet this requirement, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is completed as described in the following subsections.

16.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is as previously determined for the punching check.

16.5.4.2 Determine Required Shear Reinforcement

The shear stress is limited to a maximum of:

$$v_{\rm max} = 2v_c$$
 (CP 3.7.7.5)

Given v, v_c , and v_{max} , the required shear reinforcement is calculated as follows (CP 3.7.7.5).

• If $v \le 1.6v_c$,

$$\frac{A_{v}}{s} = \frac{\left(v - v_{c}\right)ud}{0.87 f_{yv}} \ge \frac{0.4ud}{0.87 f_{yv}},$$
(CP 3.7.7.5)

• If $1.6v_c \le v < 2.0v_c$,

$$\frac{A_{v}}{s} = \frac{5(0.7v - v_{c})ud}{0.87 f_{yv}} \ge \frac{0.4ud}{0.87 f_{yv}},$$
(CP 3.7.7.5)

• If $v > v_{\text{max}}$, a failure condition is declared. (CP 3.7.7.5)

If *v* exceeds the maximum permitted value of v_{max} , the concrete section should be increased in size.

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16.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 16-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.



Figure 16-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 1.5*d* measured in a direction parallel to the column face (CP 3.7.7.6).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

16.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in CP 3.3 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 16-, 12-, 14-, 16-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 1.5*d*. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$s_o \leq 0.5d$	(CP 3.7.7.6)
$s \leq 0.75d$	(CP 3.7.7.6)
$g \leq 1.5d$	(CP 3.7.7.6)

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Chapter 17 Design for TS 500-2000

This chapter describes in detail the various aspects of the concrete design procedure that is used by ETABS when the American code TS 500-2000 [TS 500] is selected. Various notations used in this chapter are listed in Table 17-1. For referencing to the pertinent sections or equations of the TS code in this chapter, a prefix "TS" followed by the section or equation number is used herein.

The design is based on user-specified load combinations. The program provides a set of default load combinations that should satisfy the requirements for the design of most building type structures.

English as well as SI and MKS metric units can be used for input. The code is based on Newton-millimeter-second units. For simplicity, all equations and descriptions presented in this chapter correspond to Newton-millimeter-second units unless otherwise noted.

17.1 Notations

Table 17-1 List of Symbols Used in the TS 500-2000 Code

- A_{cp} Area enclosed by the outside perimeter of the section, mm²
- A_g Gross area of concrete, mm²

A_l	Area of longitudinal reinforcement for torsion, mm ²
A_o	Area enclosed by the shear flow path, mm ²
A_{oh}	Area enclosed by the centerline of the outermost closed transverse torsional reinforcement, mm ²
A_s	Area of tension reinforcement, mm ²
A'_s	Area of compression reinforcement, mm ²
A_{ot}/s	Area of transverse torsion reinforcement (closed stirrups) per unit length of the member, mm ² /mm
A_{ov}/s	Area of transverse shear reinforcement per unit length of the member, mm ² /mm
a	Depth of compression block, mm
A_{sw}	Area of shear reinforcement, mm ²
A_{sw}/s	Area of shear reinforcement per unit length of the member, mm ² /mm
$a_{\rm max}$	Maximum allowed depth of compression block, mm
b	Width of section, mm
b_{f}	Effective width of flange (flanged section), mm
b_o	Perimeter of the punching shear critical section, mm
b_w	Width of web (flanged section), mm
b_1	Width of the punching shear critical section in the direction of bending, mm
b_2	Width of the punching shear critical section perpendicular to the di- rection of bending, mm
С	Depth to neutral axis, mm
d	Distance from compression face to tension reinforcement, mm
d'	Distance from compression face to compression reinforcement, in
E_c	Modulus of elasticity of concrete, N/mm ²

Table 17-1 List of Symbols Used in the TS 500-2000 Code

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Table 17	Table 17-1 List of Symbols Used in the TS 500-2000 Code		
E_s	Modulus of elasticity of reinforcement, N/mm ²		
f_{cd}	Designed compressive strength of concrete, N/mm ²		
f_{ck}	Characteristic compressive strength of concrete, N/mm ²		
f_{ctk}	Characteristic tensile strength of concrete, N/mm ²		
f_{yd}	Designed yield stress of flexural reinforcement, N/mm ² .		
f_{yk}	Characteristic yield stress of flexural reinforcement, N/mm ² .		
f_{ywd}	Designed yield stress of transverse reinforcement, N/mm ² .		
h	Overall depth of a section, mm		
h_{f}	Height of the flange, mm		
M_d	Design moment at a section, N/mm		
N_d	Design axial load at a section, N		
p_{cp}	Outside perimeter of concrete cross-section, mm		
p_h	Perimeter of centerline of outermost closed transverse torsional reinforcement, mm		
S	Spacing of shear reinforcement along the strip, mm		
T_{cr}	Critical torsion capacity, N/mm		
T_d	Design torsional moment at a section, N/mm		
V_c	Shear force resisted by concrete, N		
$V_{\rm max}$	Maximum permitted total factored shear force at a section, N		
V_s	Shear force resisted by transverse reinforcement, N		
V_d	Design shear force at a section, N		
α_s	Punching shear scale factor based on column location		
eta_c	Ratio of the maximum to the minimum dimensions of the punching shear critical section		
k_1	Factor for obtaining depth of the concrete compression block		

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Table 17-1 List of Symbols Used in the TS 500-2000 Code			
\mathcal{E}_{c}	Strain in the concrete		
$\mathcal{E}_{c \max}$	Maximum usable compression strain allowed in the extreme concrete fiber, (0.003 mm / mm)		
Es	Strain in the reinforcement		
<i>Е</i> си,	Maximum usable compression strain allowed in extreme concrete fiber (0.003 mm/mm)		
\mathcal{E}_s	Strain in reinforcing steel		
γm	Material factor		
γ _{mc}	Material factor for concrete		
λ	Shear strength reduction factor for light-weight concrete		

17.2 **Design Load Combinations**

The design load combinations are the various combinations of the load cases for which the structure needs to be designed. For TS 500-2000, if a structure is subjected to dead (G), live (Q), wind (W), and earthquake (E) loads, and considering that wind and earthquake forces are reversible, the following load combinations may need to be considered (TS 6.2.6):

1.4G + 1.6Q	(TS Eqn. 6.3)
$0.9G \pm 1.3W$	(TS Eqn. 6.6)
$1.0G + 1.3Q \pm 1.3W$	(TS Eqn. 6.5)
$0.9G \pm 1.0E$	(TS Eqn. 6.8)
$1.0G + 1.0Q \pm 1.0E$	(TS Eqn. 6.7)

These are the default design load combinations in ETABS whenever the TS 500-2000 code is used. The user should use other appropriate load combinations if roof live load is treated separately, or if other types of loads are present.

17 - 4 Design Load Combinations

17.3 Limits on Material Strength

The characteristic compressive strength of concrete, f_{ck} , should not be less than 16 N/mm². The upper limit of the reinforcement yield stress, f_y , is taken as 420 N/mm² and the upper limit of the reinforcement shear strength, f_{yk} is taken as 420 N/mm².

The program enforces the upper material strength limits for flexure and shear design of slab. The input material strengths are taken as the upper limits if they are defined in the material properties as being greater than the limits. The user is responsible for ensuring that the minimum strength is satisfied.

17.4 Design Strength

The design strength for concrete and steel is obtained by dividing the characteristic strength of the material by a partial factor of safety, γ_{mc} and γ_{ms} . The values used in the program are as follows:

Partial safety factor for steel, $\gamma_{ms} = 1.15$, and	(TS 6.2.5)
Partial safety factor for concrete, $\gamma_{mc} = 1.5$.	(TS 6.2.5)

These factors are already incorporated in the design equations and tables in the code. Although not recommended, the program allows them to be overwritten. If they are overwritten, the program uses them consistently by modifying the code-mandated equations in every relevant place.

17.5 Slab Design

ETABS slab design procedure involves defining sets of strips in two mutually perpendicular directions. The locations of the strips are usually governed by the locations of the slab supports. The axial force, moments and shears for a particular strip are recovered from the analysis (on the basis of the Wood-Armer technique), and a flexural design is carried out based on the ultimate strength design method.

The slab design procedure involves the following steps:

Design flexural reinforcement

- Design shear reinforcement
- Punching check

17.5.1 Design Flexural Reinforcement

For slabs, ETABS uses either design strips or the finite element based design to calculate the slab flexural reinforcement in accordance with the selected design code. For simplicity, only strip-by-strip design is document in the proceeding sections.

The design of the slab reinforcement for a particular strip is carried out at specific locations along the length of the strip. These locations correspond to the element boundaries. Controlling reinforcement is computed on either side of those element boundaries. The slab flexural design procedure for each load combination involves the following:

- Determine factored axial loads and moments for each slab strip.
- Design flexural reinforcement for the strip.
- These two steps, described in the text that follows, are repeated for every load combination. The maximum reinforcement calculated for the top and bottom of the slab within each design strip, along with the corresponding controlling load combination, is obtained and reported.

17.5.1.1 Determine Factored Moments

In the design of flexural reinforcement of concrete slab, the factored moments for each load combination at a particular design strip are obtained by factoring the corresponding moments for different load cases, with the corresponding load factors.

The slab is then designed for the maximum positive and maximum negative factored moments obtained from all of the load combinations. Calculation of bottom reinforcement is based on positive design strip moments. In such cases, the slab may be designed as a rectangular or flanged slab section. Calculation of top reinforcement is based on negative design strip moments. In such cases, the slab may be designed as a rectangular or inverted flanged slab section.

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17.5.1.2 Determine Required Flexural Reinforcement

In the flexural reinforcement design process, the program calculates both the tension and compression reinforcement. Compression reinforcement is added when the applied design moment exceeds the maximum moment capacity of a singly reinforced section. The user has the option of avoiding the compression reinforcement by increasing the effective depth, the width, or the grade of concrete.

The design procedure is based on the simplified rectangular stress block, as shown in Figure 17-1 (TS 7.1). When the applied moment exceeds the moment capacity at this design condition, the area of compression reinforcement is calculated on the assumption that the additional moment will be carried by compression and additional tension reinforcement.

The design procedure used by the program for both rectangular and flanged sections is summarized in the following subsections. It is assumed that the design ultimate axial force does not exceed $(0.1 f_{ck} A_g)$ (TS 7.3, Eqn. 7.2); hence, all of

the slabs are designed ignoring axial force; hence, all slabs are designed for major direction flexure and shear only. Axial compression greater than $(0.1 f_{ck} A_{p})$

and axial tensions are always included in flexural and shear design ...

17.5.1.2.1 Design of uniform thickness slab

In designing for a factored negative or positive moment, M_d (i.e., designing top or bottom reinforcement), the depth of the compression block is given by *a* (see Figure 17-1), where,

$$a = d - \sqrt{d^2 - \frac{2|M_d|}{0.85f_{cd}b}},$$
 (TS 7.1)

The maximum depth of the compression zone, c_b , is calculated based on the compressive strength of the concrete and the tensile steel tension using the following equation (TS 7.1):

$$c_b = \frac{\varepsilon_{cu} E_s}{\varepsilon_{cu} E_s + f_{yd}} d$$
(TS 7.1)

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The maximum allowable depth of the rectangular compression block, a_{max} , is given by

$$a_{\max} = 0.85k_1c_b$$
 (TS 7.11, 7.3, Eqn. 7.4)

where k_1 is calculated as follows:

$$k_l = 0.85 - 0.006 (f_{ck} - 25), \quad 0.70 \le k_l \le 0.85.$$
 (TS 7.1, Table 7.1)



Figure 17-1 Uniform Thickness Slab Design

• If $a \le a_{\text{max}}$, the area of tension reinforcement is then given by:

$$A_{s} = \frac{M_{d}}{f_{yd} \left(d - \frac{a}{2} \right)}$$

This reinforcement is to be placed at the bottom if M_d is positive, or at the top if M_d is negative.

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- If $a > a_{\text{max}}$, compression reinforcement is required (TS 7.1) and is calculated as follows:
 - The compressive force developed in the concrete alone is given by:

$$C = 0.85 f_{cd} b a_{max},$$
 (TS 7.1)

and the moment resisted by concrete compression and tension reinforcement is:

$$M_{dc} = C \left(d - \frac{a_{\max}}{2} \right).$$

- Therefore the moment required to be resisted by compression reinforcement and tension reinforcement is:

$$M_{ds} = M_d - M_{dc}.$$

- The required compression reinforcement is given by:

$$A'_{s} = \frac{M_{ds}}{\left(\sigma'_{s} - 0.85f_{cd}\right)\left(d - d'\right)}, \text{ where}$$
$$\sigma'_{s} = E_{s}\varepsilon_{cu} \left[\frac{c_{\max} - d'}{c_{\max}}\right] \le f_{yd}. \tag{TS 7.1}$$

- The required tension reinforcement for balancing the compression in the concrete is:

$$A_{s1} = \frac{M_{ds}}{f_{yd} \left[d - \frac{a_{\max}}{2} \right]},$$

and the tension reinforcement for balancing the compression reinforcement is given by:

$$A_{s2} = \frac{M_{ds}}{f_{yd} \left(d - d' \right)}$$

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Therefore, the total tension reinforcement is $A_s = A_{s1} + A_{s2}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top if M_d is positive, and vice versa if M_d is negative.

17.5.1.2.2 Design of nonuniform thickness slab

In designing a flanged-shaped section, a simplified stress block, as shown in Figure 17-2, is assumed if the flange is under compression, i.e., if the moment is positive. If the moment is negative, the flange comes under tension, and the flange is ignored. In that case, a simplified stress block similar to that shown in Figure 17-1 is assumed on the compression side.



Figure 17-2 Nonuniform Thickness Slab Design

17.5.1.2.2.1 Flanged Slab Section Under Negative Moment

In designing for a factored negative moment, M_d (i.e., designing top reinforcement), the calculation of the reinforcement area is exactly the same as described previously, i.e., no flanged data is used.

17.5.1.2.2.2 Flanged Slab Section Under Positive Moment

If $M_d > 0$, the depth of the compression block is given by:

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$$a = d - \sqrt{d^2 - \frac{2M_d}{0.85f_{cd}b_f}}$$

The maximum depth of the compression zone, c_b , is calculated based on the compressive strength of the concrete and the tensile steel tension using the following equation (TS 7.1):

$$c_b = \frac{\varepsilon_c E_s}{\varepsilon_{cu} E_s + f_{yd}} d \tag{TS 7.1}$$

The maximum allowable depth of the rectangular compression block, a_{max} , is given by

$$a_{\max} = 0.85k_1c_b$$
 (TS 7.11, 7.3, Eqn. 7.4)

where k_1 is calculated as follows:

$$k_1 = 0.85 - 0.006 (f_{ck} - 25), \quad 0.70 \le k_1 \le 0.85.$$
 (TS 7.1, Table 7.1)

- If a ≤ d_s, the subsequent calculations for A_s are exactly the same as previously defined for the uniform thickness slab section design. However, in that case, the width of the slab is taken as b_f, as shown in Figure 17-2. Compression reinforcement is required if a > a_{max}.
- If *a* > *d_s*, the calculation for *A_s* has two parts. The first part is for balancing the compressive force from the flange, *C_f*, and the second part is for balancing the compressive force from the web, *C_w*, as shown in Figure 17-2. *C_f* is given by:

$$C_f = 0.85 f_{cd} \left(b_f - b_w \right) \times \min\left(d_s, a_{\max} \right)$$
(TS 7.1)

Therefore, $A_{s1} = \frac{C_f}{f_{yd}}$ and the portion of M_d that is resisted by the flange is

given by:

$$M_{df} = C_f \left(d - \frac{\min(d_s, a_{\max})}{2} \right)$$

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Therefore, the balance of the moment, M_d , to be carried by the web is given by:

$$M_{dw} = M_d - M_{df}$$

The web is a rectangular section of dimensions b_w and d, for which the design depth of the compression block is recalculated as:

$$a_1 = d - \sqrt{d^2 - \frac{2M_{dw}}{0.85f_{cd} \ b_w}}$$
(TS 7.1)

• If $a_1 \le a_{max}$ (TS 7.1), the area of tensile steel reinforcement is then given by:

$$A_{s2} = \frac{M_{dw}}{f_{yd} \left(d - \frac{a_1}{2} \right)}, \text{ and}$$

$$A_s = A_{s1} + A_{s2}$$

This steel is to be placed at the bottom of the T-shaped section.

• If $a_1 > a_{\text{max}}$, compression reinforcement is required and is calculated as follows:

The compression force in the web concrete alone is given by:

$$C = 0.85 f_{cd} b_w a_{max}$$
 (TS 7.1)

Therefore the moment resisted by the concrete:

$$M_{dc} = C\left(d - \frac{a_{\max}}{2}\right),$$

The tensile steel for balancing compression in the web concrete is:

$$A_{s2} = \frac{M_{dc}}{f_{yd} \left[d - \frac{a_{\max}}{2} \right]},$$

The moment resisted by compression steel and tensile steel is:

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$$M_{ds} = M_{dw} - M_{dc}$$

Therefore, the compression steel is computed as:

$$A'_{s} = \frac{M_{ds}}{\left(\sigma'_{s} - 0.85f_{cd}\right)\left(d - d'\right)}, \text{ where}$$
$$\sigma'_{s} = E_{s}\varepsilon_{cu} \left[\frac{c_{\max} - d'}{c_{\max}}\right] \le f_{yd}, \text{ and} \qquad (\text{TS 7.1})$$

the tensile steel for balancing the compression steel is:

$$A_{s3} = \frac{M_{ds}}{f_{yd} \left(d - d' \right)}$$

The total tensile reinforcement is $A_s = A_{s1} + A_{s2} + A_{s3}$, and the total compression reinforcement is A'_s . A_s is to be placed at the bottom and A'_s is to be placed at the top.

17.5.1.2.3 Minimum and Maximum Tensile Reinforcement

The minimum flexural tension reinforcement required for each direction of a slab is given by the following limits (TS 11.4.5):

$$A_{s,\min} = 0.0020 \ bh \ \text{for steel grade S220} \tag{TS 11.4.5}$$

$$A_{s,\min} = 0.00175 \ bh \ for \ steel \ grade \ S420 \ and \ S500$$
 (TS 11.4.5)

In addition, an upper limit on both the tension reinforcement and compression reinforcement has been imposed to be 0.04 times the gross cross-sectional area.

17.5.2 Design Slab Shear Reinforcement

The shear reinforcement is designed for each load combination at each station along the design strip. In designing the shear reinforcement for a particular strip, for a particular load combination, at a particular station due to the slab major shear, the following steps are involved:

- Determine the factored shear force, V_d.
- Determine the shear force, V_c , that can be resisted by the concrete.
- Determine the shear reinforcement required to carry the balance.

The following three sections describe in detail the algorithms associated with these steps.

17.5.2.1 Determine Factored Shear Force

In the design of the slab shear reinforcement, the shear forces for each load combination at a particular design strip station are obtained by factoring the corresponding shear forces for different load cases, with the corresponding load combination factors.

17.5.2.2 Determine Concrete Shear Capacity

Given the design force set N_d and V_d , the shear force carried by the concrete, V_c , is calculated as follows:

• If the slab is subjected to axial loading, *N_d* is positive in this equation regardless of whether it is a compressive or tensile force,

$$V_{cr} = 0.65 f_{ctd} b_w d \left(1 + \frac{\gamma N_d}{A_g} \right),$$
 (TS 8.1.3, Eqn. 8.1)

where,

0.07 for axial compression $\gamma = -0.3$ for axial tension 0 when tensile stress < 0.5 MPa

$$V_c = 0.8V_{cr}$$
, (TS 8.1.4, Eqn. 8.4)

17.5.2.3 Determine Required Shear Reinforcement

Given V_d and V_c , the required shear reinforcement in the form of stirrups or ties within a spacing, *s*, is given for rectangular and circular columns by the following:

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• The shear force is limited to a maximum of

$$V_{\rm max} = 0.22 f_{cd} A_w$$
 (TS 8.1.5b)

• The required shear reinforcement per unit spacing, A_v / s , is calculated as follows:

If
$$V_d \leq V_{cr}$$
,

$$\frac{A_{sw}}{s} = 0.3 \frac{f_{ctd}}{f_{ywd}} b_w,$$
(TS 8.1.5, Eqn. 8.6)

else if $V_{cr} < V_d \le V_{\max}$,

$$\frac{A_{sw}}{s} = \frac{(V_d - V_c)}{f_{ywd}d},$$
 (TS 8.1.4, Eqn. 8.5)

$$\frac{A_{sw}}{s} \ge 0.3 \frac{f_{ctd}}{f_{ywd}} b_w$$
(TS 8.1.5, Eqn. 8.6)

else if $V_d > V_{\text{max}}$,

a failure condition is declared. (TS 8.1.5b)

If V_d exceeds its maximum permitted value V_{max} , the concrete section size should be increased (TS 8.1.5b).

The maximum of all of the calculated A_{sw}/s values, obtained from each design load combination, is reported along with the controlling shear force and associated design load combination name.

The slab shear reinforcement requirements considered by the program are based purely on shear strength considerations. Any minimum stirrup requirements to satisfy spacing and volumetric considerations must be investigated independently of the program by the user.

17.5.3 Check for Punching Shear

The algorithm for checking punching shear is detailed in the section entitled "Slab Punching Shear Check" in the Chapter 1. Only the code-specific items are described in the following sections.

17.5.3.1 Critical Section for Punching Shear

The punching shear is checked on a critical section at a distance of d/2 from the face of the support (TS 8.3.1). For rectangular columns and concentrated loads, the critical area is taken as a rectangular area with the sides parallel to the sides of the columns or the point loads (TS 8.3.1). Figure 17-3 shows the auto punching perimeters considered by ETABS for the various column shapes. The column location (i.e., interior, edge, corner) and the punching perimeter may be overwritten using the Punching Check Overwrites.



Figure 17-3 Punching Shear Perimeters

17.5.3.2 Determine Concrete Capacity

The concrete punching shear stress capacity is taken as the following limit:

$$v_{pr} = f_{ctd} = 0.35 \sqrt{f_{ck}} / \gamma_c$$
 (TS 8.3.1)

17.5.3.3 Computation of Maximum Shear Stress

Given the punching shear force and the fractions of moments transferred by eccentricity of shear, the nominal design shear stress, v_{pd} , is calculated as:

$$v_{pd} = \frac{V_{pd}}{u_p d} \left[1 + \eta \frac{0.4M_{pd,2}u_p d}{V_{pd}W_{m,2}} + \eta \frac{0.4M_{pd,3}u_p d}{V_{pd}W_{m,3}} \right], \text{ where } (\text{TS 8.3.1})$$

 η factor to be used in punching shear check

$$\eta = \frac{1}{1 + \sqrt{b_2 / b_1}}$$
 where $b_2 \ge 0.7b_1$

When the aspect ratio of loaded area is greater than 3, the critical primeter is limited assuming h = 3b

- u_p is the effective perimeter of the critical section
- *d* is the mean effective depth of the slab
- M_{pd} is the design moment transmitted from the slab to the column at the connection along bending axis 2 and 3
- V_{pd} is the total punching shear force
- W_m section modulus of area within critical punching perimeter (u_p) along bending axis 2 and 3.

17.5.3.4 Determine Capacity Ratio

Given the punching shear force and the fractions of moments transferred by eccentricity of shear about the two axes, the shear stress is computed assuming linear variation along the perimeter of the critical section. The ratio of the maximum shear stress and the concrete punching shear stress capacity is reported as the punching shear capacity ratio by ETABS. If this ratio exceeds 1.0, punching shear reinforcement is designed as described in the following section.

17.5.4 Design Punching Shear Reinforcement

The use of shear studs as shear reinforcement in slabs is permitted, provided that the slab thickness is greater than or equal to 250 mm, a (TS 8.3.2). If the slab thickness does not meet these requirements, the punching shear reinforcement is not designed and the slab thickness should be increased by the user.

The algorithm for designing the required punching shear reinforcement is used when the punching shear capacity ratio exceeds unity. The *Critical Section for Punching Shear* and *Transfer of Unbalanced Moment* as described in the earlier sections remain unchanged. The design of punching shear reinforcement is described in the subsections that follow.

17.5.4.1 Determine Concrete Shear Capacity

The concrete punching shear stress capacity of a section with punching shear reinforcement is limited to:

$$v_{pr} = f_{ctd} = 0.35 \sqrt{f_{ck} / \gamma_c}$$
 (TS 8.3.1)

17.5.4.2 Determine Required Shear Reinforcement

The shear force is limited to a maximum of:

$$v_{pr,\text{max}} = 1.5\gamma f_{ctd} = 0.525\gamma \sqrt{f_{ck}} / \gamma_c$$
 for shear links/shear studs (TS 8.3.1)

Given V_{pd} , V_{pr} , and $V_{pr,max}$, the required shear reinforcement is calculated as follows,

$$\frac{A_{v}}{s} = \frac{\left(V_{pd} - V_{pr}\right)}{f_{yd}d}$$
(TS8.1.4)

- If $V_{pd} > V_{pr,max}$, a failure condition is declared. (TS 8.3.1)
- If *V_{pd}* exceeds the maximum permitted value of *V_{pr,max}*, the concrete section should be increased in size.

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17.5.4.3 Determine Reinforcement Arrangement

Punching shear reinforcement in the vicinity of rectangular columns should be arranged on peripheral lines, i.e., lines running parallel to and at constant distances from the sides of the column. Figure 17-4 shows a typical arrangement of shear reinforcement in the vicinity of a rectangular interior, edge, and corner column.

NOTE: Shear Stud and shear links requirements are computed based on ACI 318-08 code as Turkish TS 500-2000 refers to special literature on this topic.



Figure 17-4 Typical arrangement of shear studs and critical sections outside shear-reinforced zone

The distance between the column face and the first line of shear reinforcement shall not exceed d/2(ACI R11.3.3, 11.11.5.2. The spacing between adjacent shear reinforcement in the first line (perimeter) of shear reinforcement shall not exceed 2*d* measured in a direction parallel to the column face (ACI 11.11.3.3).

Punching shear reinforcement is most effective near column corners where there are concentrations of shear stress. Therefore, the minimum number of lines of shear reinforcement is 4, 6, and 8, for corner, edge, and interior columns respectively.

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17.5.4.4 Determine Reinforcement Diameter, Height, and Spacing

The punching shear reinforcement is most effective when the anchorage is close to the top and bottom surfaces of the slab. The cover of anchors should not be less than the minimum cover specified in ACI 7.7 plus half of the diameter of the flexural reinforcement.

Punching shear reinforcement in the form of shear studs is generally available in 10-, 12-, 14-, 16-, and 20-millimeter diameters.

When specifying shear studs, the distance, s_o , between the column face and the first peripheral line of shear studs should not be smaller than 0.5*d*. The spacing between adjacent shear studs, *g*, at the first peripheral line of studs shall not exceed 2*d*, and in the case of studs in a radial pattern, the angle between adjacent stud rails shall not exceed 60 degrees. The limits of s_o and the spacing, *s*, between the peripheral lines are specified as:

$$s_o \le 0.5d$$
 (ACI 11.11.5.2)

$$s \leq \begin{cases} 0.75d & \text{for} & v_{u} \leq 6\phi\lambda\sqrt{f_{c}'} \\ 0.50d & \text{for} & v_{u} > 6\phi\lambda\sqrt{f_{c}'} \end{cases}$$
(ACI 11.11.5.2)
$$g \leq 2d$$
(ACI 11.11.5.3)

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The limits of s_o and the spacing, s, between for the links are specified as:

$s_o \leq 0.5d$	(ACI 11.11.3)

$$s \le 0.50d$$
 (ACI 11.11.3)

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